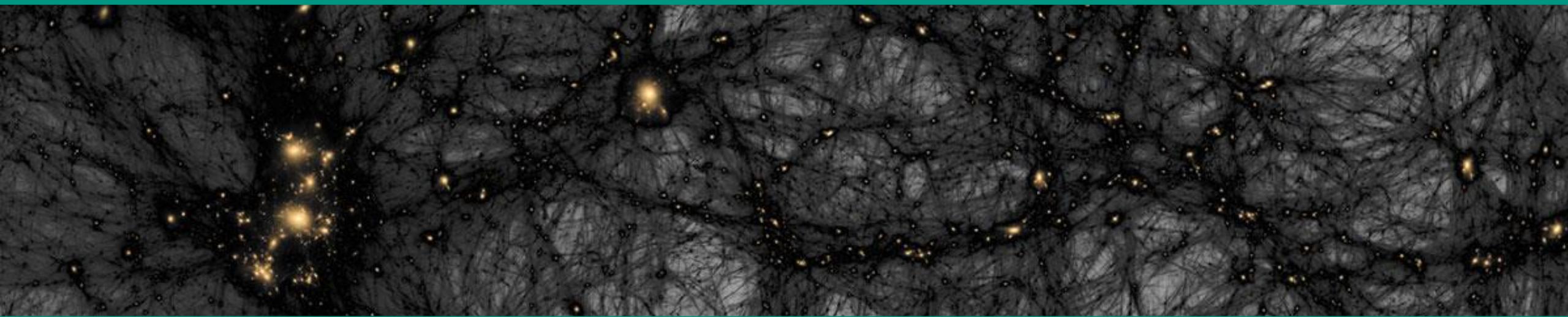


Astroparticle physics I – Dark Matter

WS22/23 Lecture 11

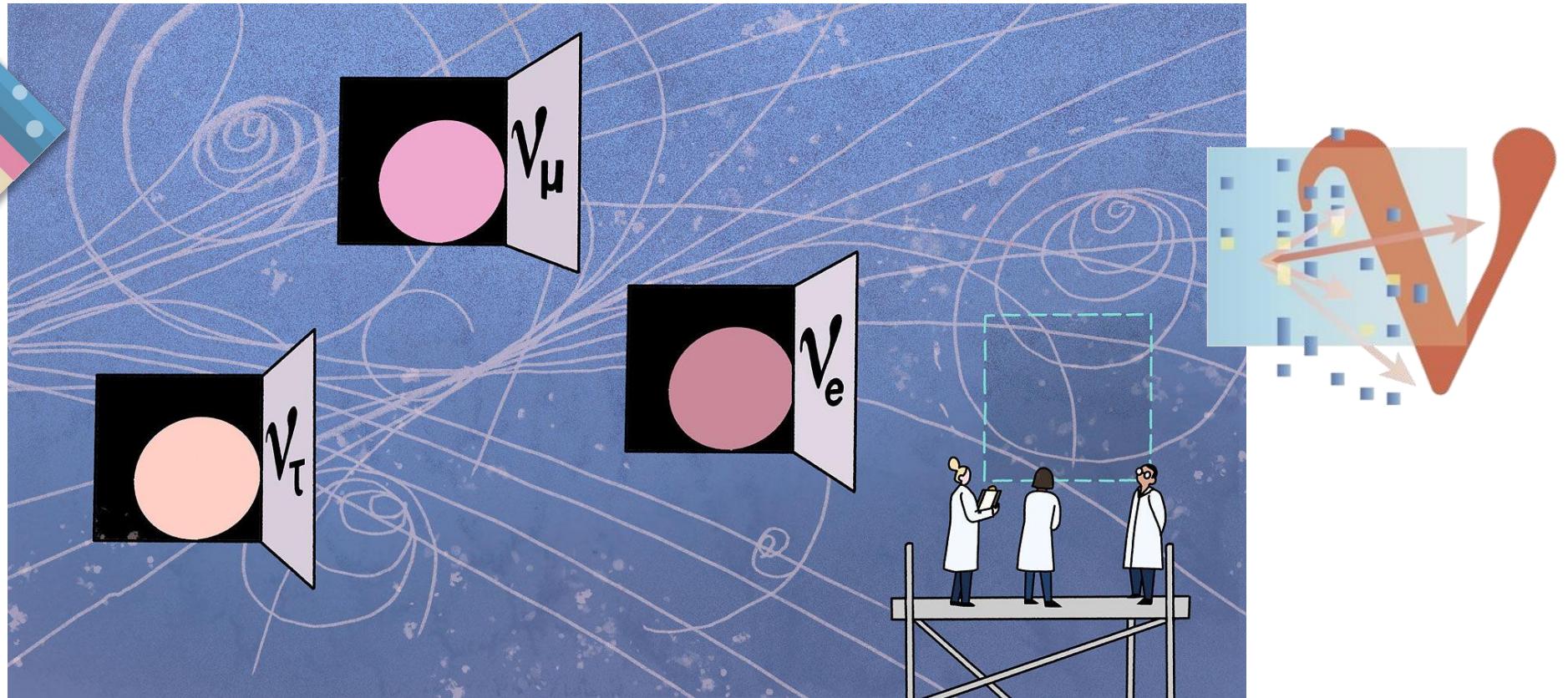
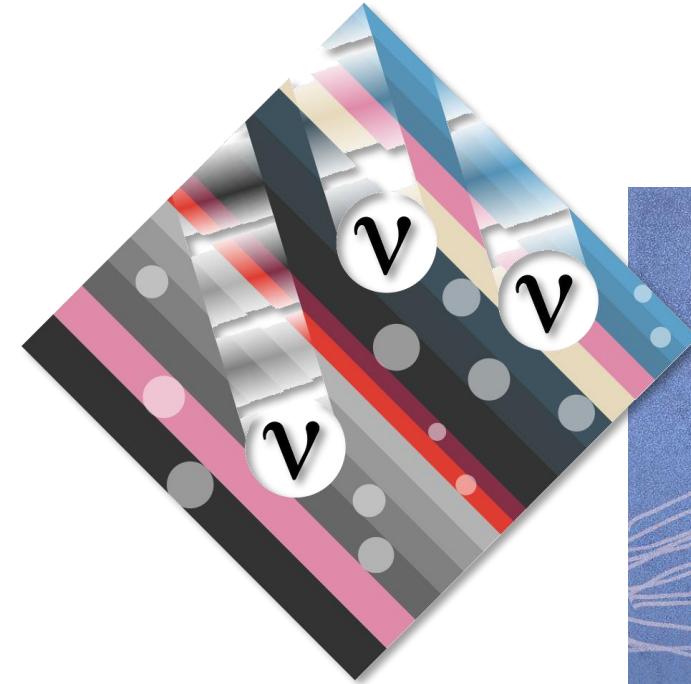
Dec. 8, 2022



Recap of Lecture 10

■ Shielding against background and origin of background processes

- reduction of μ –induced processes via underground lab (**LNGS**,...)
- shielding against gammas from rock: veto, Pb – bricks, PE, high-purity Cu
- 4 primordial decay chains: ^{232}Th , ^{235}U , ^{237}Np , ^{238}U
- usually the entire chain is in **secular equilibrium** (all A_j identical)
- important isotope: ^{210}Pb (Roman- Pb or electro-formed Cu)
- **radon**: ^{222}Rn ^{220}Rn especially dangerous due to emanation in closed spaces



CHAPTER 3 – NEUTRINOS

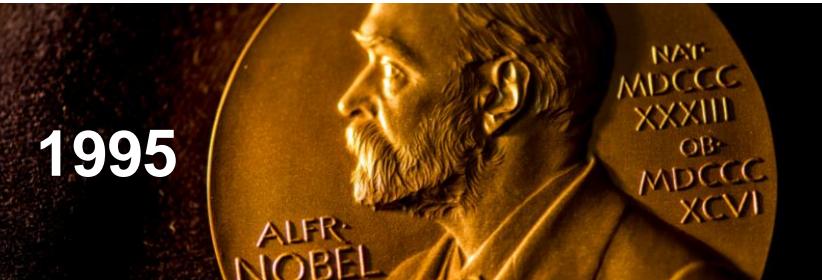
3.1 Introduction

■ Experimental starting point: Fred Reines on the track of neutrinos

- project '*Poltergeist*': first detection of neutrinos (Savannah River reactor)

Hanford 1954: first (unsuccessful) neutrino detector '*Herr Auge*'

300 ℓ liquid scintillator with 90 PMTs!



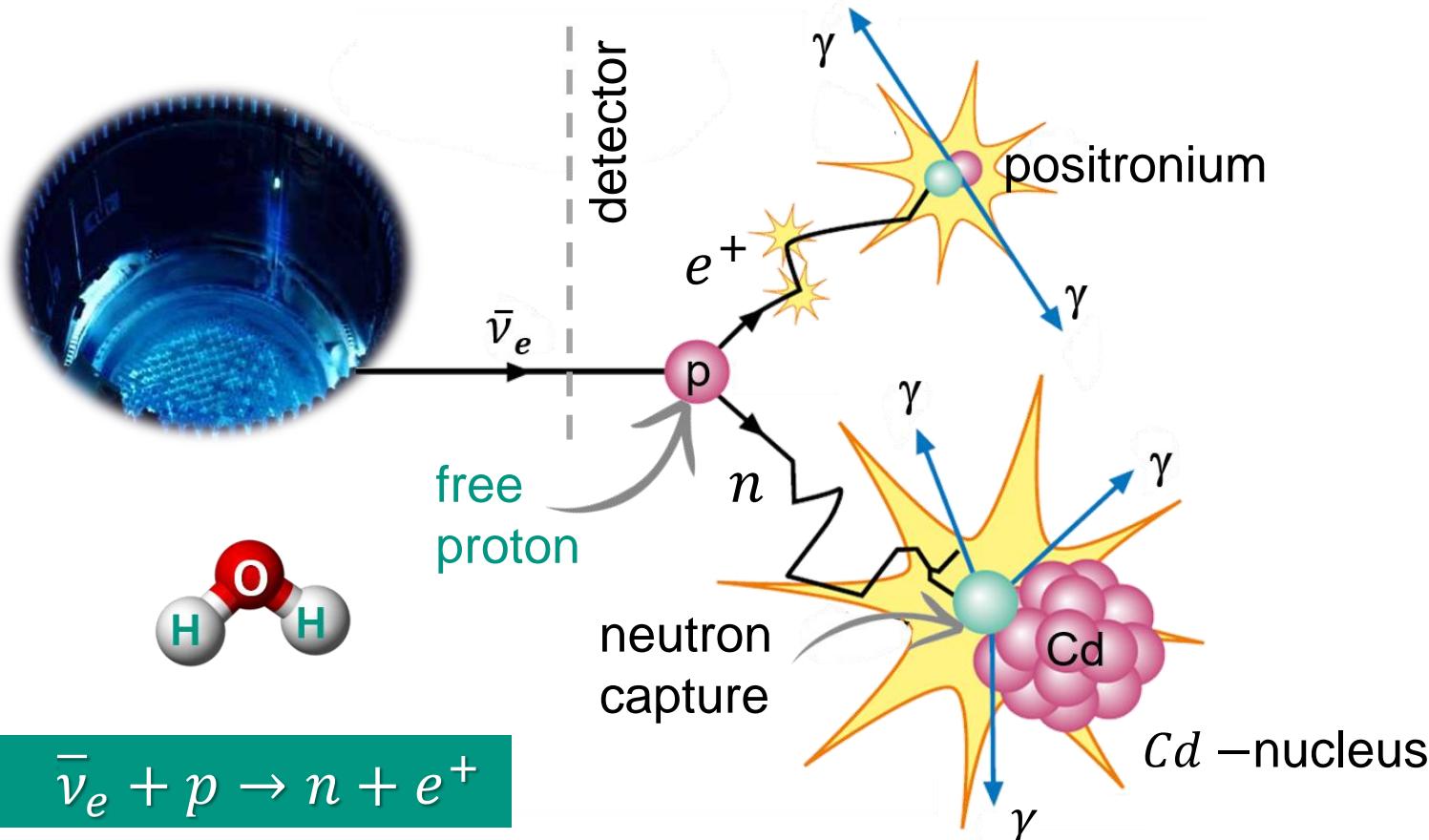
"for the detection of the *neutrino*"

Fred Reines
1918 – 1998



Inverse β^- decay: 'classical' detection reaction

- A unique 'delayed coincidence' signature: **prompt e^+ & delayed (n, γ)**



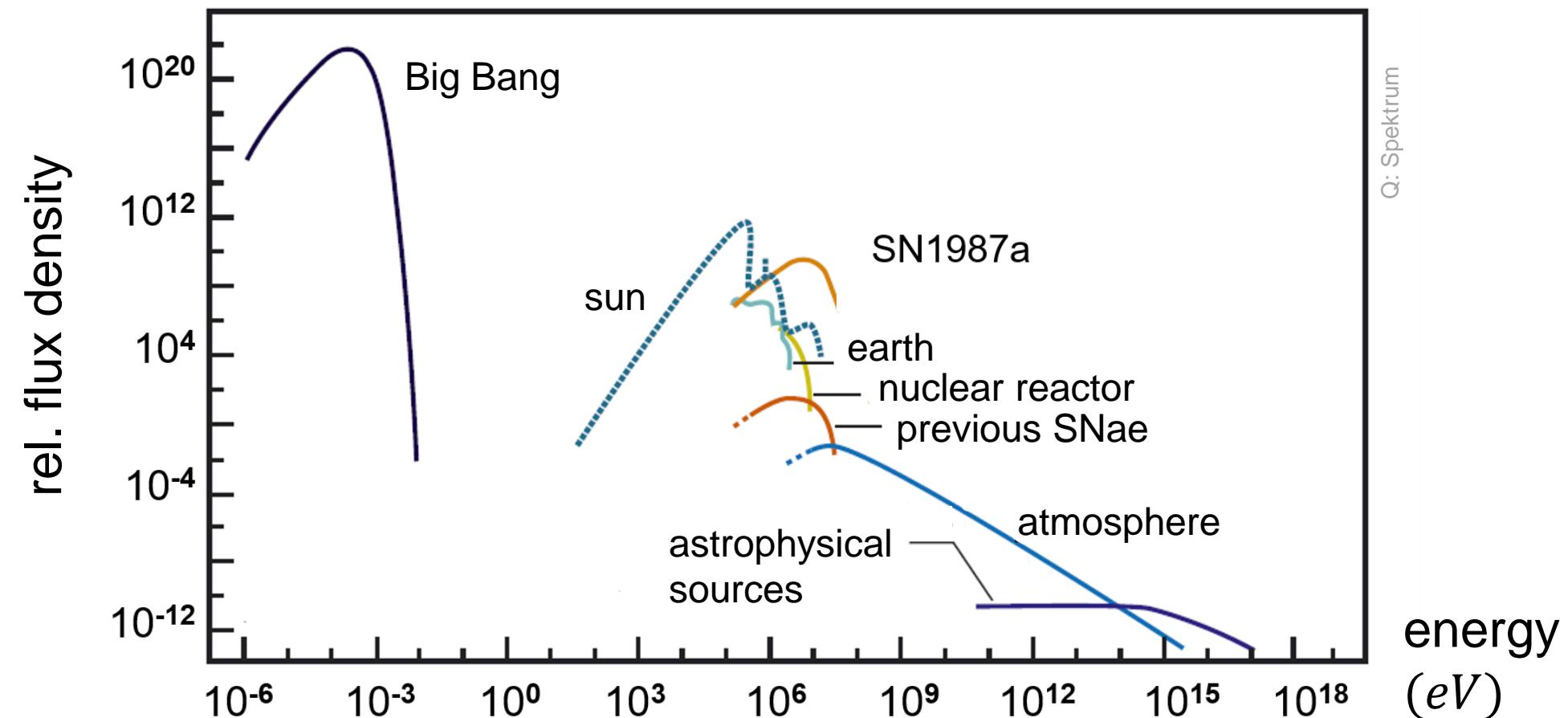
positronium:
annihilation of e^+ and e^- into
two γ 's ($2 \times 511 \text{ keV}$)

coincidence of the 2 signals

neutron-capture (nucleus):
several γ 's , release of the $n -$
binding energy ($\Sigma E_\gamma \sim 7 - 8 \text{ MeV}$)

Neutrino sources: an overview from μeV ... PeV

■ sources: from primordial ν 's to astrophysical ν 's from AGNs...

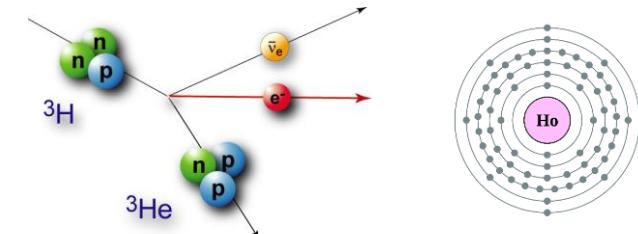


3.2 kinematic determination of the ν – mass

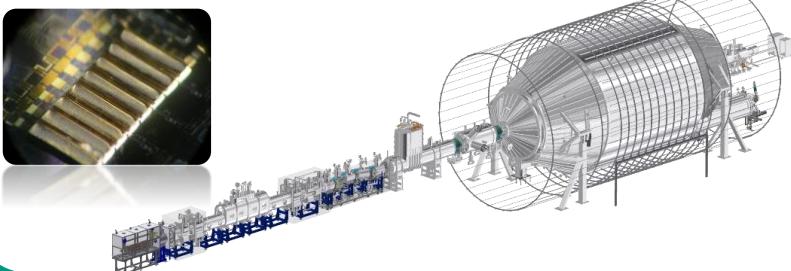
■ three complementary approaches: laboratory-based & cosmology

kinematics of weak decays

- β –decay: 3H , EC: ${}^{163}Ho$
- **model-independent**

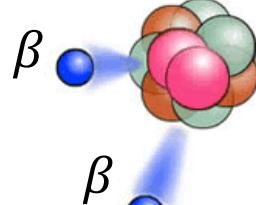


$$m(\nu_e) = \sqrt{\sum_{i=1}^3 |U_{ei}|^2 \cdot m_i^2}$$

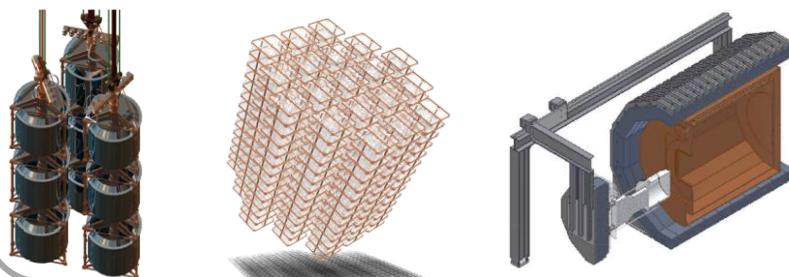


search for $0\nu\beta\beta$ – decay

- $\beta\beta$ –decay: ${}^{76}Ge$, ${}^{136}Xe$, ...
- model-dependent (α_i)

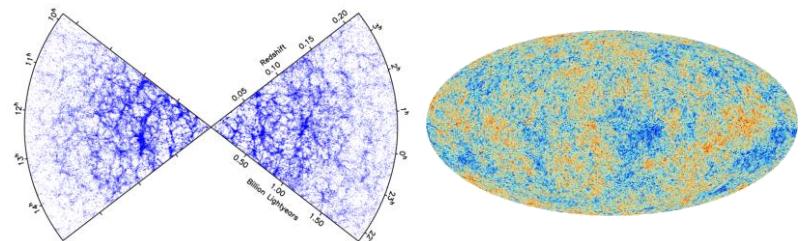


$$\langle m_{\beta\beta} \rangle = \left| \sum_{i=1}^3 U_{ei}^2 \cdot m_i \right|$$

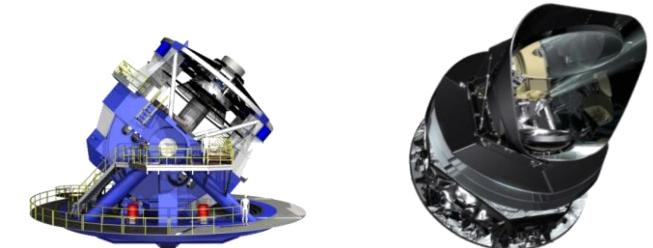


large-scale structures

- CMB, galaxy surveys, ...
- model-dependent (H_0)



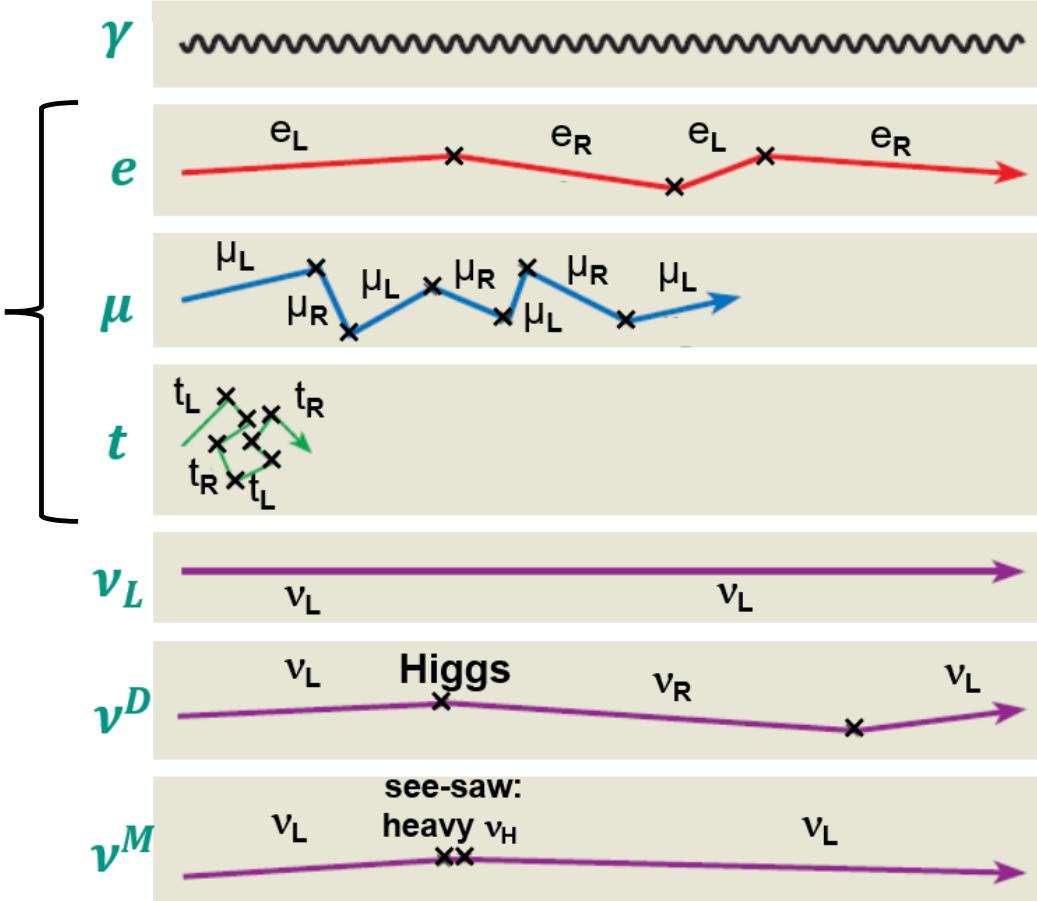
$$m_{tot} = \sum_{i=1}^3 m_i$$



Neutrinos – intrinsic properties

Higgs vs. see-saw* mechanism

masses m_i
via Higgs-
coupling, but
change of the
handedness



chiral LH
 \leftrightarrow chiral RH

particle	scale	$m(MeV)$
photon γ	massless	0
electron e	light	0.511
muon μ	medium	105.6
top quark t	heavy	$1.71 \cdot 10^5$
SM neutrino ν_L	massless	0
Dirac-ν ν^D	very light	$10^{-8} \dots 10^{-6}$
Majorana-ν ν^M	very light	$10^{-8} \dots 10^{-6}$

Neutrinos: Dirac- or Majorana-type

Dirac Neutrino

4ν – states

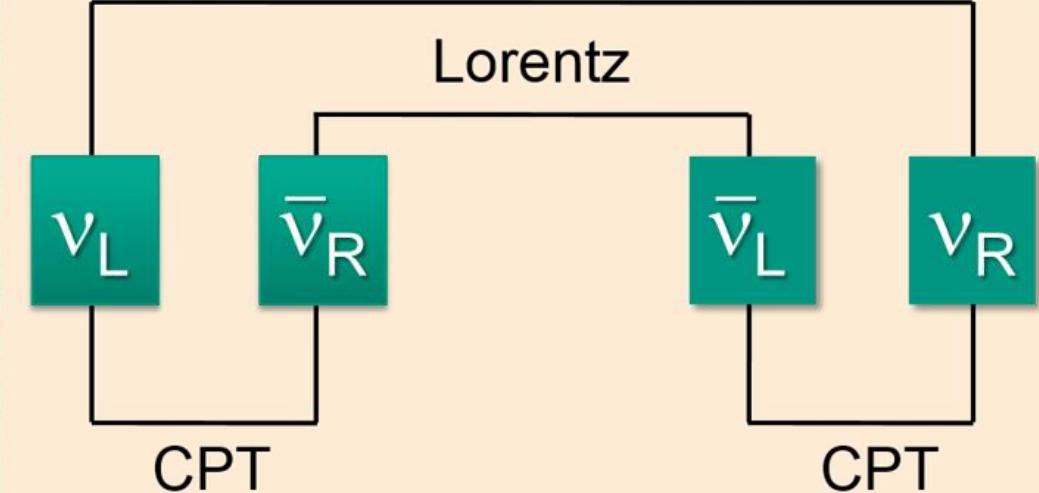
Lepton number conservation

$$\Delta L = 0$$

neutrino \neq anti-neutrino



ν^D



Majorana Neutrino

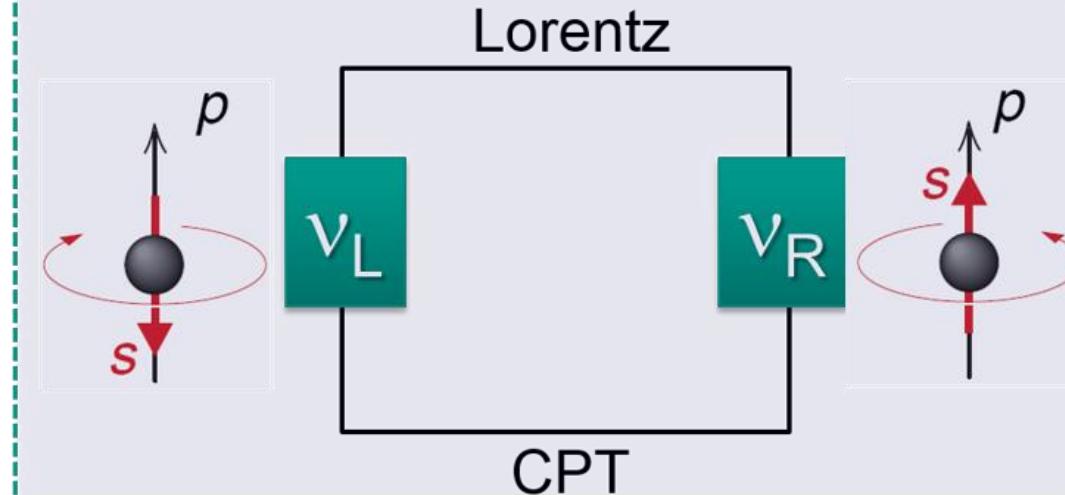
2ν – states

Lepton number violation

$$\Delta L = 2$$



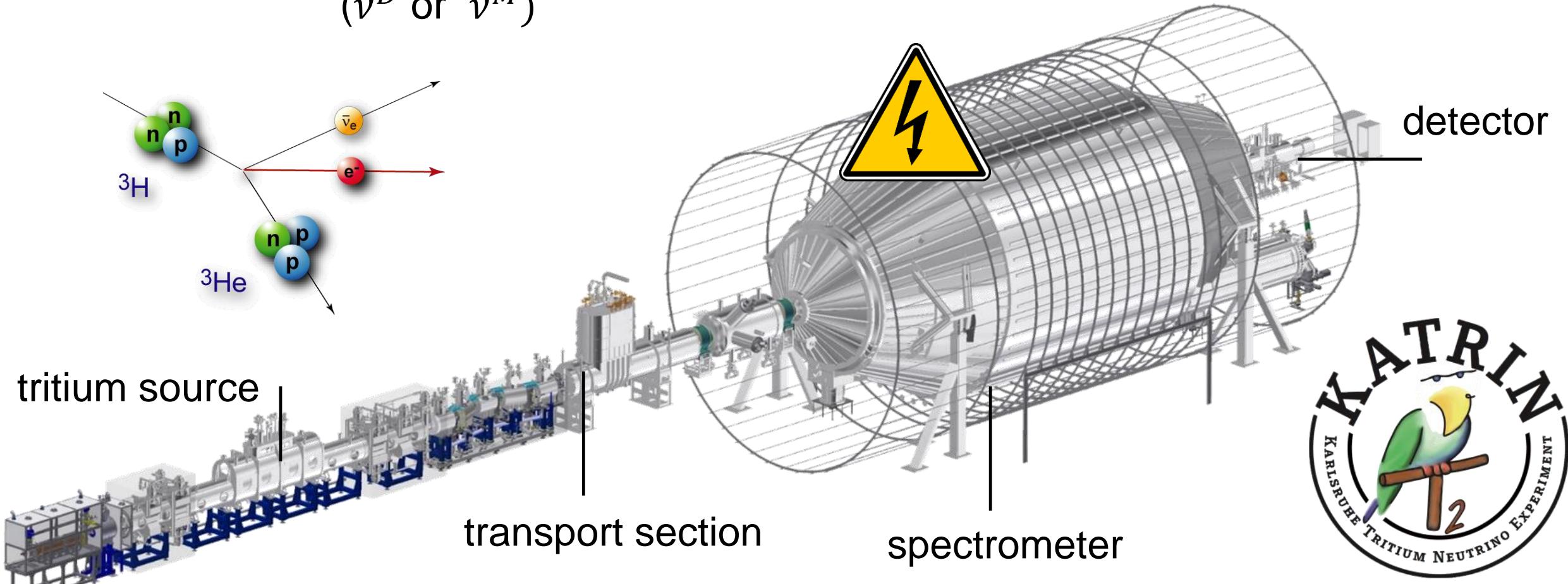
ν^M



KATRIN neutrino mass experiment

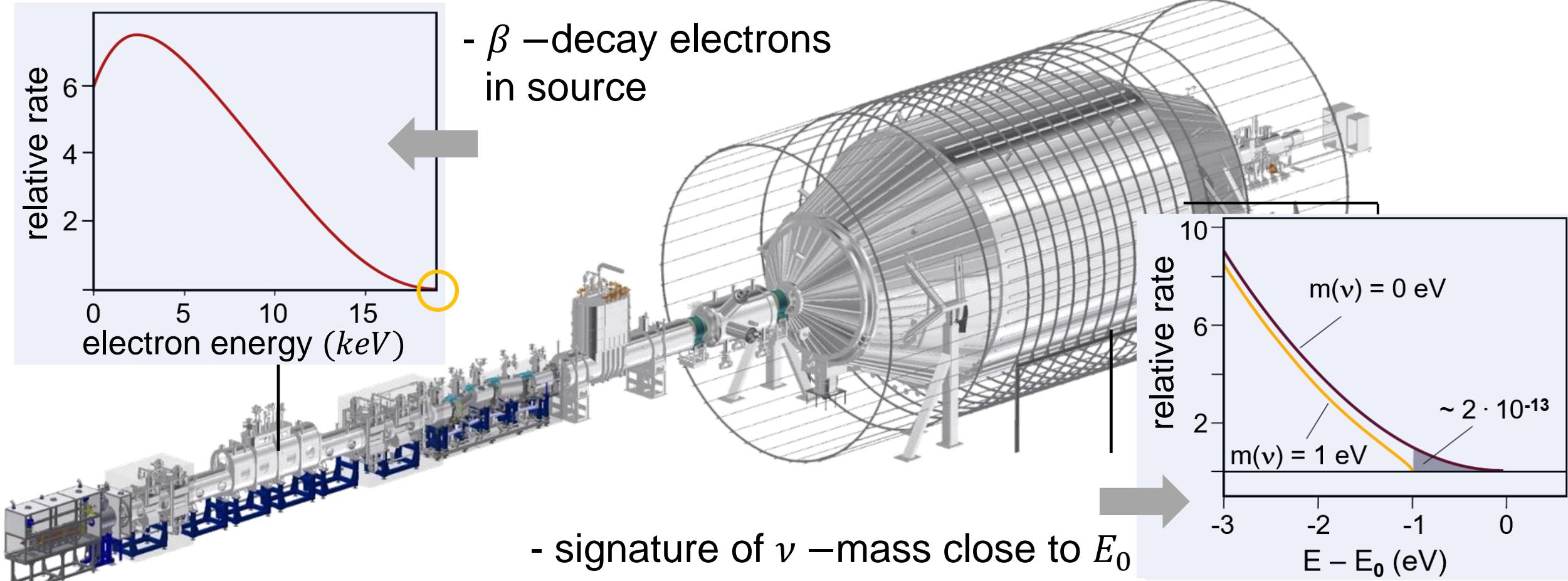
■ direct, model-independent measurement of the fundamental ν –mass scale

(ν^D or ν^M)



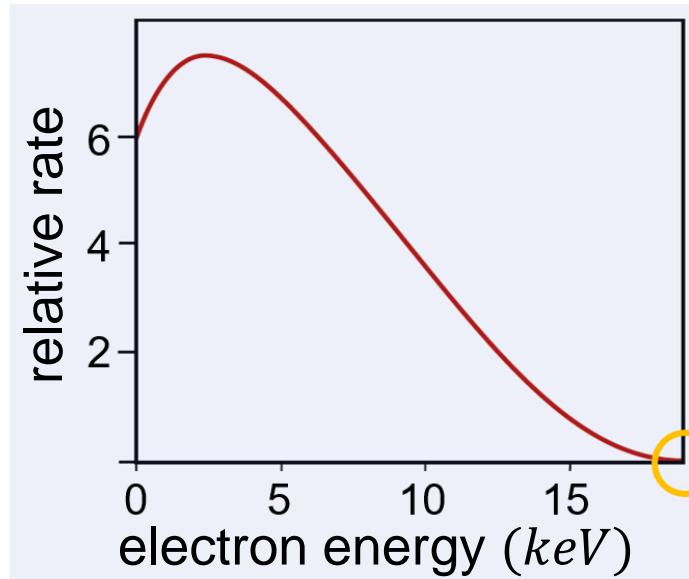
KATRIN neutrino mass experiment

- $10^{11} \beta^-$ -decays from a molecular, gaseous T_2 source at cryogenic $T \sim 80\text{ K}$



KATRIN neutrino mass experiment

- Fermi theory of β – decay: **kinematic variables** only to describe spectrum



electron:

momentum p , energy E , mass m_e

neutrino:

3 mass eigenstates m_i

phase space:

maximum energy E_0

final state interaction:

Fermi function $F(E, Z)$



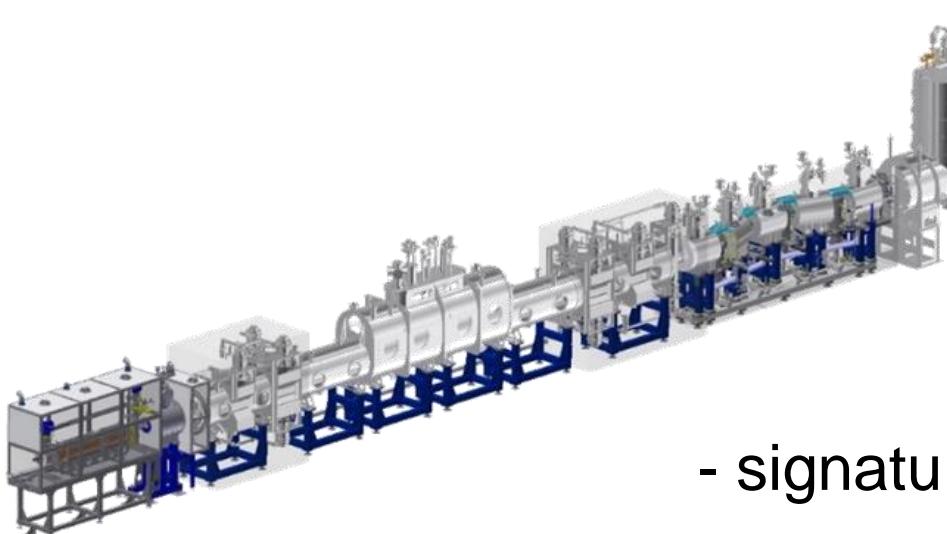
$$\frac{d\Gamma_i}{dE} = C \cdot p \cdot (E + m_e) \cdot (E_0 - E) \cdot \sqrt{(E_0 - E)^2 - m_i^2} \cdot F(E, Z) \cdot \theta(E_0 - E - m_i)$$

KATRIN neutrino mass experiment

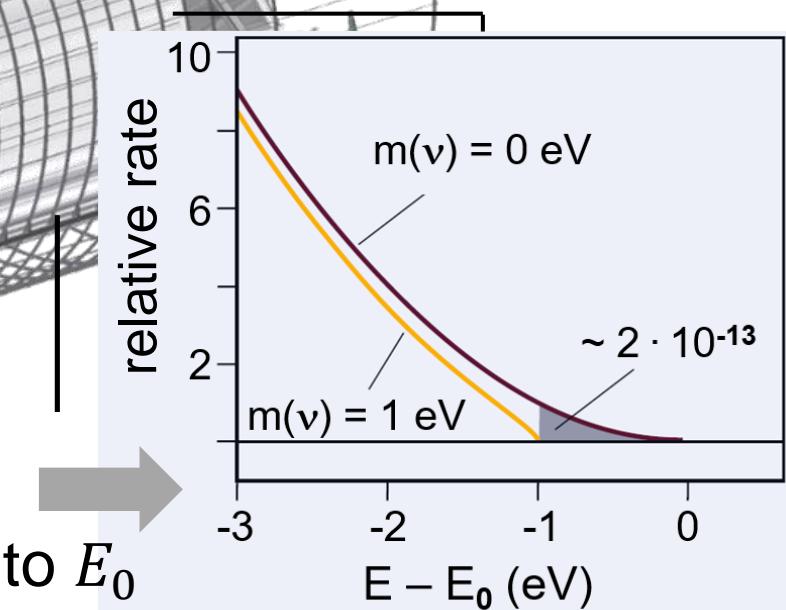
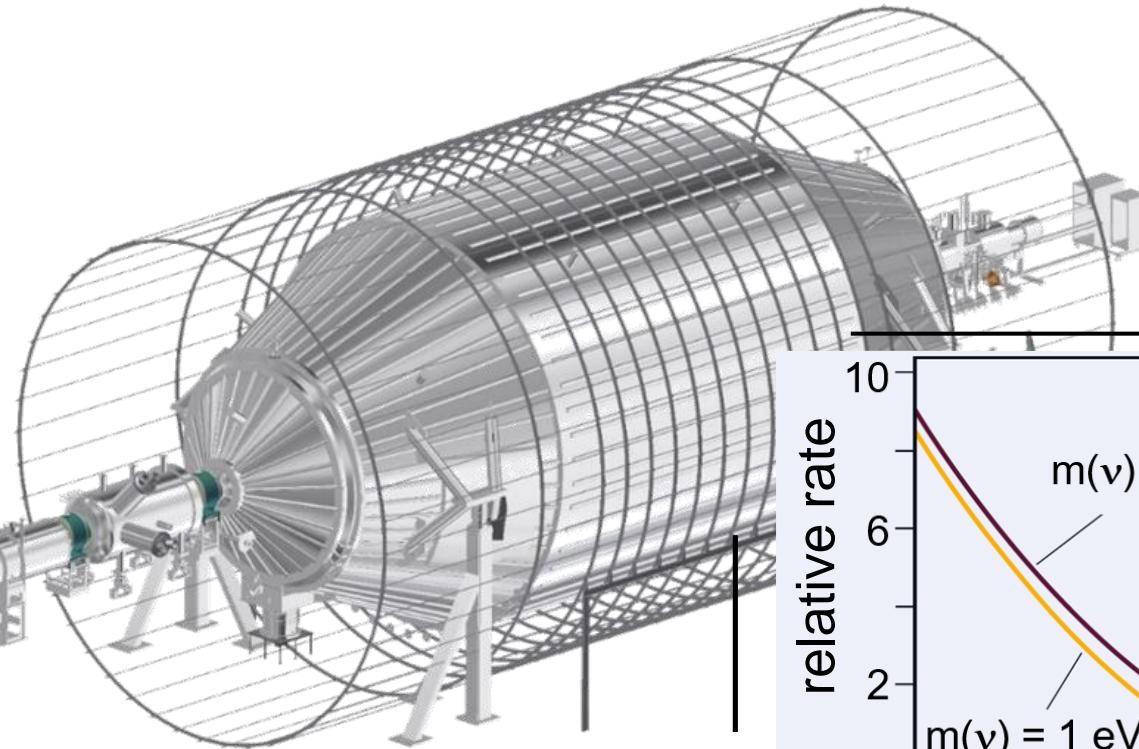
- 'effective mass' of the electron neutrino ν_e : incoherent sum of masses m_i

$$m(\nu_e) = \sqrt{\sum_{i=1}^3 |U_{ei}|^2 \cdot m_i^2}$$

'effective electron neutrino mass'

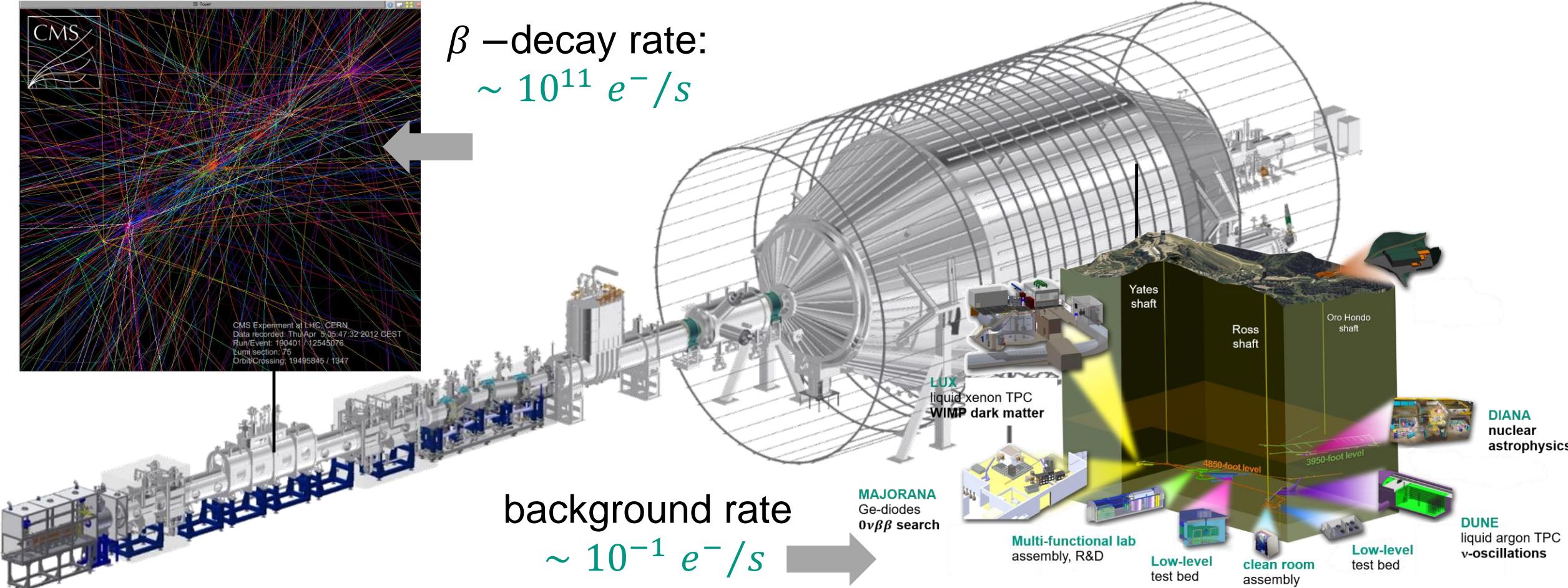


- signature of ν -mass $m(\nu_e)$ close to E_0



KATRIN neutrino mass experiment

■ challenges: combining a huge rate (*LHC-equiv.*) with low-level technologies



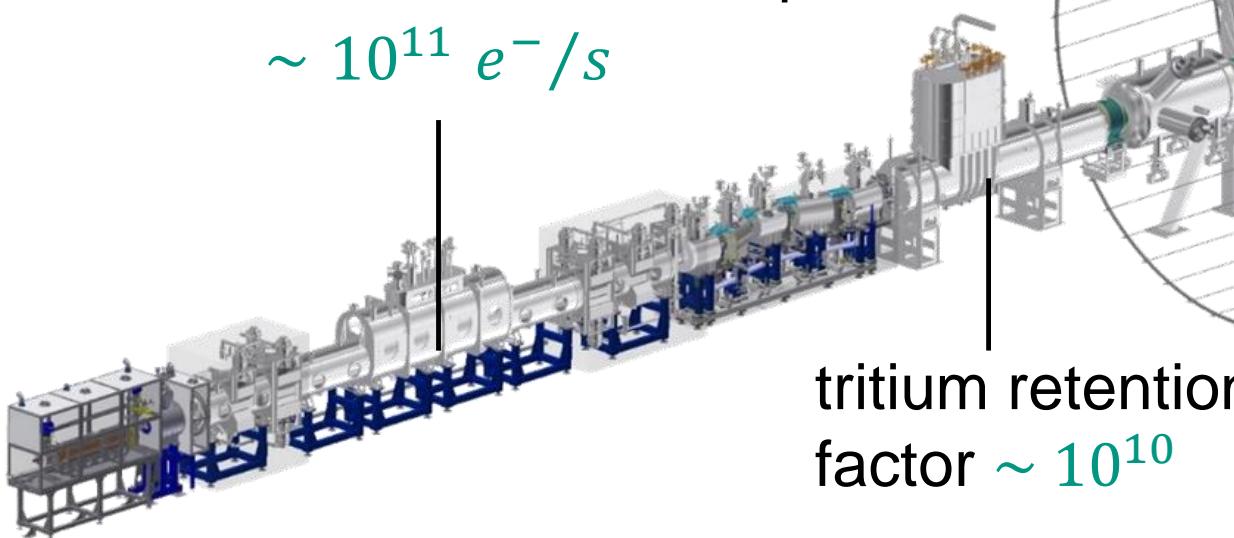
KATRIN neutrino mass experiment – challenges

- precision spectroscopy (*sub – eV*) of β –decay electrons (*keV – scale*)

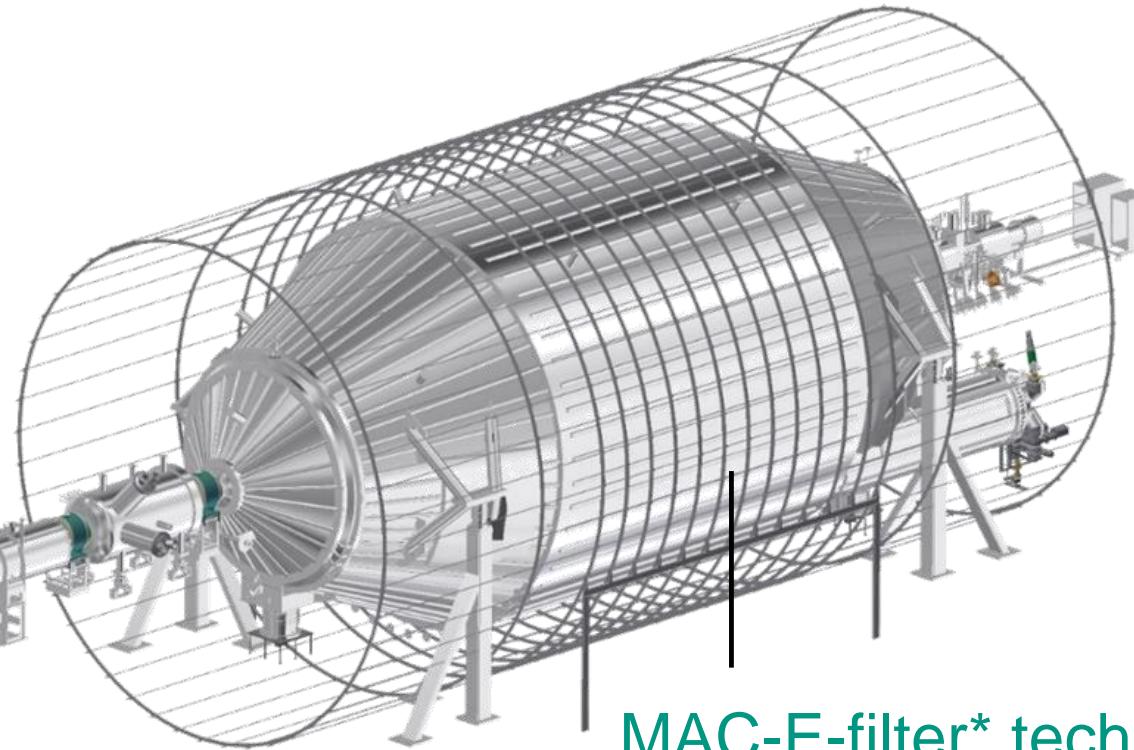
CHALLENGE
ACCEPTED

adiabatic electron transport:

$$\sim 10^{11} \text{ } e^-/\text{s}$$



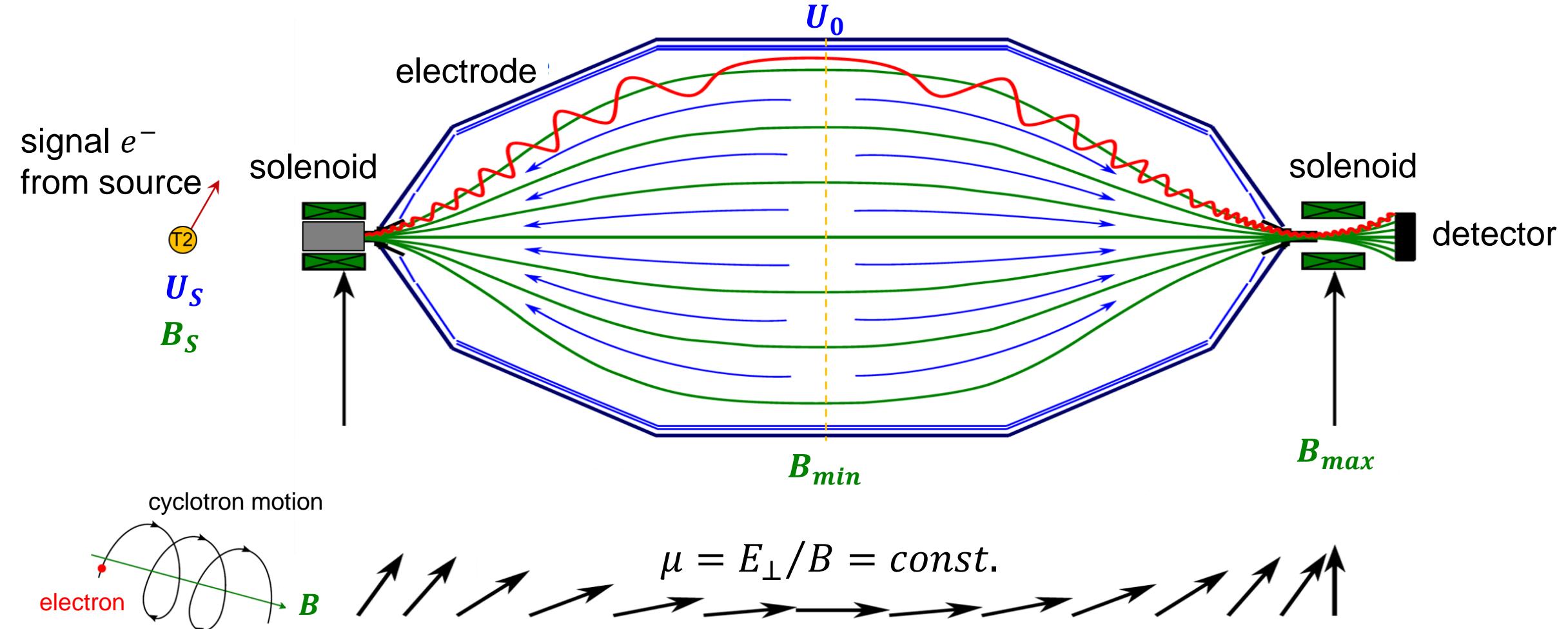
tritium retention
factor $\sim 10^{10}$



MAC-E-filter* technology:
- large angular acceptance
- very narrow filter width

KATRIN neutrino mass experiment – principle

■ MAC-E filter: Magnetic Adiabatic Collimation with Energy filter



KATRIN – measurement principle & strategy

■ measurement: integrated rate above spectrometer retarding potential U_0

- calendar year:

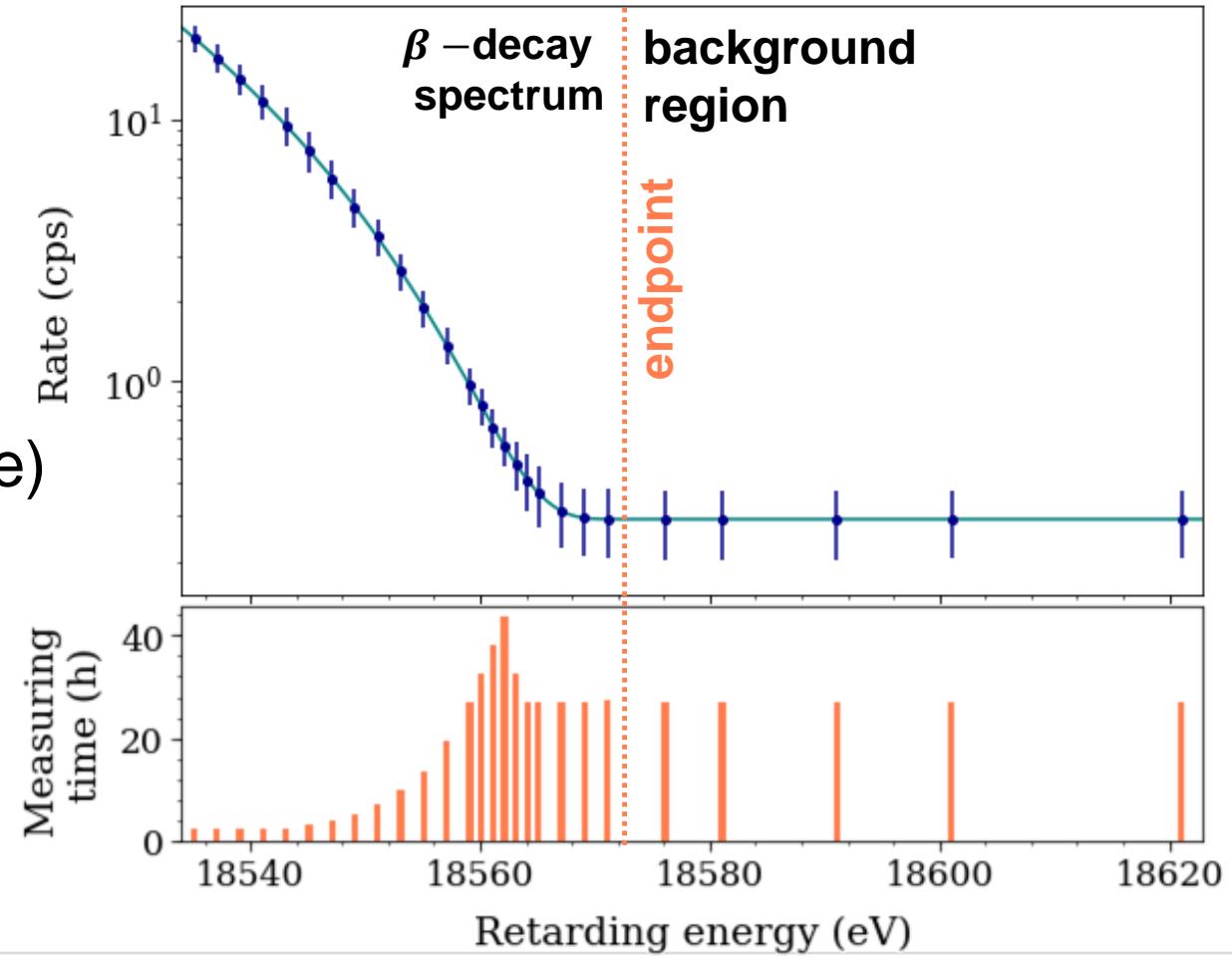
several measurement campaigns
(KNM x), typically 4 – 5

- campaign:

several (up to 8) weeks
hundreds of β – scans (up-down mode)

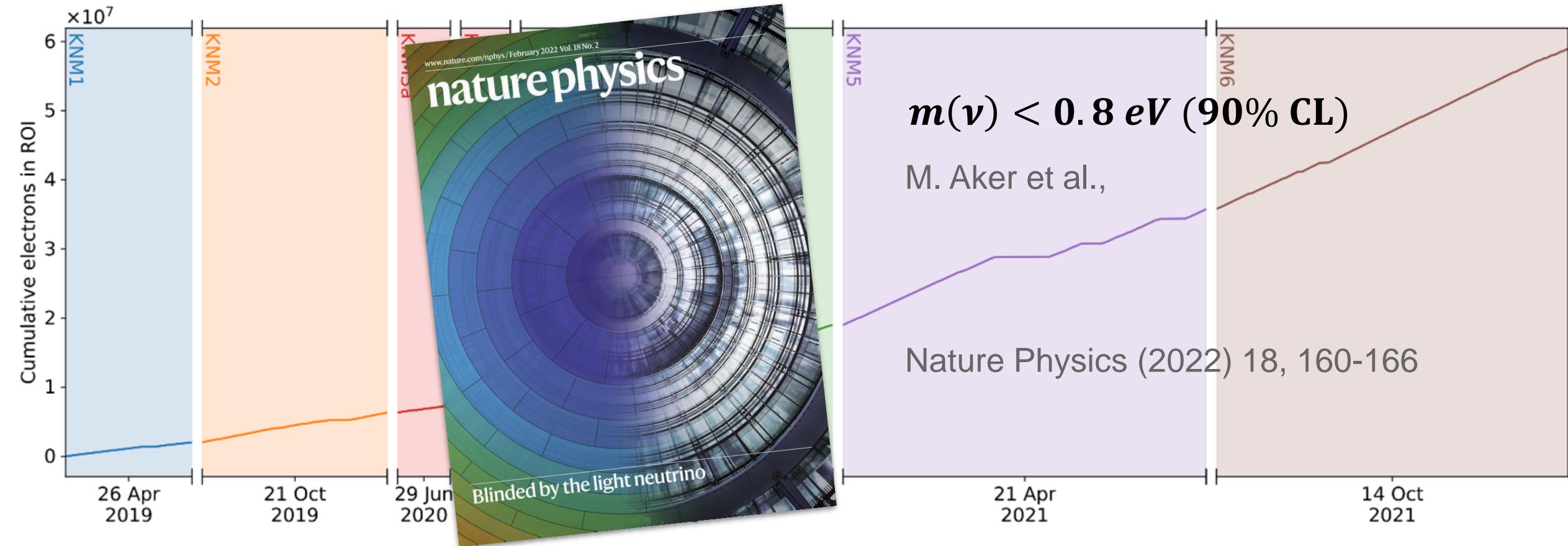
- β -scan:

typical scan time: 2 h
30 HV set points with specific
holding time & U_0 distribution
interval [$E_0 - 40$ eV, $E_0 + 130$ eV]



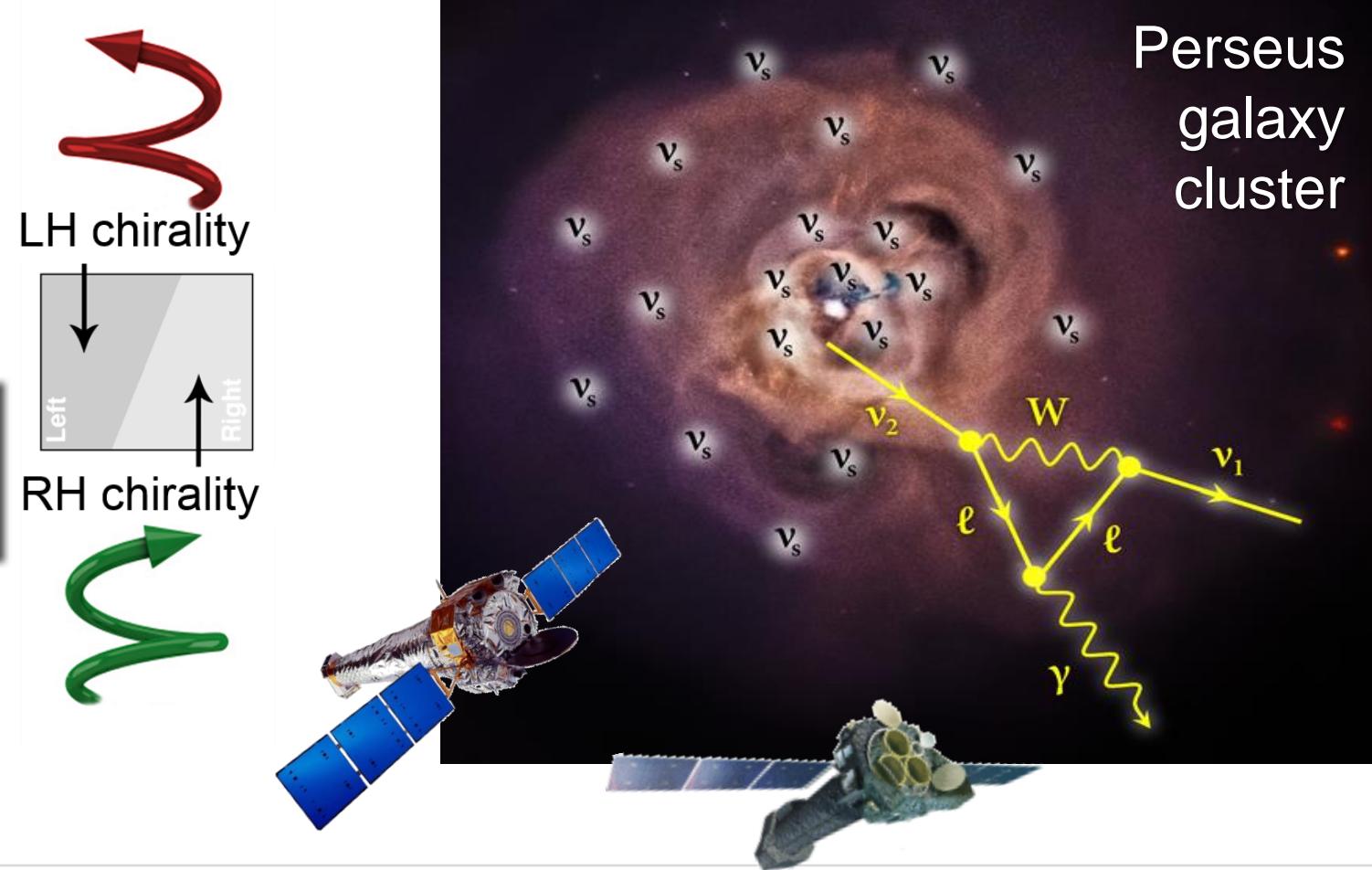
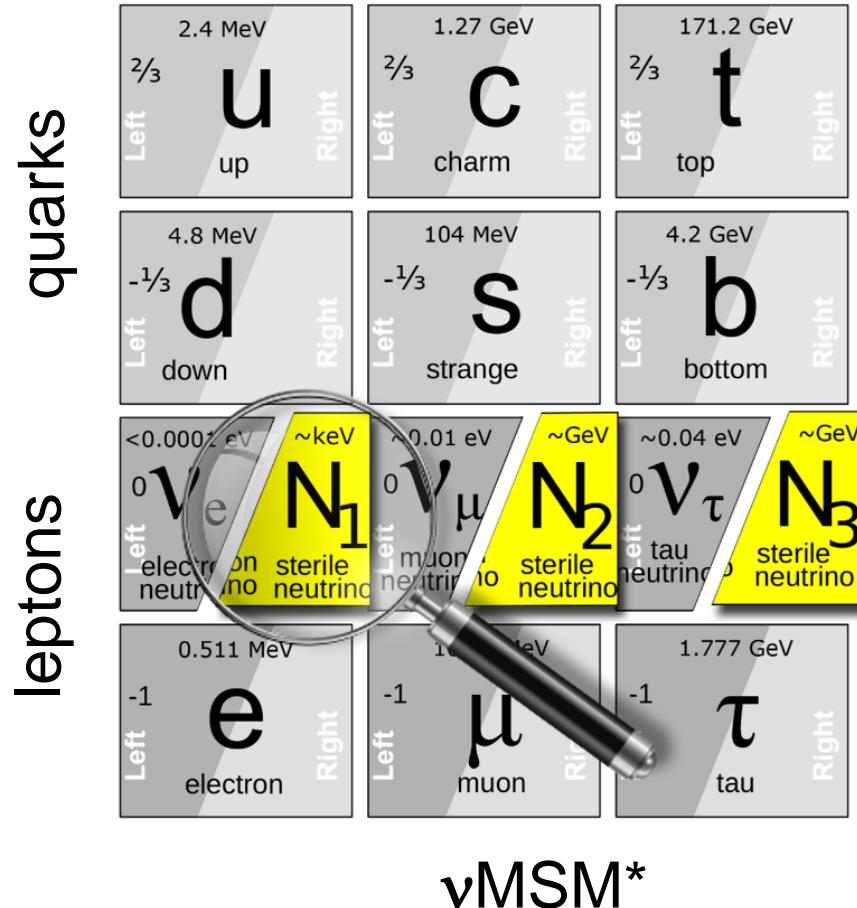
KATRIN data taking: first 2 campaigns KNM1+2

- 2019: initial 91 days of β – scanning (spring & autumn)



KATRIN experiment – future programme

■ Hunting sterile neutrinos at the mass scale m_s of several keV

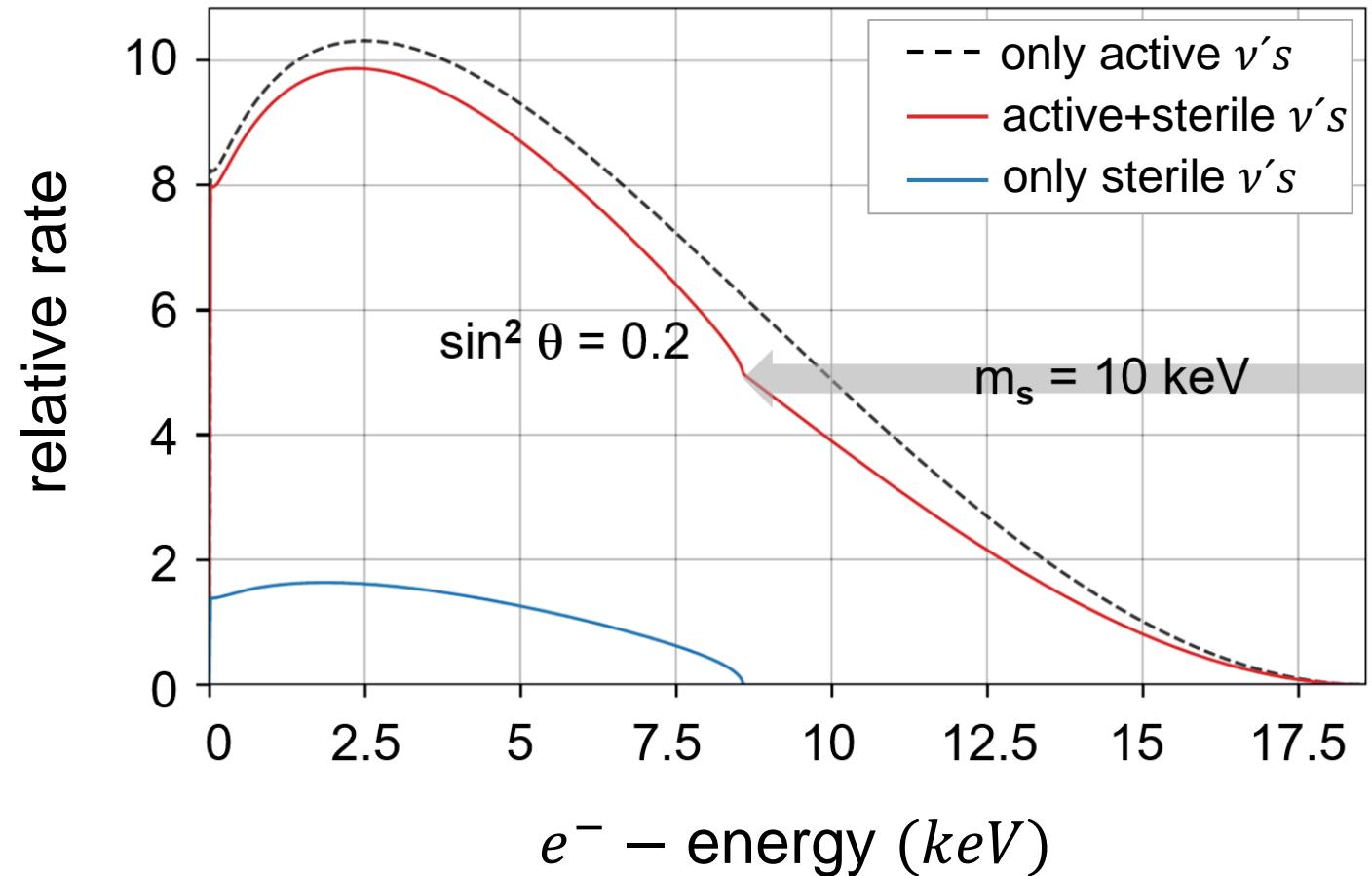


KATRIN experiment – future programme

■ Signature of sterile ν 's at the mass scale of keV via characteristic 'kink'

- investigate **entire phase space** of β – decay of T_2 sensitive to masses of ν_s with $m_s < 18 \text{ keV}$ and mixing angle $\sin^2 \theta \sim 10^{-6}$

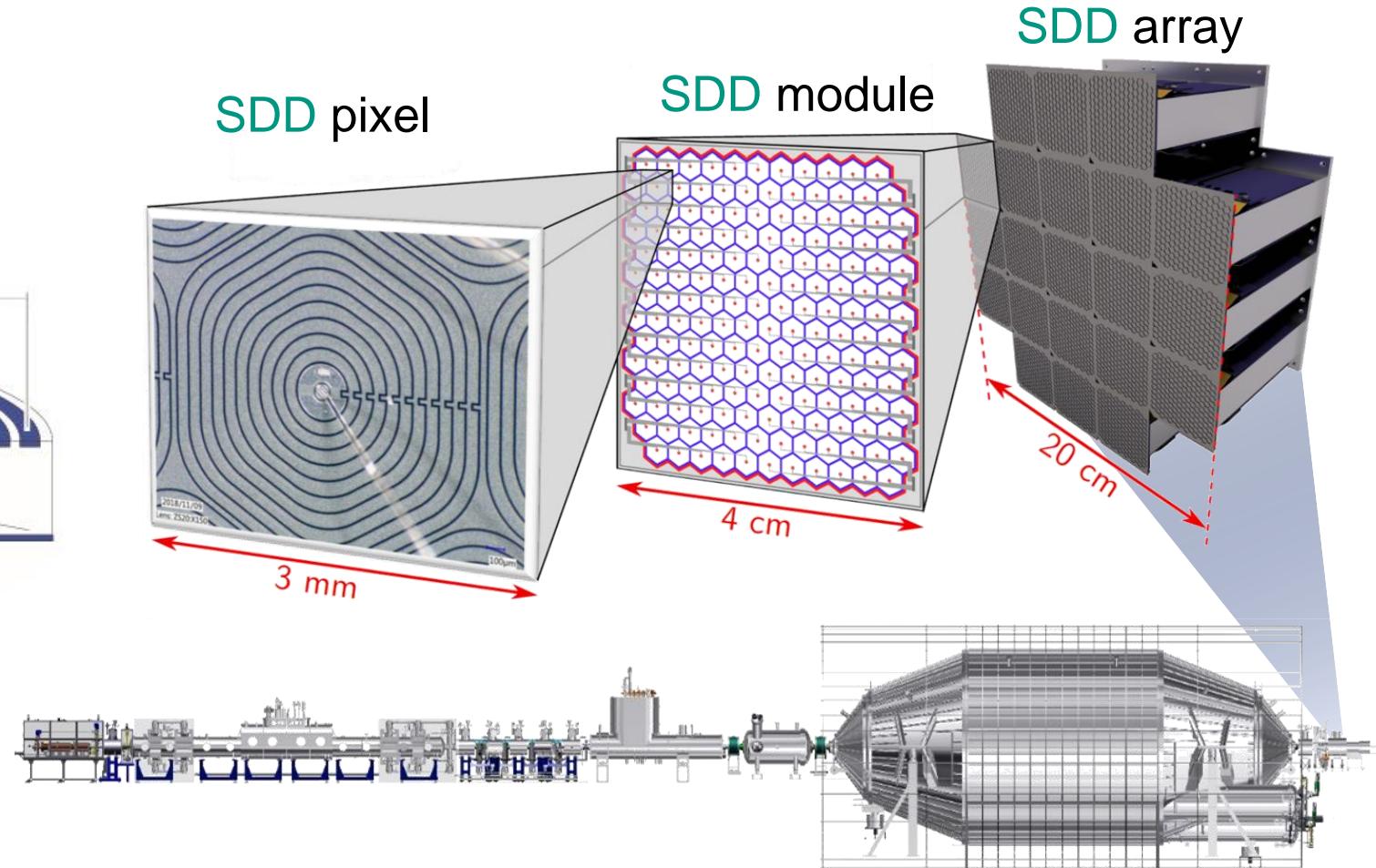
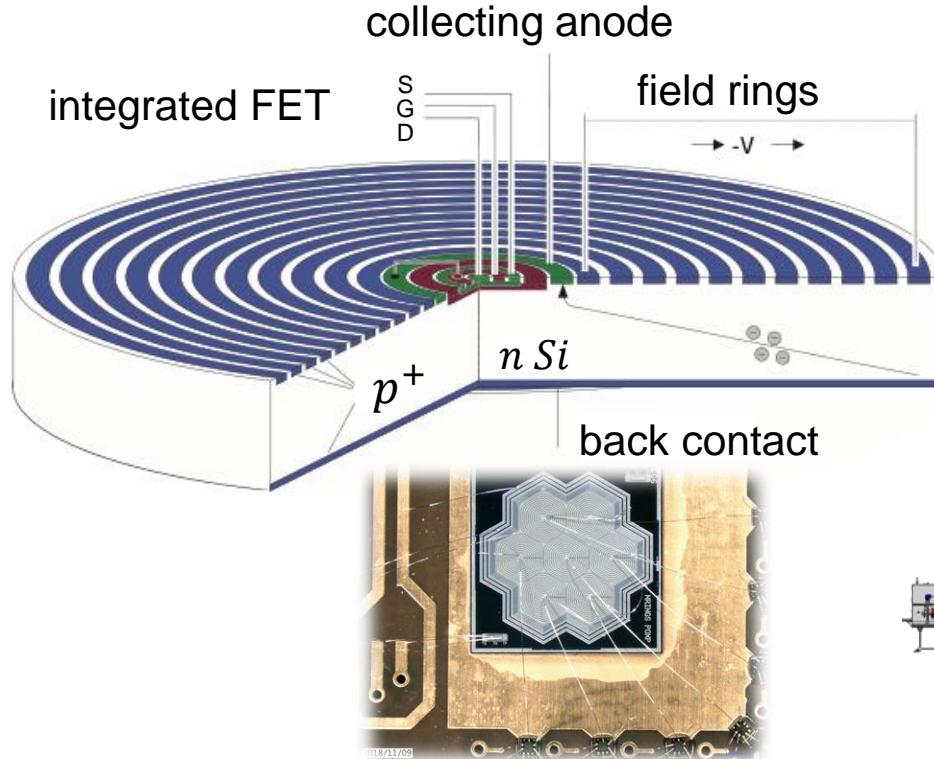
$$\frac{dN}{dE} = \cos^2 \theta_s \cdot \frac{dN}{dE}(m_{active}) + \sin^2 \theta_s \cdot \frac{dN}{dE}(m_{sterile})$$



KATRIN experiment – future programme

■ Signature of sterile ν 's requires new detector technology - SDDs

- novel detector technology:
Silicon Drift Detector



3.2 Search for $0\nu\beta\beta$ processes

■ Rare event searches hot on the track of Lepton Number (L) violation

- definition:

$$L = N(\ell) - N(\bar{\ell})$$

ℓ = lepton $\bar{\ell}$ = anti-lepton

- L and L_i :

$$L = L_e + L_\mu + L_\tau$$

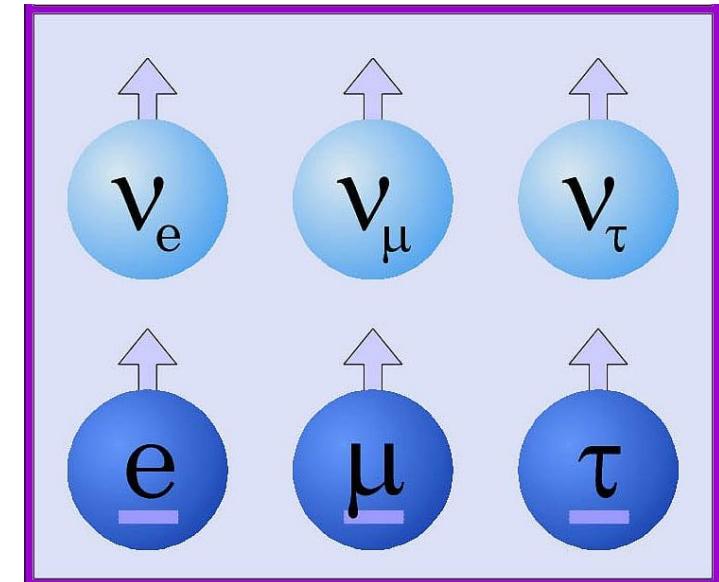
- flavour

$$L_e = +1 \text{ for } e^-, \nu_e \quad L_e = -1 \text{ for } e^+, \bar{\nu}_e$$

specific L_i :

$$L_\mu = +1 \text{ for } \mu^-, \nu_\mu \quad L_\mu = -1 \text{ for } \mu^+, \bar{\nu}_\mu$$

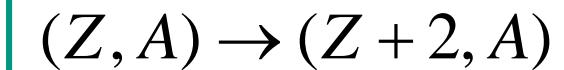
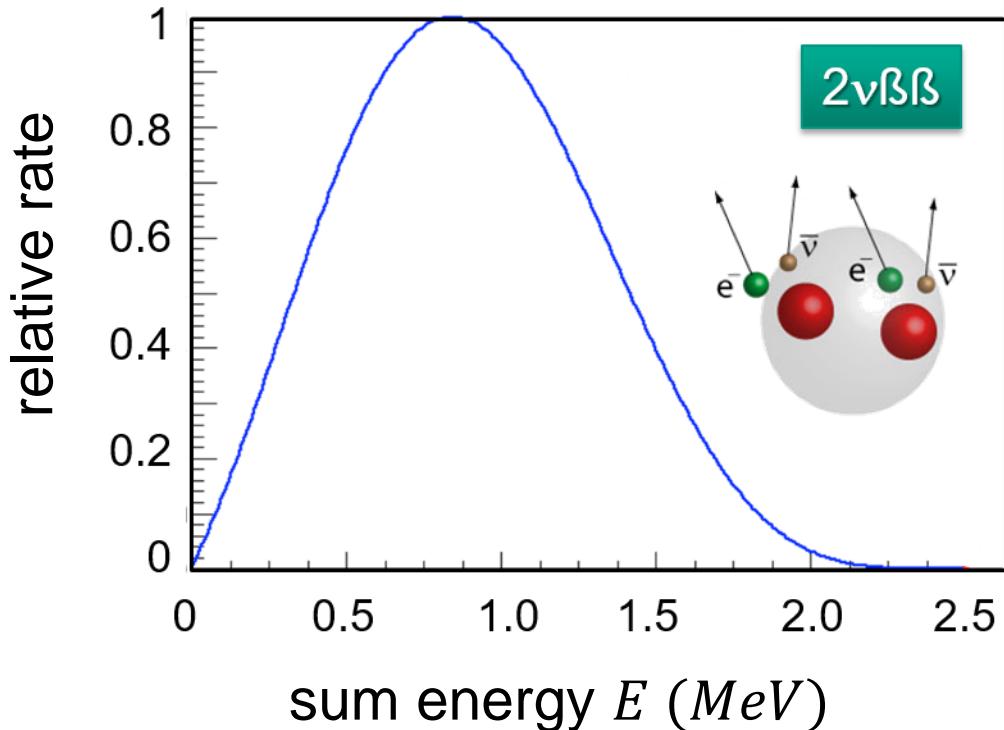
- flavour-specific L_i is not conserved due to ν –flavour oscillations* ($\nu_e \rightarrow \nu_\mu$),
but total lepton number L is conserved



Search for $0\nu\beta\beta$ processes – introduction

■ The 'classical' process $2\nu\beta\beta$: an allowed, second order weak interaction

- SM-allowed process with **4 particles** in the final state: $2 e^-$ & $2 \bar{\nu}_e$
- small transition rate, as weak interaction process of 2^{nd} order

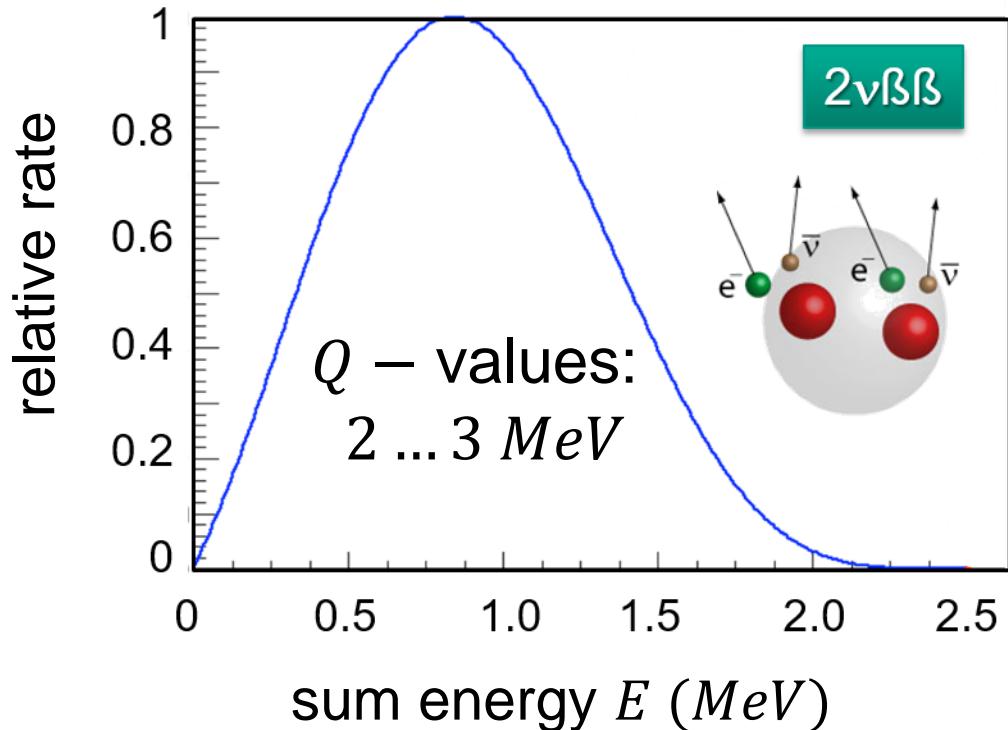


- $2\nu\beta\beta$: long half-lives $t_{1/2} \sim 10^{19} \dots 10^{21} \text{ yr}$
- $2\nu\beta\beta$: observed in > 10 isotopes
- similar process: double electron capture $\varepsilon\varepsilon$

Search for $0\nu\beta\beta$ processes – introduction

■ The 'classical' process $2\nu\beta\beta$: an allowed, second order weak interaction

- SM-allowed process with **4 particles** in the final state: $2 e^-$ & $2 \bar{\nu}_e$
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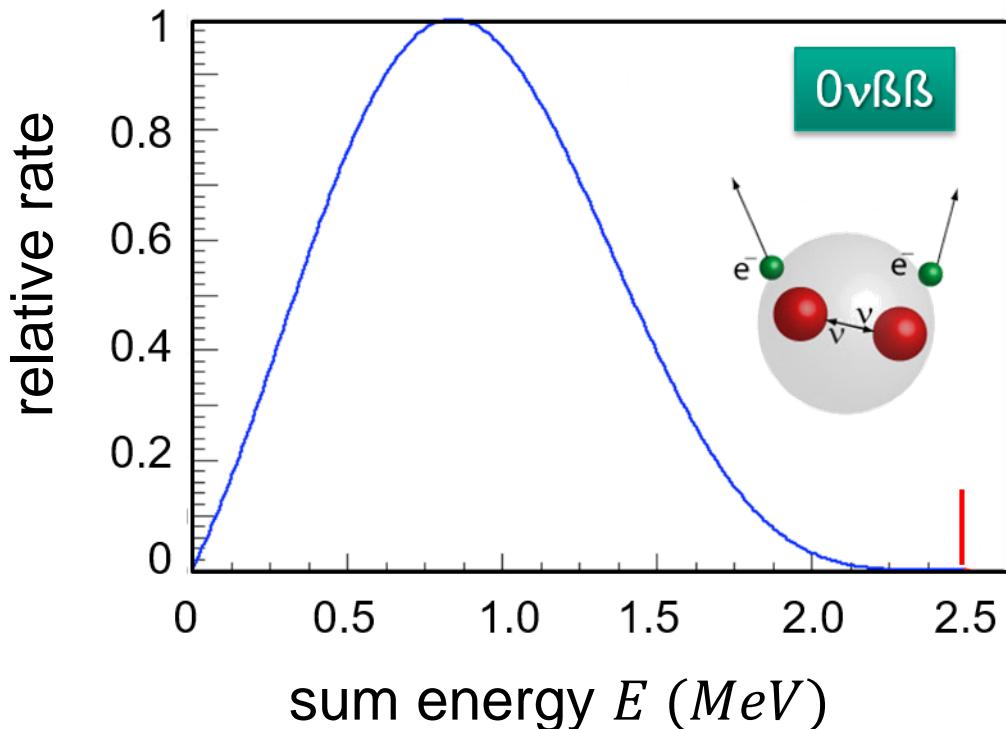
- first description of a $2\nu\beta\beta$ – by **Maria Goeppert-Mayer** (1935)
- first indirect evidence of $2\nu\beta\beta$ –processes (of ^{130}Te) obtained by radiochemical methods in 1950



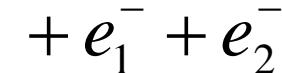
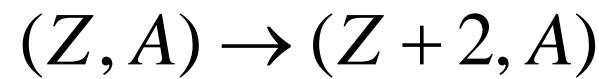
Search for $0\nu\beta\beta$ processes – introduction

■ 'Forbidden' process $0\nu\beta\beta$: second order weak interaction, no ν –emission

- SM-forbidden process with 2 particles in the final state: 2 e^-
- extremely small transition rate, allowed only if neutrinos are Majorana particles



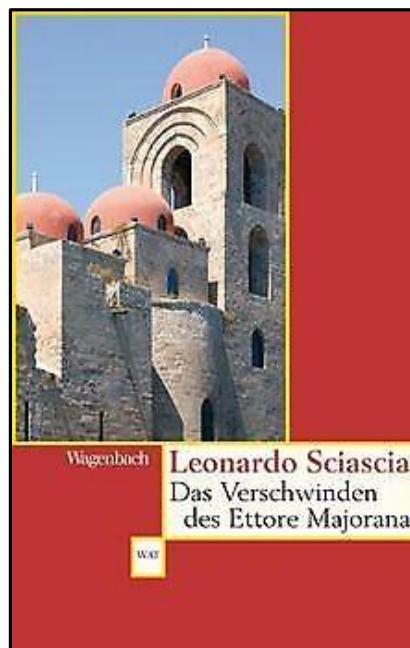
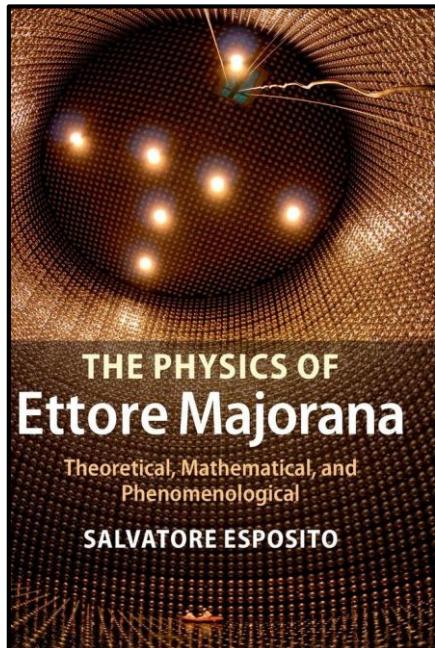
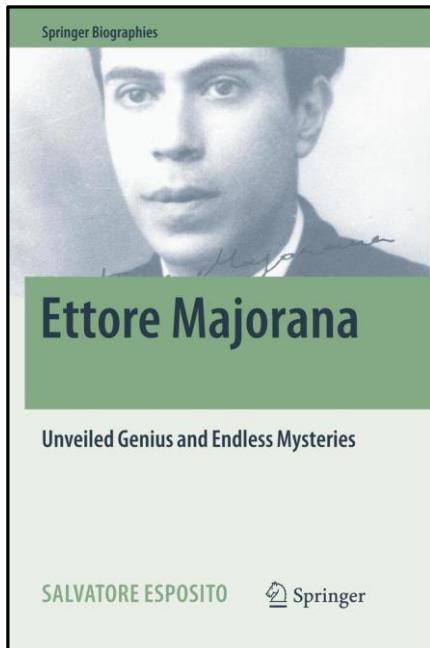
- first description of a $0\nu\beta\beta$ –
by George Racah & Ettore Majorana (1937)



Search for $0\nu\beta\beta$ processes – the case of Ettore

■ ‘Forbidden’ process $0\nu\beta\beta$: second order weak interaction, no ν –emission

“There are several categories of scientists in the world; those of second or third rank do their best but never get very far. Then there is the first rank, those who make important discoveries, fundamental to scientific progress. But then there are the geniuses, like Galilei and Newton. Majorana was one of these.” E. Fermi



Ettore Majorana (1937)*

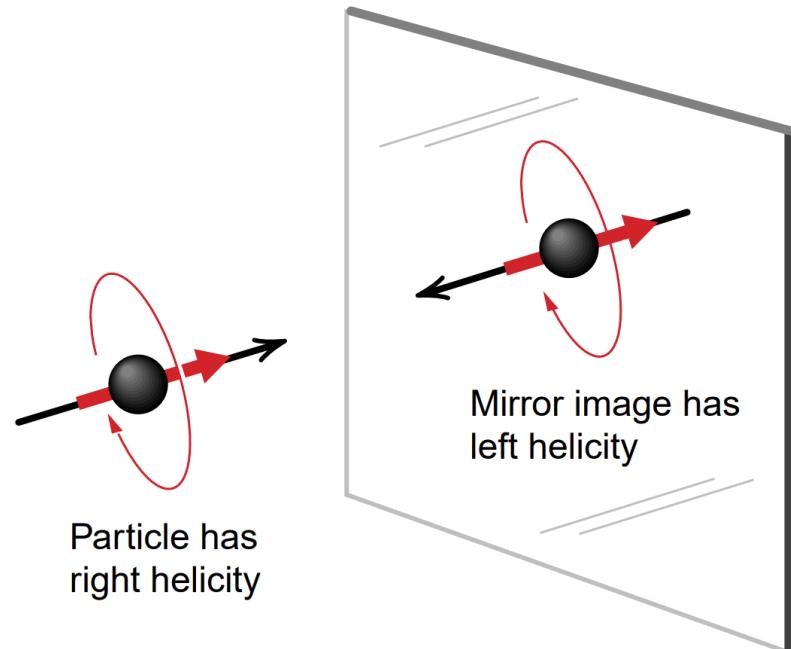
*disappeared on
March 25, 1938



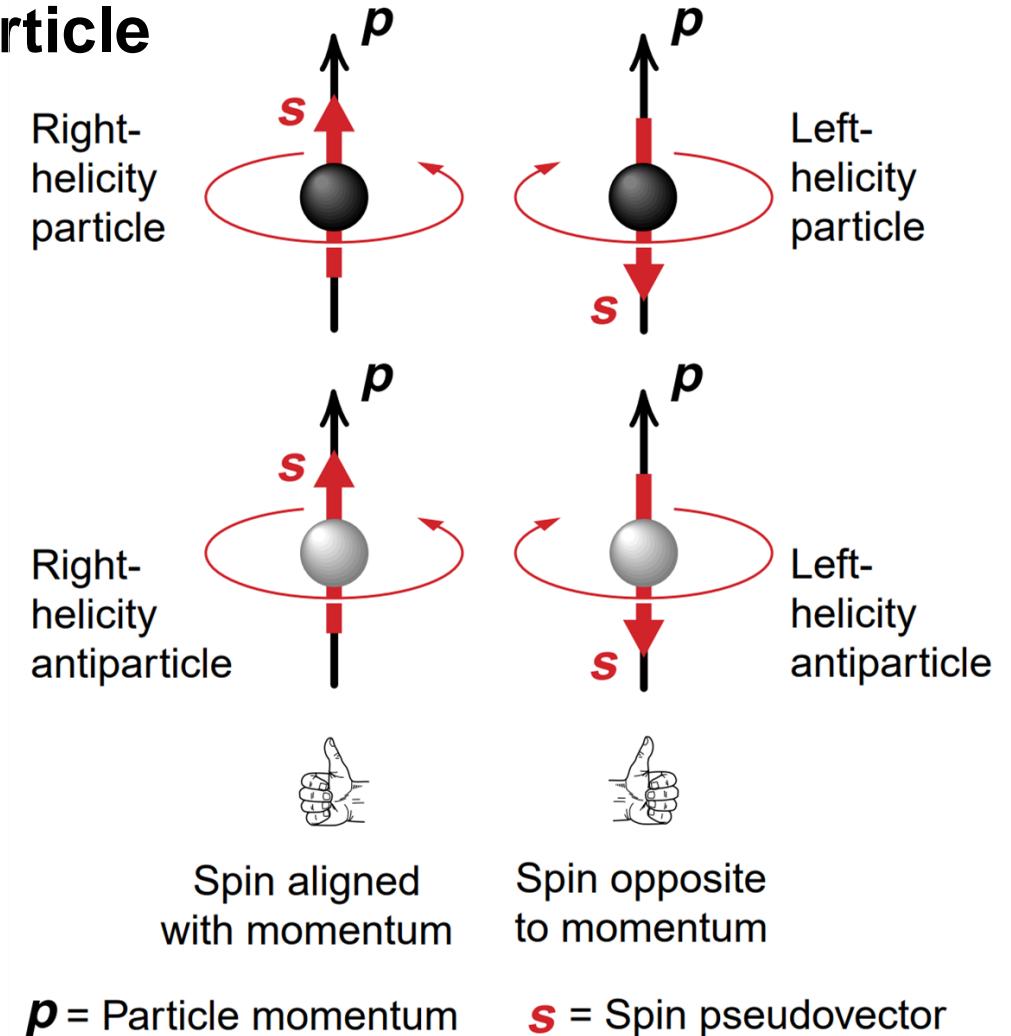
$0\nu\beta\beta$ processes – description

■ RECAP: helicity states of a massive particle

- the **four states** of a spin $s = \frac{1}{2}$ particle



- **mirror image** of a spin $s = \frac{1}{2}$ particle



$0\nu\beta\beta$ processes – description

■ Feynman diagram: exchange of a massive Majorana neutrino

- the exchanged neutrino undergoes a helicity flip

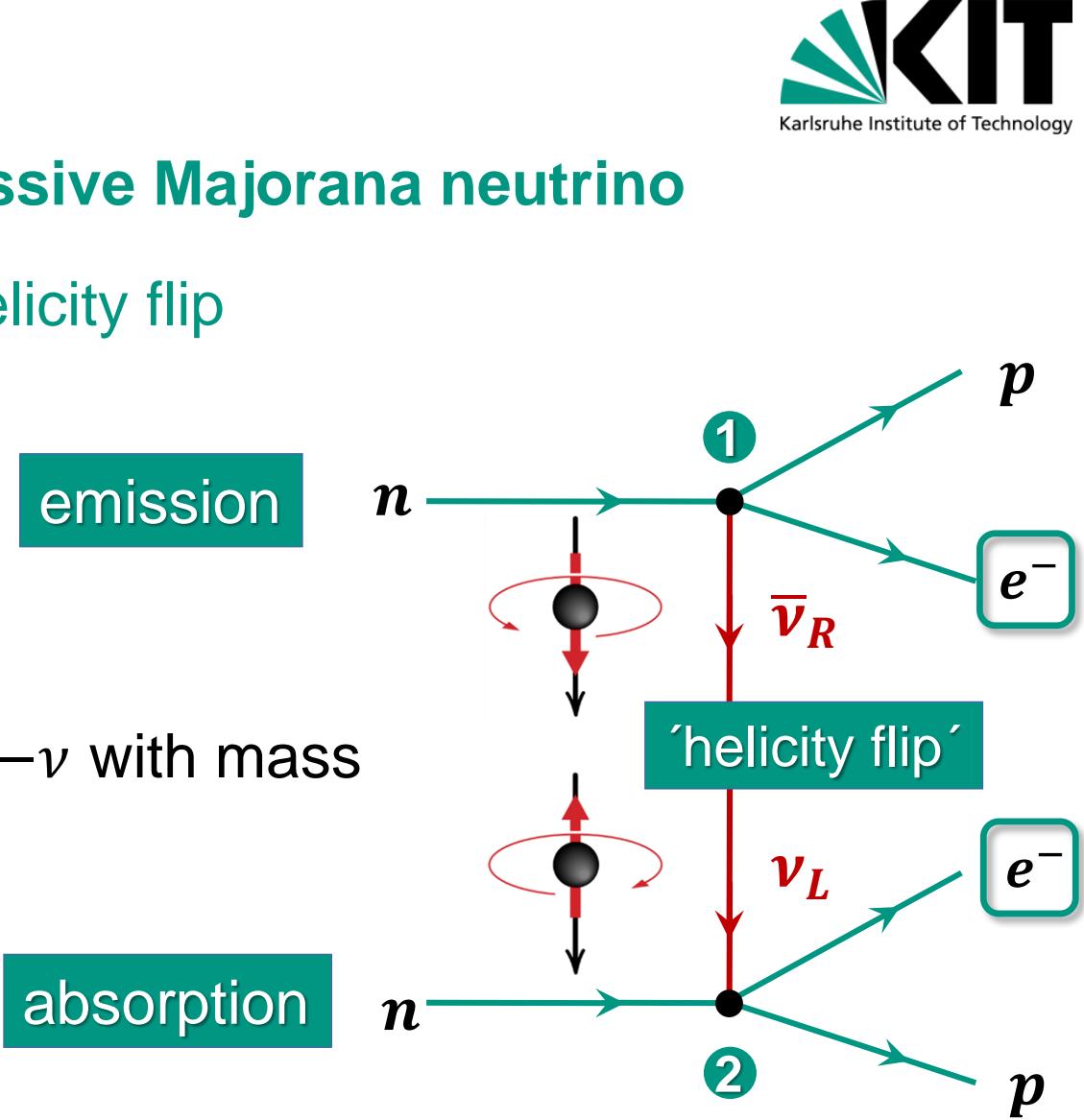
vertex ①: emission as **RH state**
from the decay of a **n**

exchange of a virtual Majorana- ν with mass

vertex ②: absorption as **LH state**
by a second **n**

emission

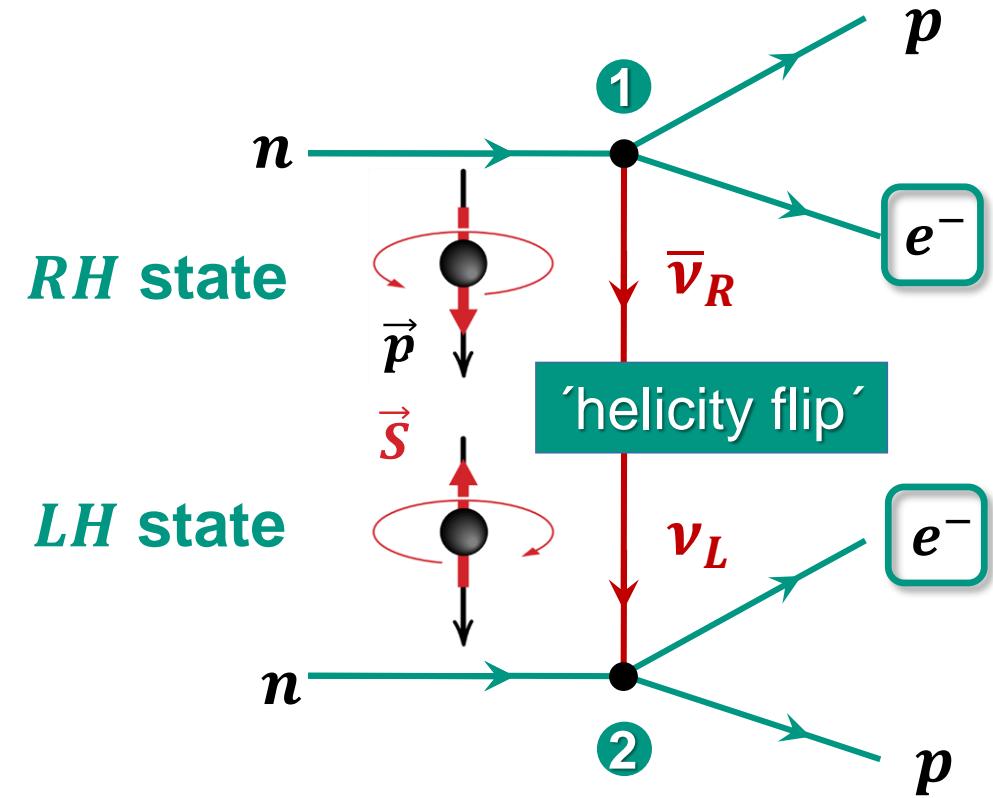
absorption



$0\nu\beta\beta$ processes – description

■ Feynman diagram: the Racah process

- **helicity flip** of the exchanged ν corresponds to a **Majorana mass term**
- intrinsic properties of a Majorana neutrino:
 - does not carry additive quantum numbers
 - does not carry a **lepton number L**
 - has vanishing electric & magnetic dipole moments $\mu_i = 0$
 - 'neutrino is its own antiparticle'**



$0\nu\beta\beta$ processes – kinematics & nuclear size

- nucleons inside nucleus carry a large Fermi momentum $p_F \sim 100 \text{ MeV}/c$

- virtual, light ($m_\nu \sim \text{meV}$) Majorana- ν is ultra-relativistic due to

$$E_\nu \sim p_\nu \sim 100 \text{ MeV}$$

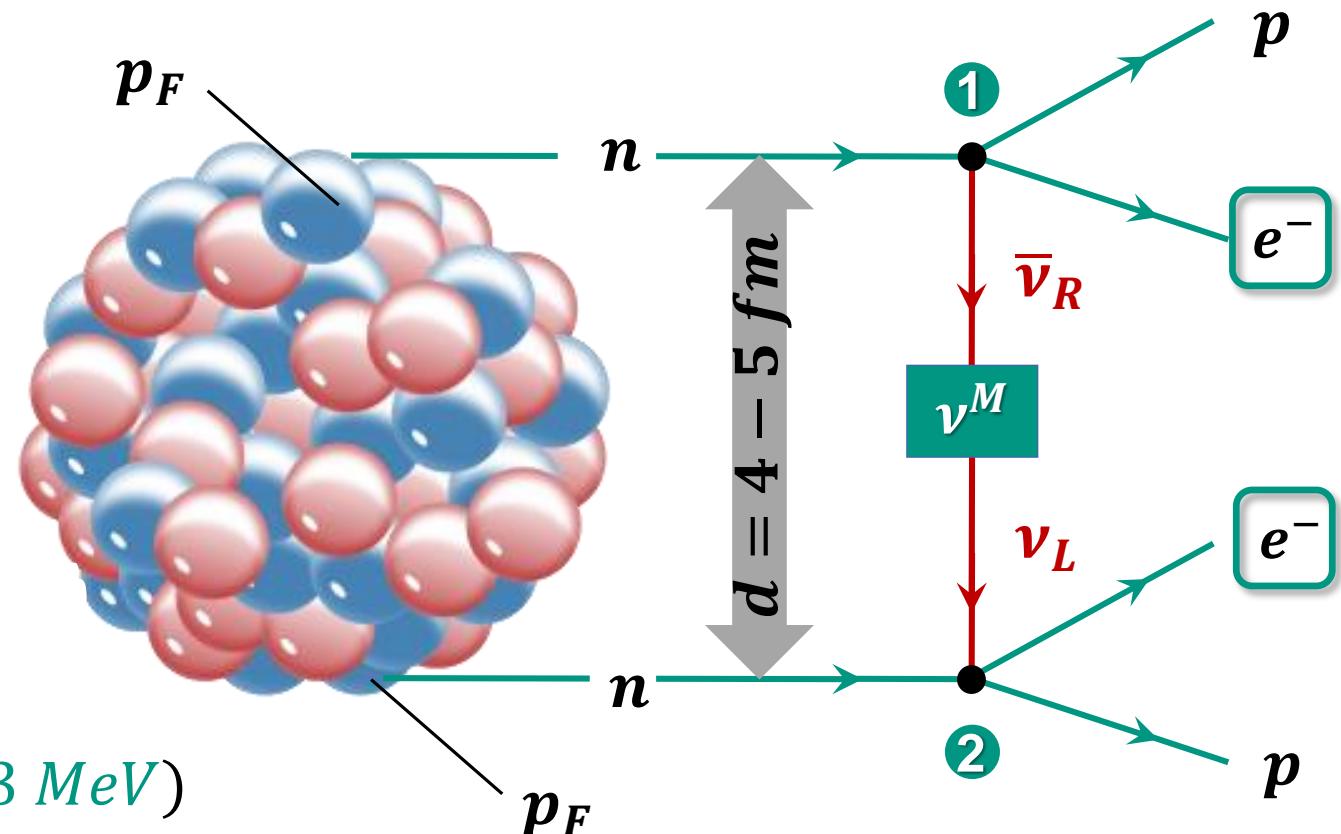
- travel distance of ν^M between emission & absorption ($2 n$)

$$d \sim 4 - 5 \text{ fm}$$

(size of a nucleus)

- kinematics: compare ν –energy to reaction Q – value:

$$E_\nu \text{ (100 MeV)} \gg Q \text{ – value (2 – 3 MeV)}$$



$0\nu\beta\beta$ processes – kinematics & nuclear size

- nucleons inside nucleus carry a large Fermi momentum $p_F \sim 100 \text{ MeV}/c$

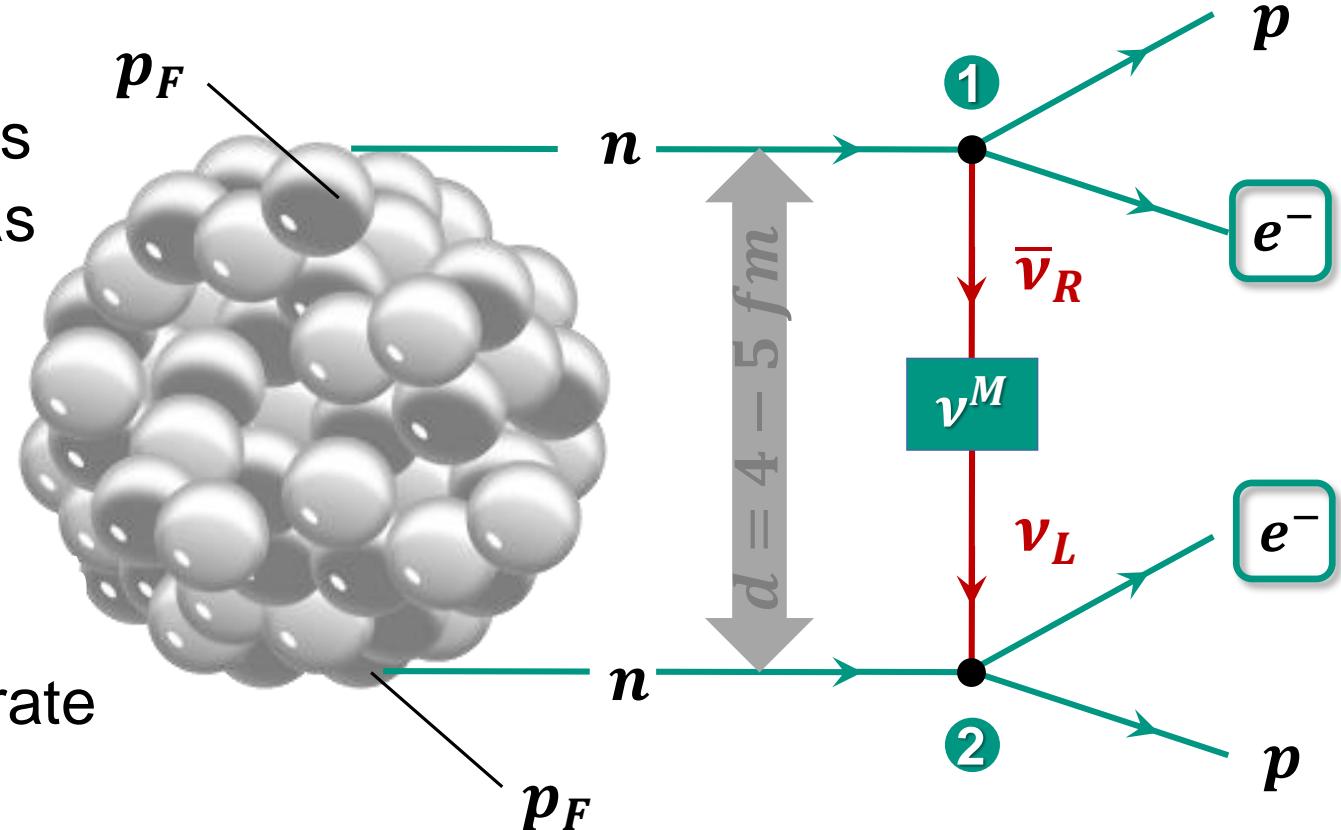
- virtual, light ($m_\nu \sim \text{meV}$) Majorana- ν is **ultra-relativistic** due to

$$E_\nu \sim p_\nu \sim 100 \text{ MeV}$$

- expected $0\nu\beta\beta$ –rate should thus be larger even than β – decay, as it scales as

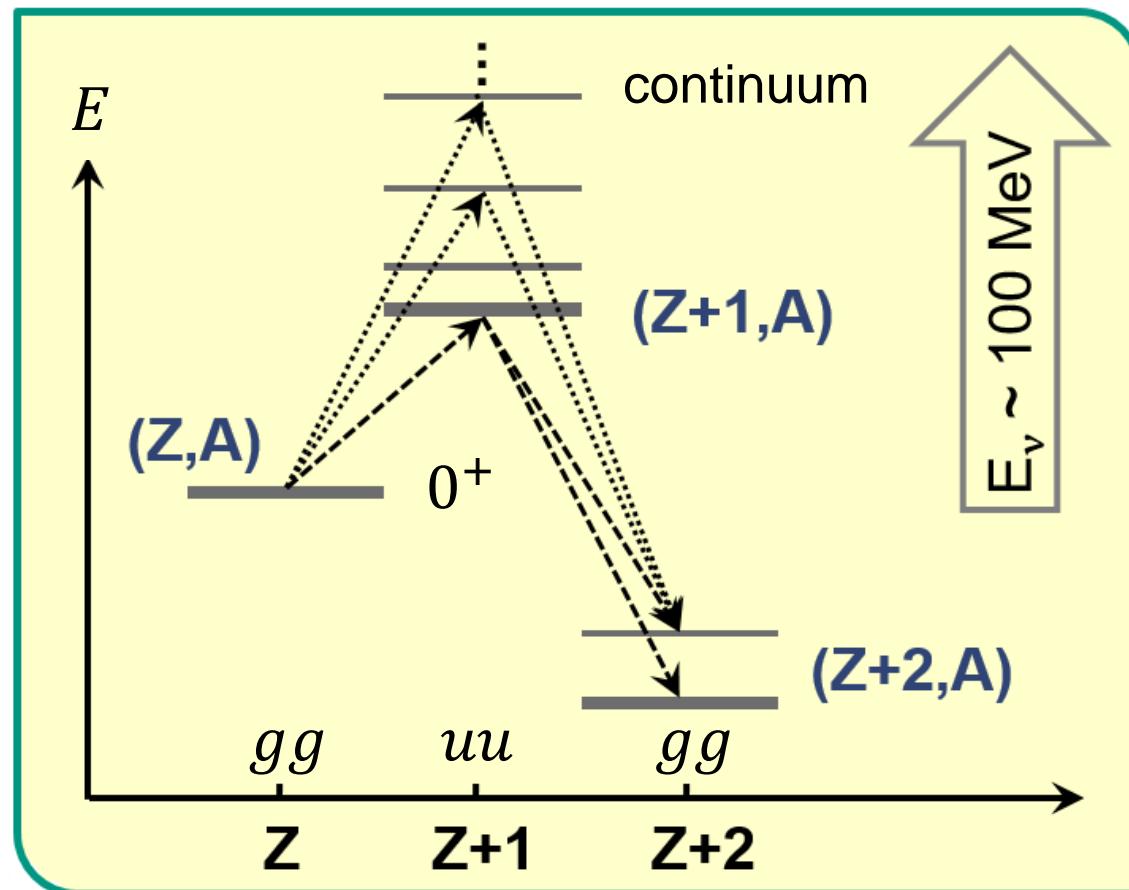
$$\Gamma \sim (E_\nu/Q)^5 \sim 10^6$$

- however, the **ultra-relativistic nature of neutrinos** in $0\nu\beta\beta$ – processes reduces the spin-flip rate by many, many, many orders...

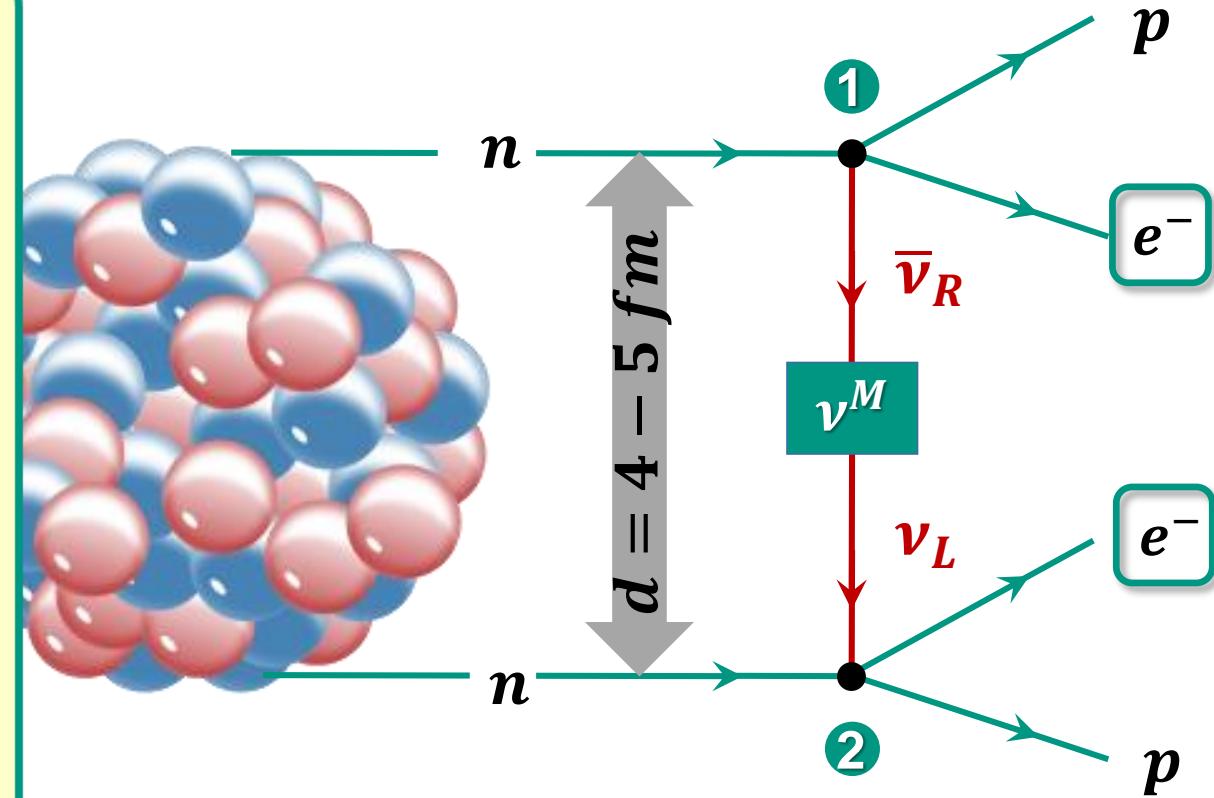


$0\nu\beta\beta$ processes – a ‘virtual’ intermediate state

- When going from Z_A nucleus to ${}^{Z+2}A$ we form many intermediate states ${}^{Z+1}A$



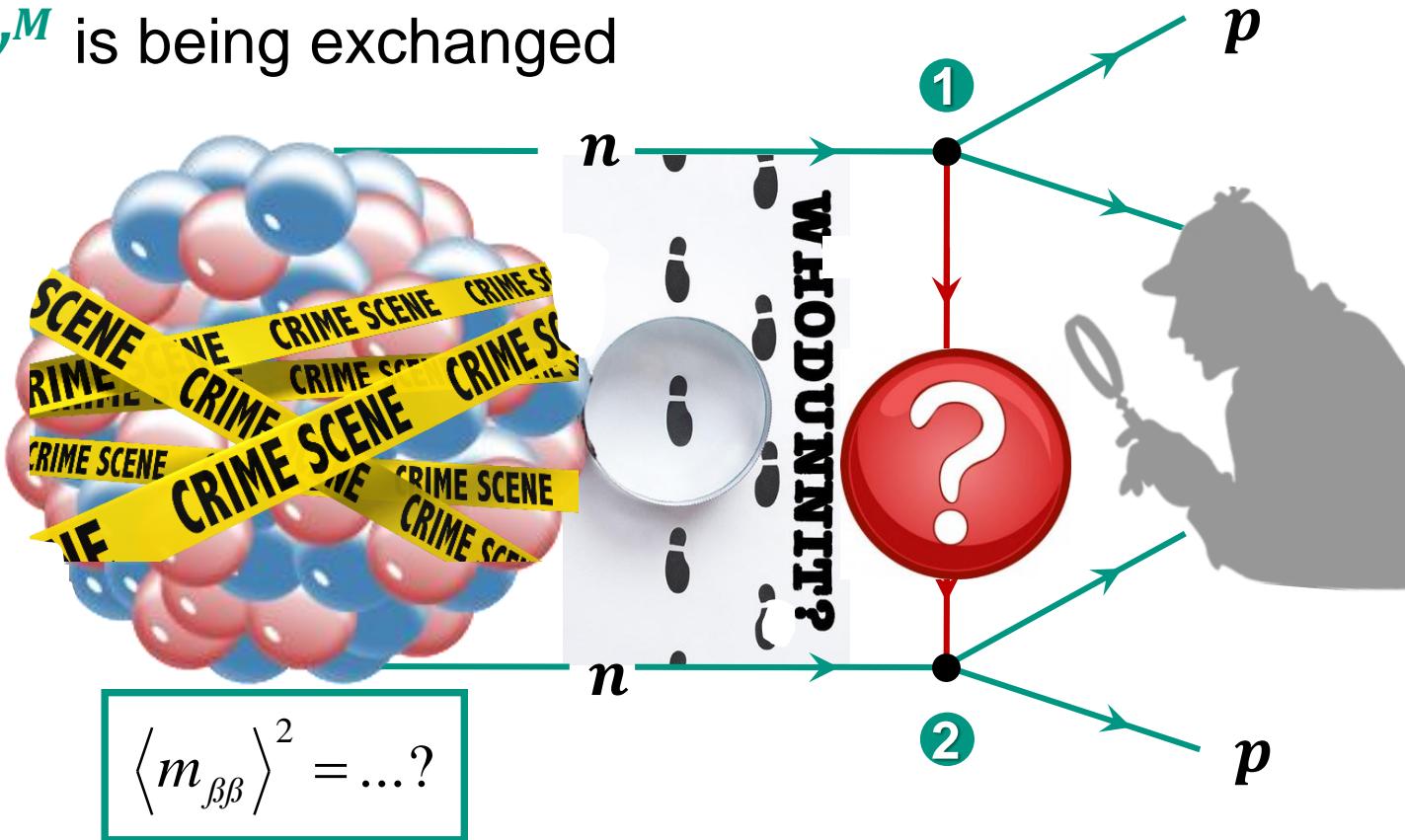
- this is a big challenge for theory!



$0\nu\beta\beta$ processes – ‘virtual’ nature of Majorana – ν

■ Which virtual (!) particle is exchanged between the two neutrons?

- expected rate of $0\nu\beta\beta$ – events is usually calculated under the assumption that ONLY a **light ν^M** is being exchanged
- new particles at the TeV-scale (neutralinos, lepto-quarks) could modify the $0\nu\beta\beta$ – rate
- new physics at the TeV-scale (RH weak currents with W_R – bosons) could modify the $0\nu\beta\beta$ – rate



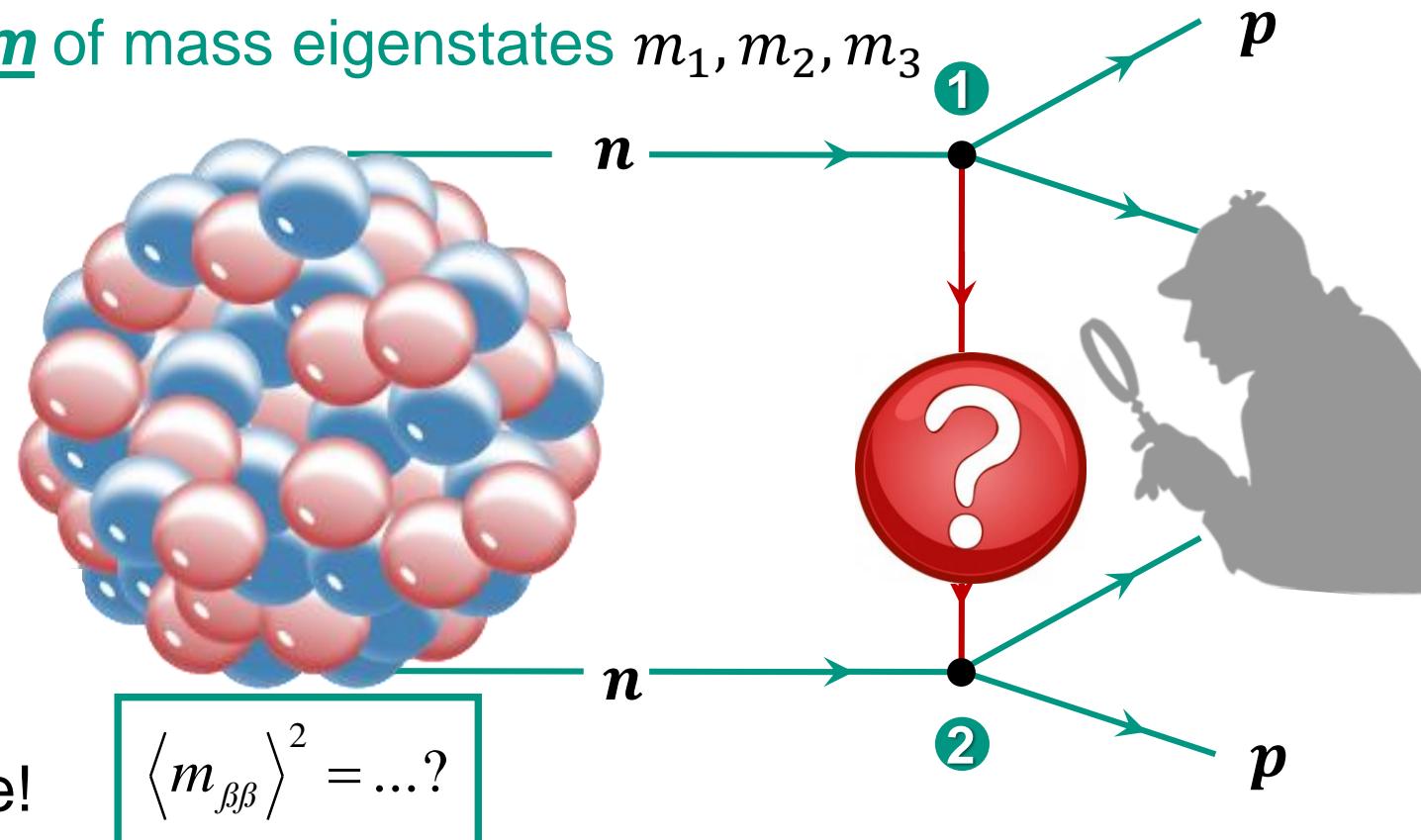
$0\nu\beta\beta$ processes – ‘virtual’ nature of Majorana – ν

■ How do the mass eigenstates m_1, m_2, m_3 interfere in $0\nu\beta\beta$?

- rate of $0\nu\beta\beta$ – events depends on the effective Majorana ν –mass $m_{\beta\beta}$ which is the coherent sum of mass eigenstates m_1, m_2, m_3



virtual quantum states interfere!



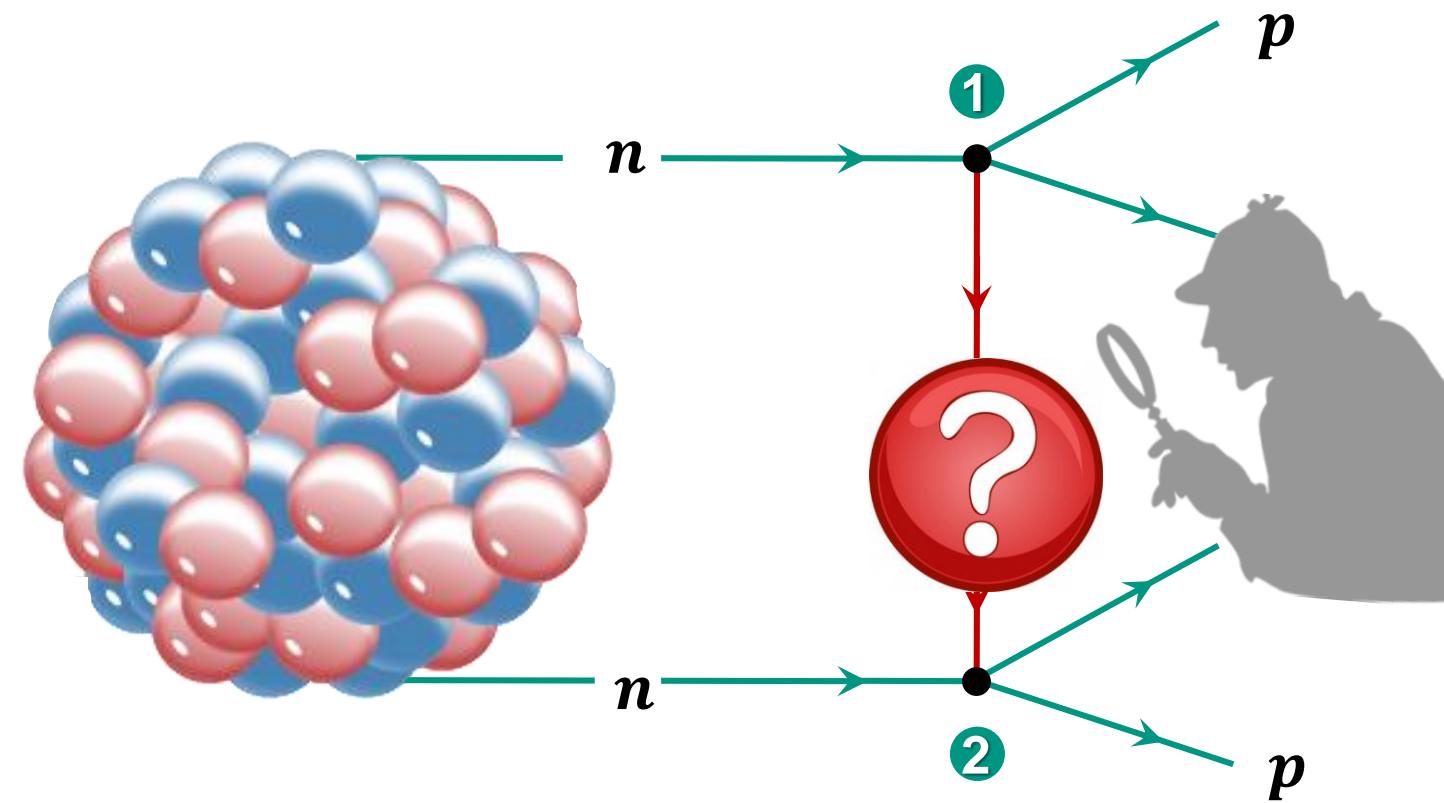
$0\nu\beta\beta$ processes – CP phases of Majorana – ν 's

■ How do the mass eigenstates m_1, m_2, m_3 interfere in $0\nu\beta\beta$?

- rate of $0\nu\beta\beta$ – events depends on more unknown parameters,
the **Majorana CP-phases α_i**

$$\langle m_{\beta\beta} \rangle = \left| \sum_{i=1}^3 |U_{e,i}|^2 m_i \cdot e^{i\alpha_i} \right|$$

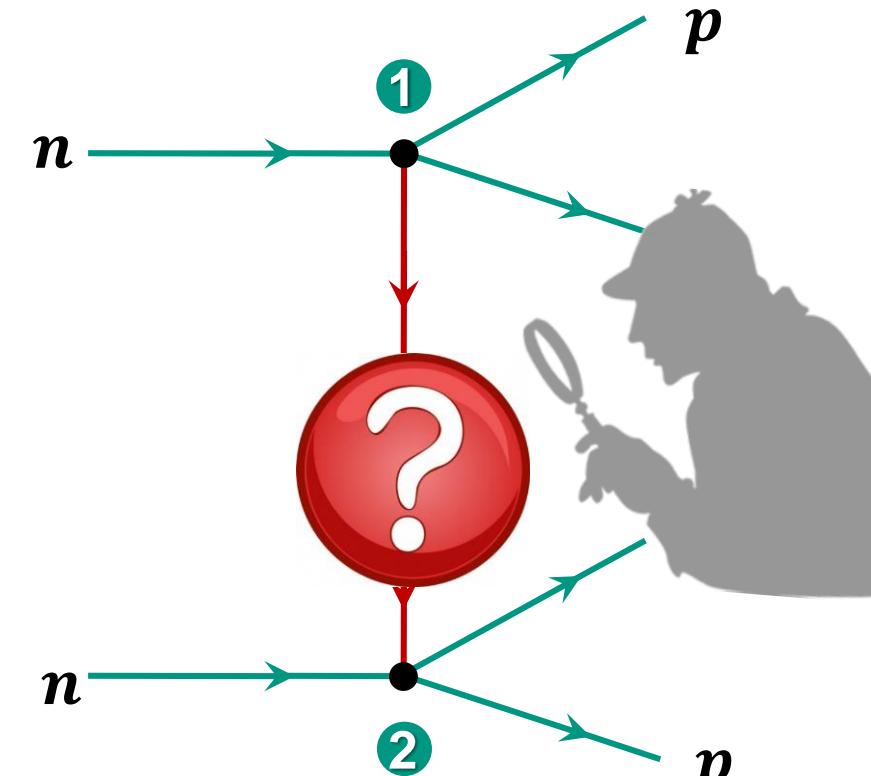
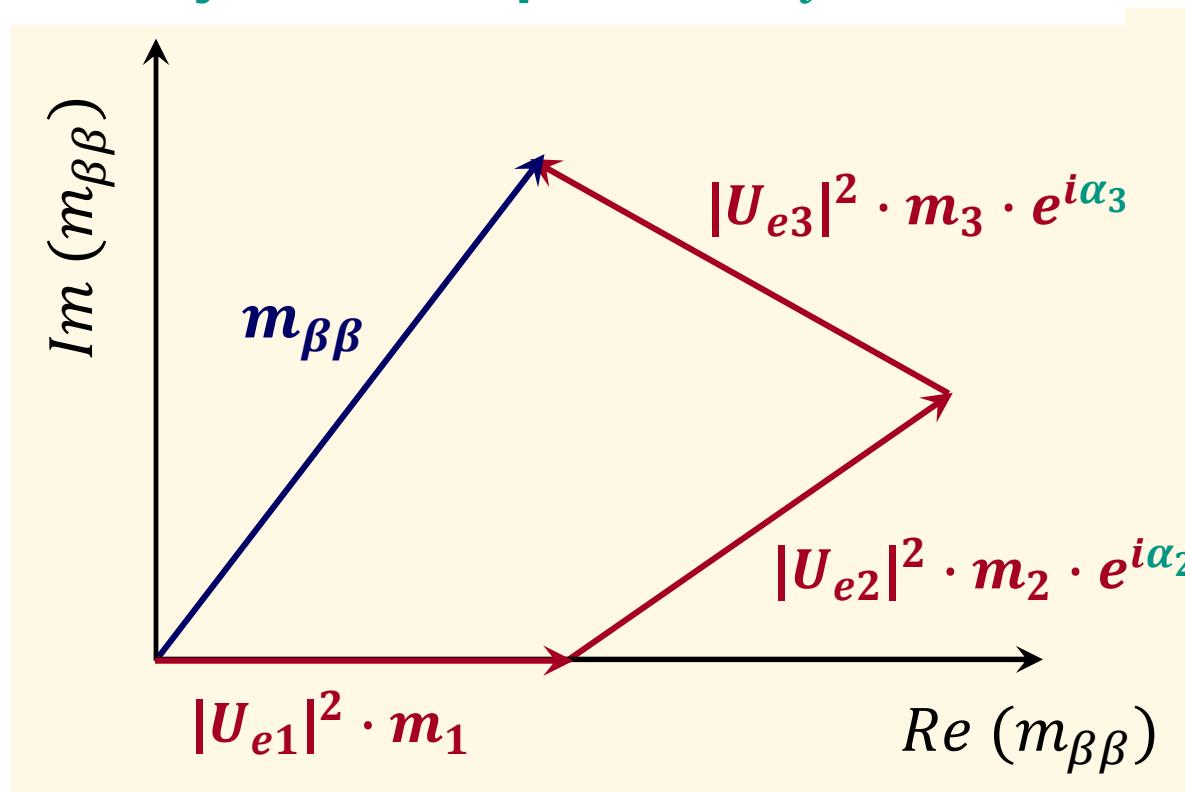
two independent phases:
⇒ can result in cancellations



$0\nu\beta\beta$ processes – CP phases of Majorana – ν 's

■ How do the mass eigenstates m_1, m_2, m_3 interfere in $0\nu\beta\beta$?

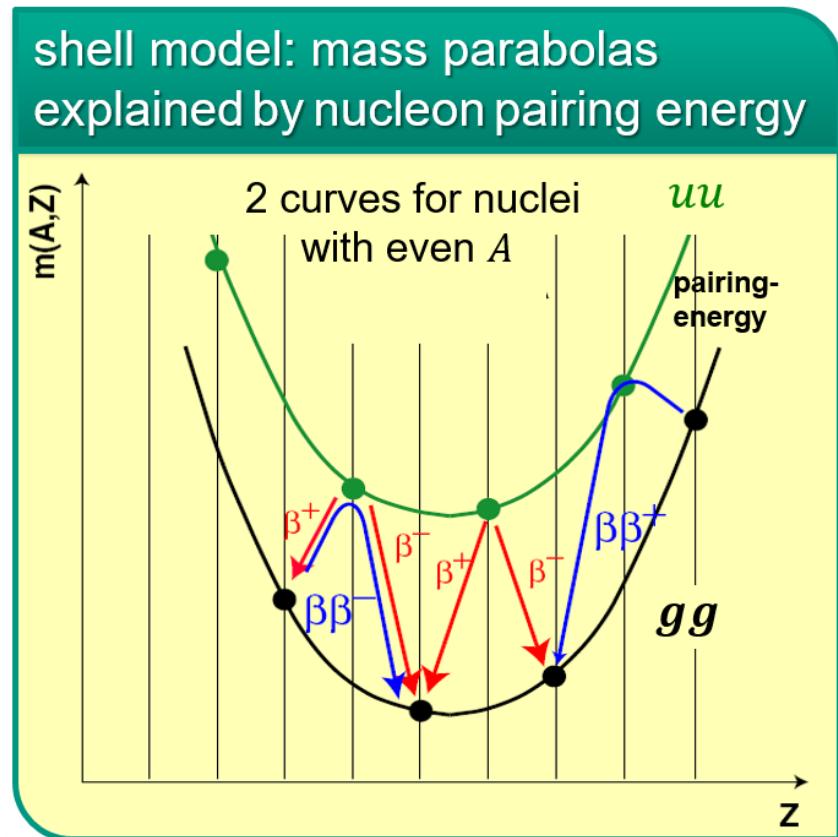
- rate of $0\nu\beta\beta$ – events depends on two* more unknown parameters, the **Majorana CP-phases α_i**



$0\nu\beta\beta$ processes: gg –isotopes as target

■ Double beta decay is only possible for gg –nuclei

- mass parabolas of gg and uu nuclei

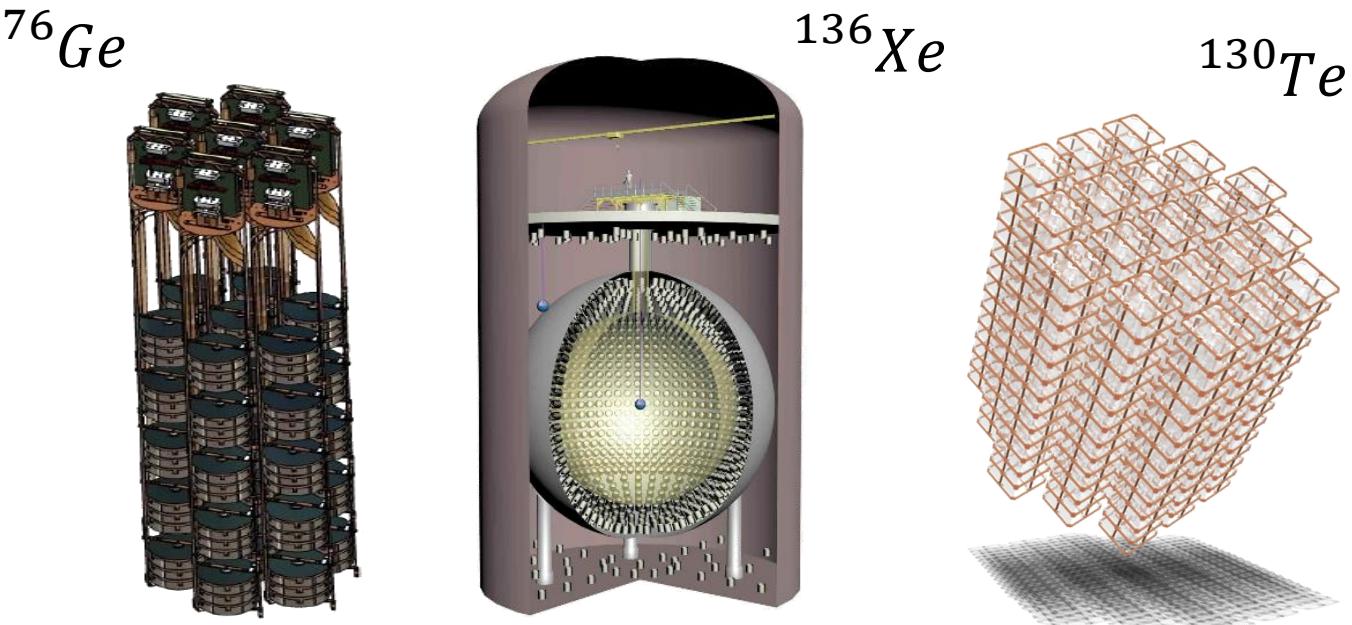


	Q – value	relative abundance %
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	4.271	0.187
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	2.040	7.8
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	2.995	9.2
$^{96}\text{Zr} \rightarrow ^{96}\text{Mo}$	3.350	2.8
$^{100}\text{Mo} \rightarrow ^{100}\text{Ru}$	3.034	9.6
$^{110}\text{Pd} \rightarrow ^{110}\text{Cd}$	2.013	11.8
$^{116}\text{Cd} \rightarrow ^{116}\text{Sn}$	2.802	7.5
$^{124}\text{Sn} \rightarrow ^{124}\text{Te}$	2.228	5.64
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	2.530	33.8
$^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$	2.479	8.9
$^{150}\text{Nd} \rightarrow ^{150}\text{Sm}$	3.367	5.6

$0\nu\beta\beta$ processes: gg –isotopes as target

■ Double beta decay is only possible for gg –nuclei

- 11 isotopes with $Q_{\beta\beta} > 2 \text{ MeV}$
- 3 promising isotopes especially suited to perform a **high-sensitivity** $0\nu\beta\beta$ search

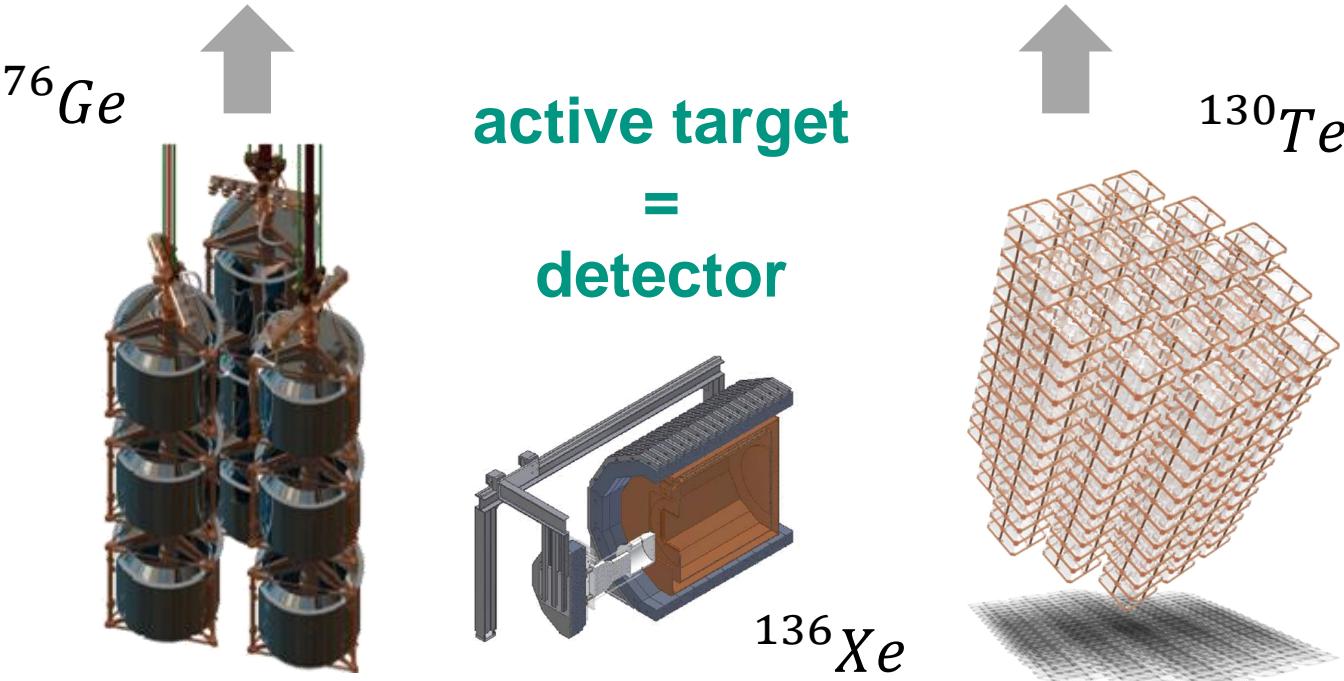


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$0\nu\beta\beta$ processes: gg –isotopes as target

■ Use of gg –isotopes as active detector target

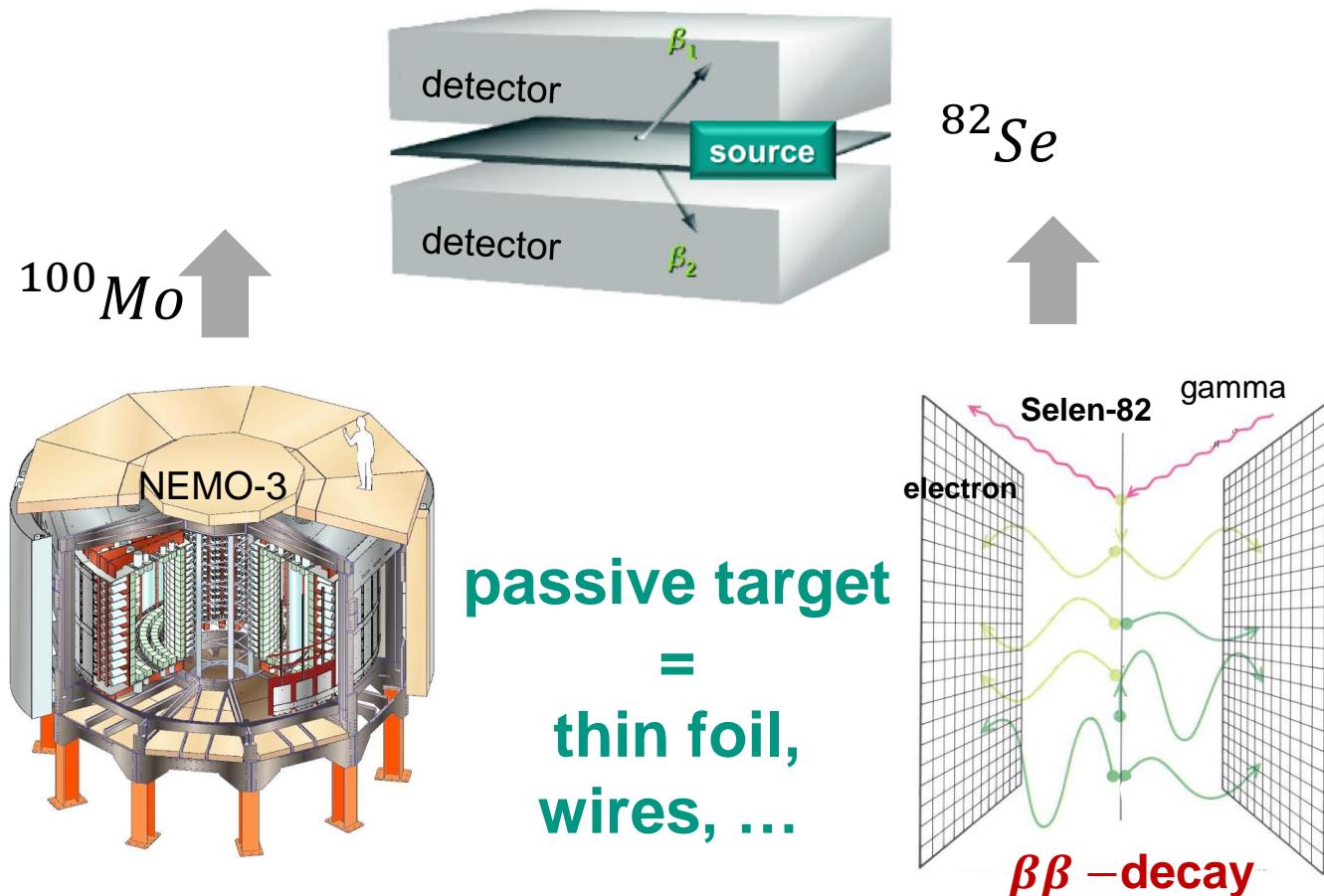
$\beta\beta$ –signal via
ionization of a
solid state detector $\beta\beta$ –signal via
heat deposit in
cryogenic quantum sensor



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$0\nu\beta\beta$ processes: gg –isotopes as target

■ Use of gg –isotopes as passive target

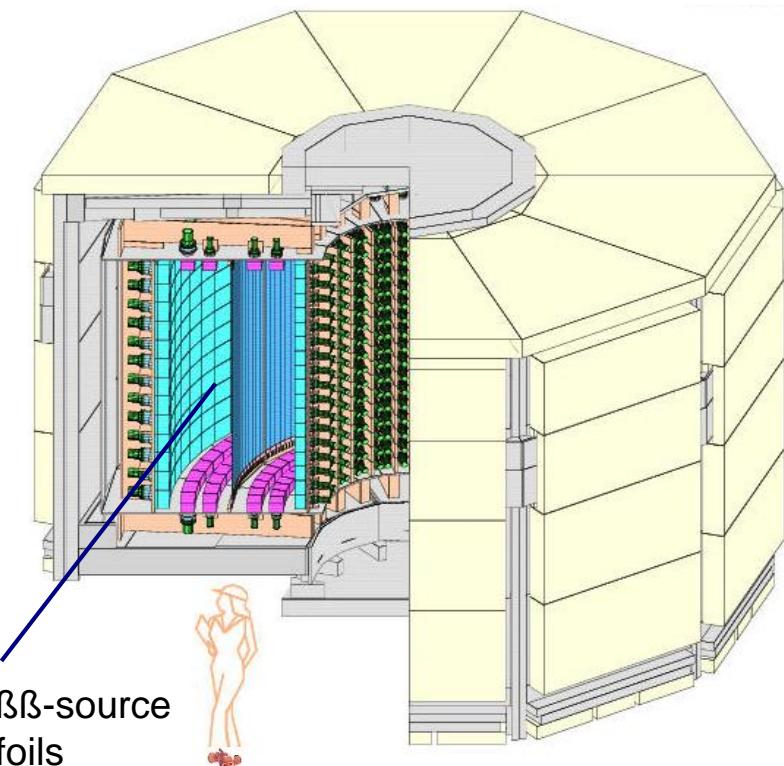


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$0\nu\beta\beta$ processes: gg –isotopes as target

■ Use of gg –isotopes as passive target: example NEMO

Neutrino Ettore Majorana Observatory at Modane underground laboratory



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