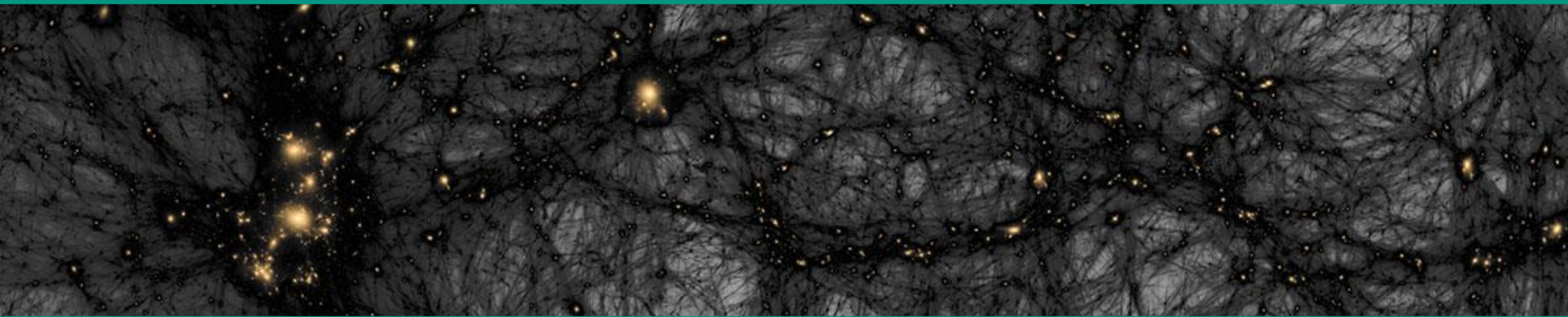


Astroparticle physics I – Dark Matter

WS22/23 Lecture 20

Feb. 9, 2023



Recap of Lecture 19

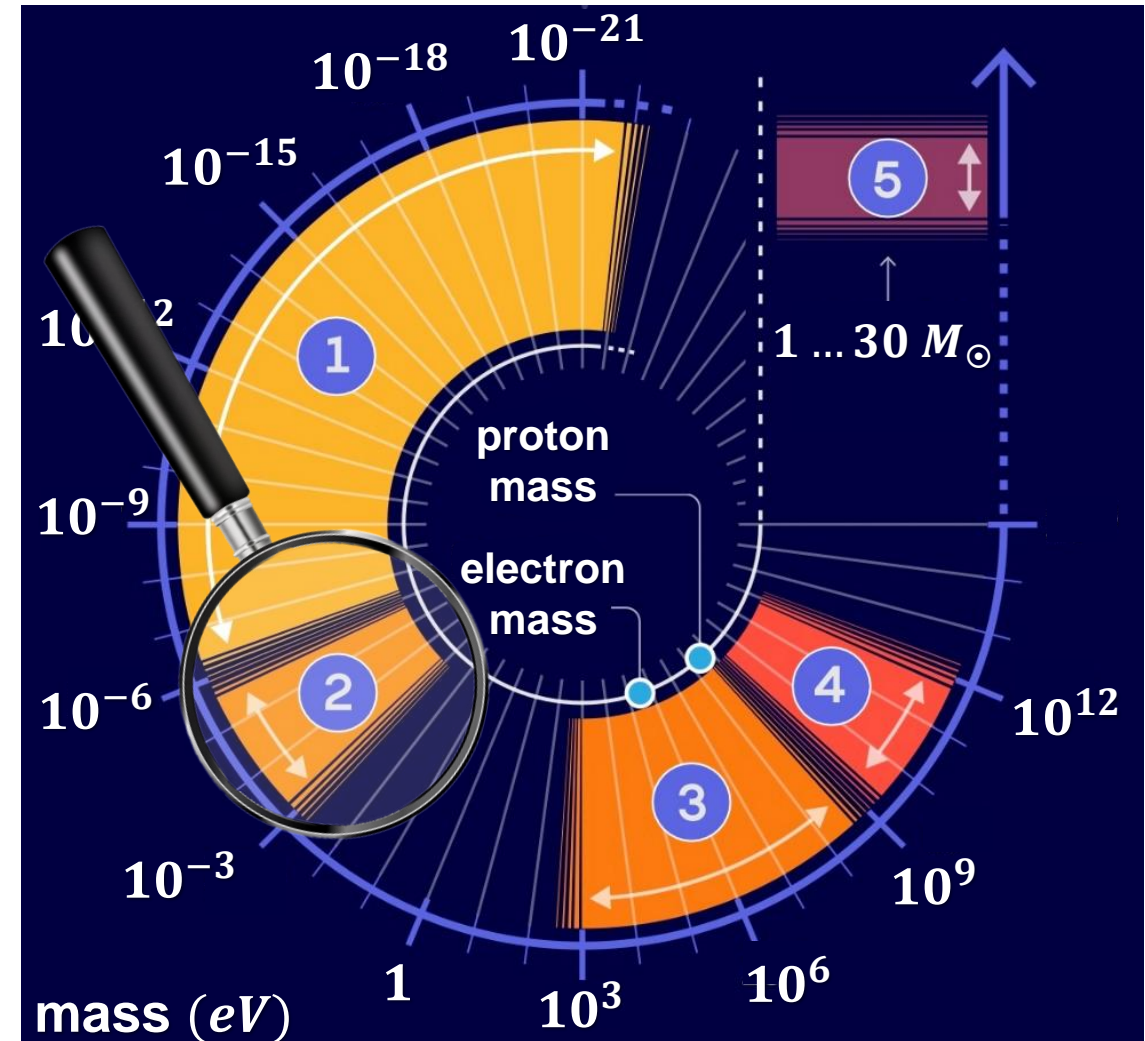
- Hunting **low-mass *WIMPs*** (GeV – scale & below) with **cryogenic bolometers**
 - read-out of **ballistic & thermal phonons** requires mK – temperature regime
 - requirement to minimize **specific heat C_V** : low-mass bolometers $m = g$ – scale
 - **thermal** phonons: read-out via ***NTD*** – thermistors (high impedance)
 - **ballistic** phonons: read-out via ***TES*** – thermistors (low impedance) + ***SQUIDS***
 - **Particle IDentification (*PID*)**: via quenching of charge signal / scintillation light
 - **no *WIMP* – signals** found so far in ***CRESST***, Edelweiss,...

4.6 Non-thermal DM – candidates

■ Generating DM : **non-thermal** means

- A truly broad mass scale:

- ❶ ultra-light DM (Axion-like Particles, ALPs & axions)
- ❷ **axions** (\Rightarrow strong CP –problem)
- ❸ DM on *sub* – GeV scale \Rightarrow bolometers
- ❹ WIMPs: **neutralinos** \Rightarrow Xe/Ar TPCs
- ❺ primordial black holes (MACHOs*)



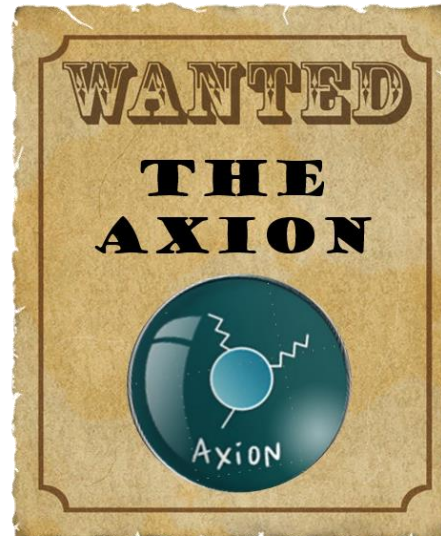
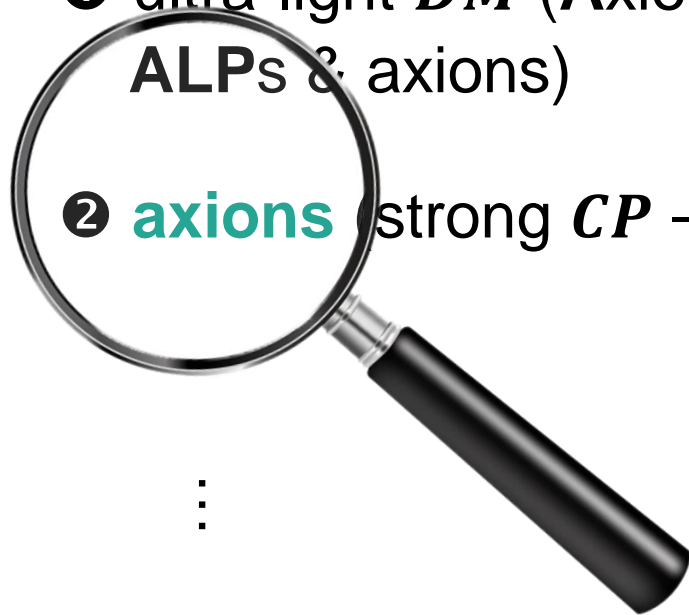
Non-thermal DM – candidates: axions

■ Generating Dark Matter in a non-thermal way by a new symmetry principle

❶ ultra-light DM (Axion-like Particles, ALPs & axions)

❷ axions (strong CP –problem)

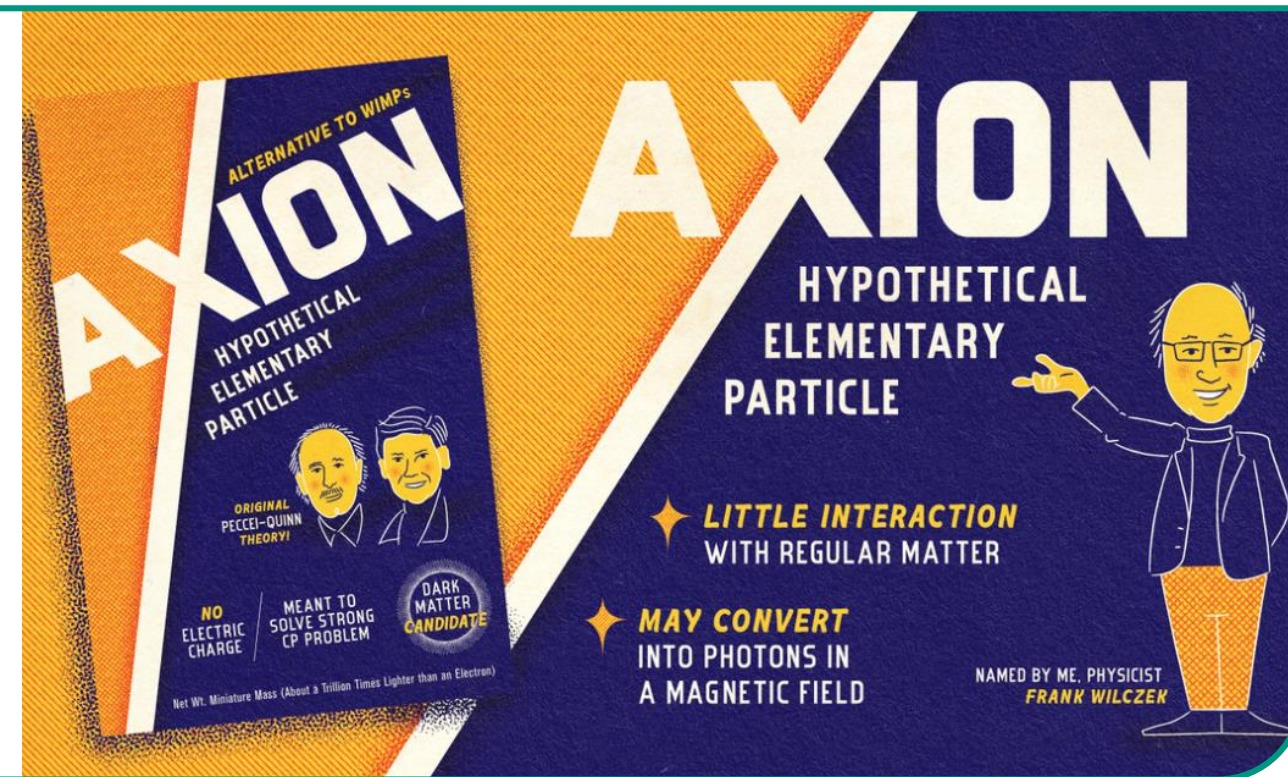
⋮



4.6.1 Axions

■ Properties of axions as Dark Matter in the universe

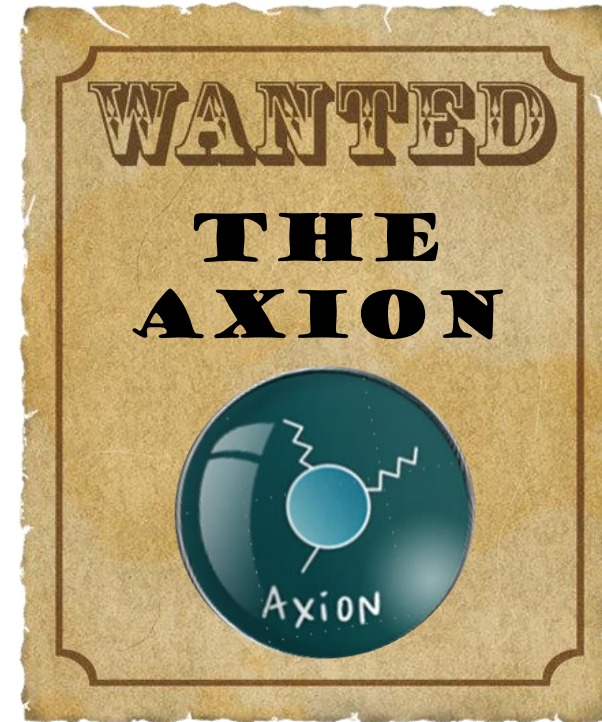
- central motivation for the axion: the **strong CP –problem**



Axions – a completely new *DM* – candidate

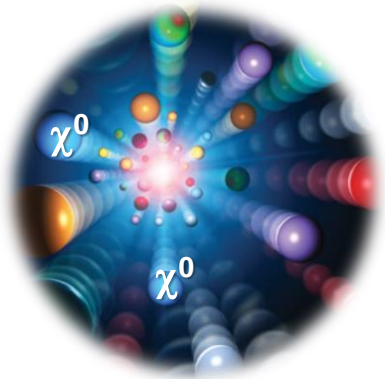
■ Basics of the surprising origin of the axion: ‘who ordered that*?’

- massive neutral boson with $J^P = 0^-$
(pseudo-scalar)
 - ⇒ extremely light: $m_a \sim (10^{-9} \dots 1) \text{ eV}$
 - ⇒ extremely small interaction (coupling)
with normal matter (‘the *invisible* axion’)
 - ⇒ extremely long-lived $\tau_a > \tau_{\text{Hubble}}$ for $m_a < 20 \text{ eV}$
- solves the ‘**strong CP –problem**’



Axions – a completely different *DM* – candidate

- Comparing axions as *WISPs* to our ‘good olde’ massive *WIMPs*



thermal production

WIMP

$$S = \frac{1}{2}$$

‘thermal gas’

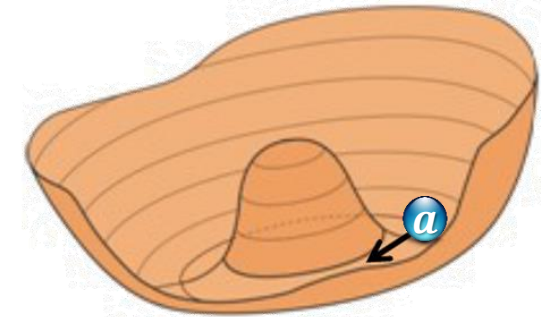


mass:

GeV ... TeV

mass:

$\mu\text{eV} ... \text{meV}$



non-thermal production

WISP

$$S = 0$$

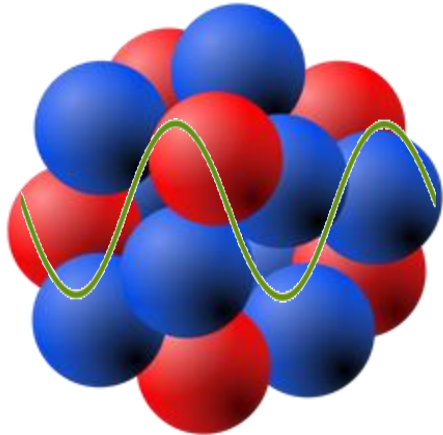
‘Bose condensate’

Axions – a completely different *DM* – candidate

- Comparing axions as *WISPs* to massive *WIMPs*: *de Broglie* wavelength λ



elementary particle

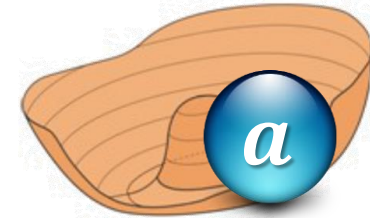


$\lambda \sim nm$



de Broglie wavelength

$$\lambda = \frac{h}{p}$$



field-oscillation

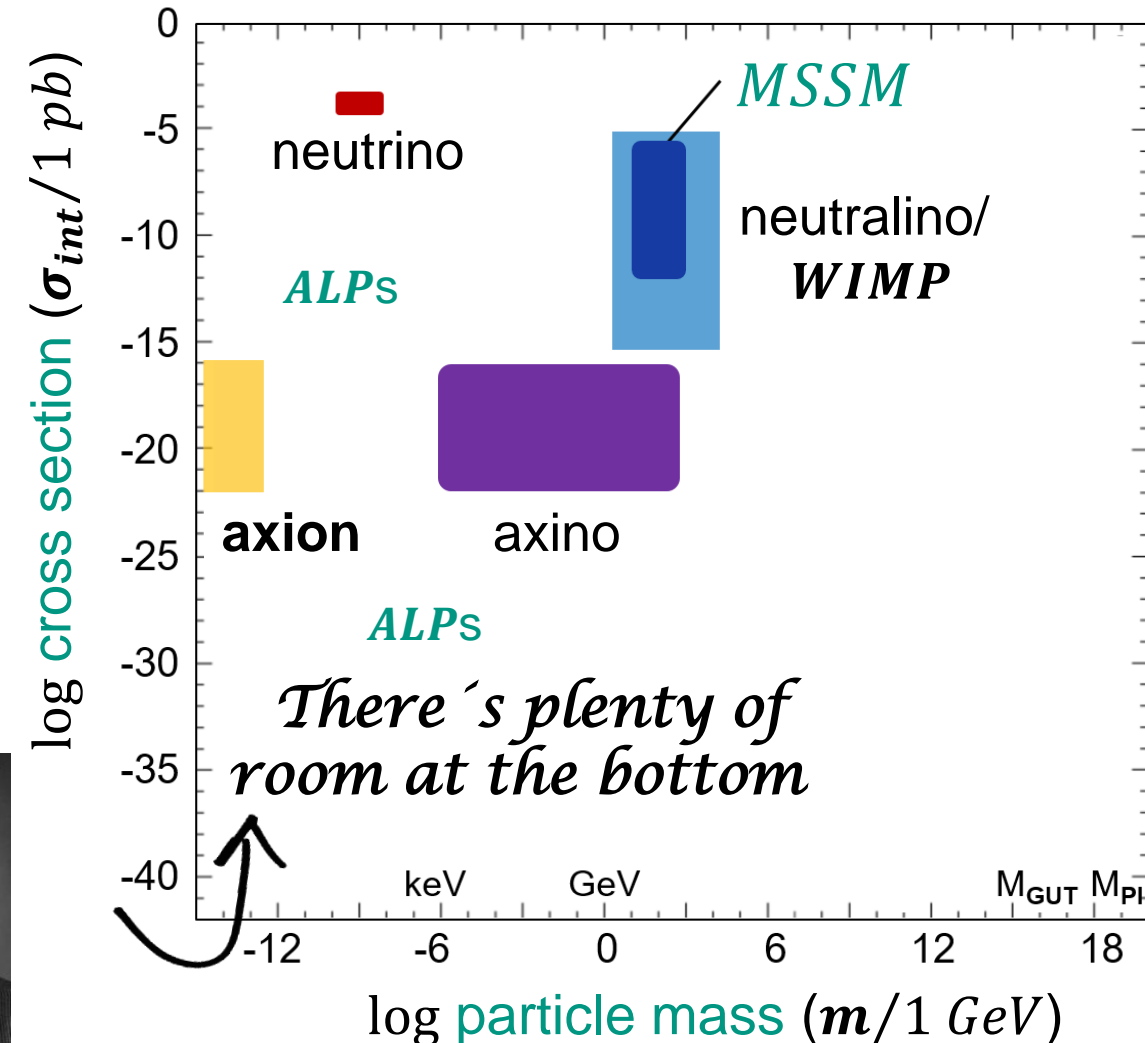


$\lambda \sim m \dots km \dots pc$

RECAP: DM – candidates with mass m & xsec σ

■ Axion a as $WISP$

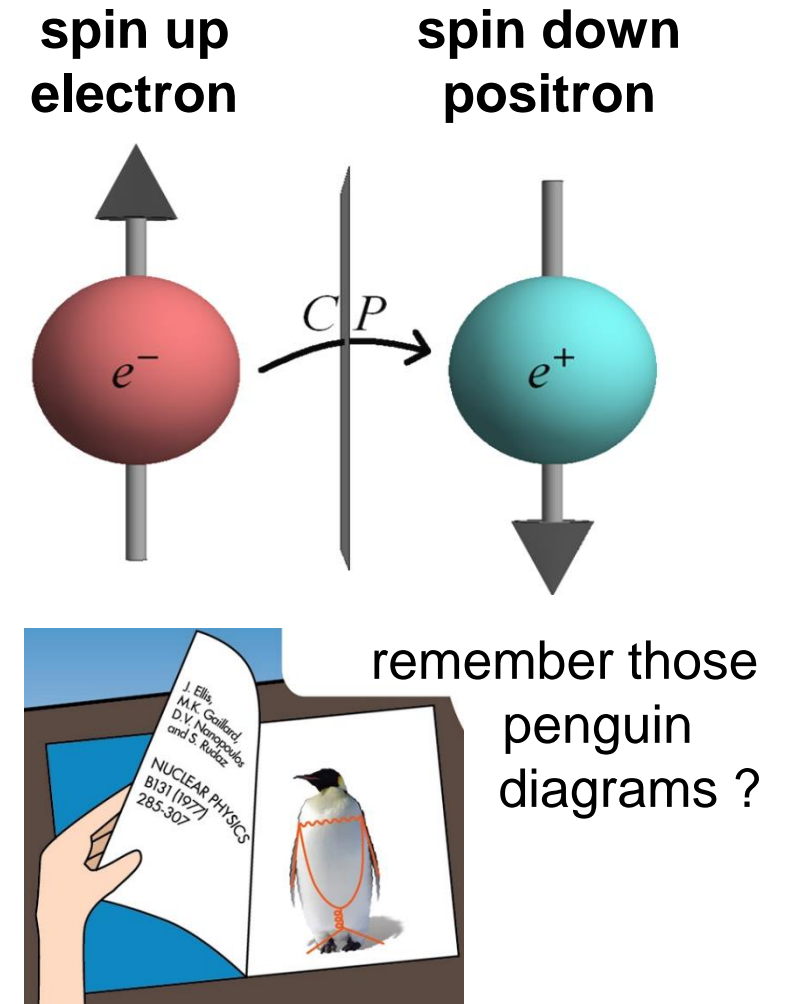
- motivation: ' QCD – axion' for conservation of CP in QCD
- axion = prototype of a $WISP$
- axions could act as CDM in universe if their mass falls in the range:
 $m_a = (10^{-6} \dots 10^{-3}) \text{ eV}$
- $ALPs$ = Axion Like Particles



Axions and the symmetry CP in QCD

■ How to solve the ‘strong CP – problem’

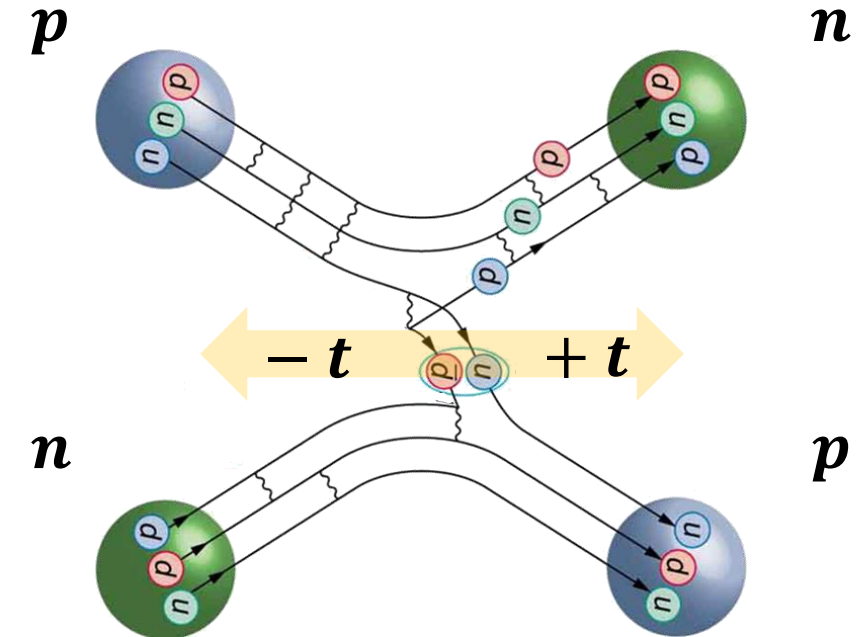
- general statement: in case that **CP invariance** is violated:
 \Rightarrow violation of **T invariance** (& vice versa)
- **CP** – violation so far only detected in the **weak interaction!**
- **CP** – violation has never been detected in the **strong interaction!**



Axions and the symmetry CP in QCD

■ Implications of ‘strong CP – problem’

- general statement: in case that **CP invariance** is violated:
 \Rightarrow violation of **T invariance** (& vice versa)
- **CP** – violation so far only detected in the **weak interaction**!
- **CP** – violation has never been detected in the **strong interaction**!



QCD : do we have **CP** – and **T** – symmetry ?

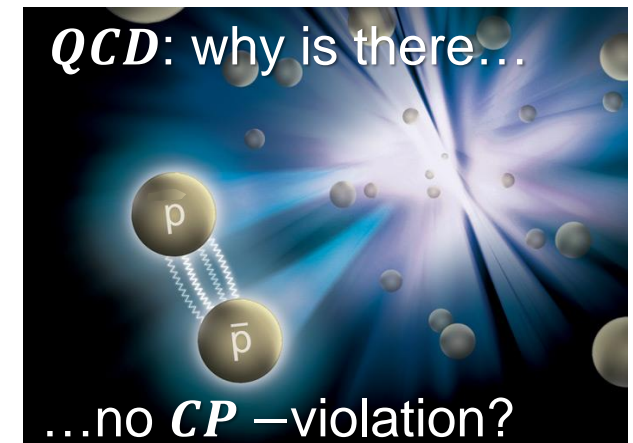
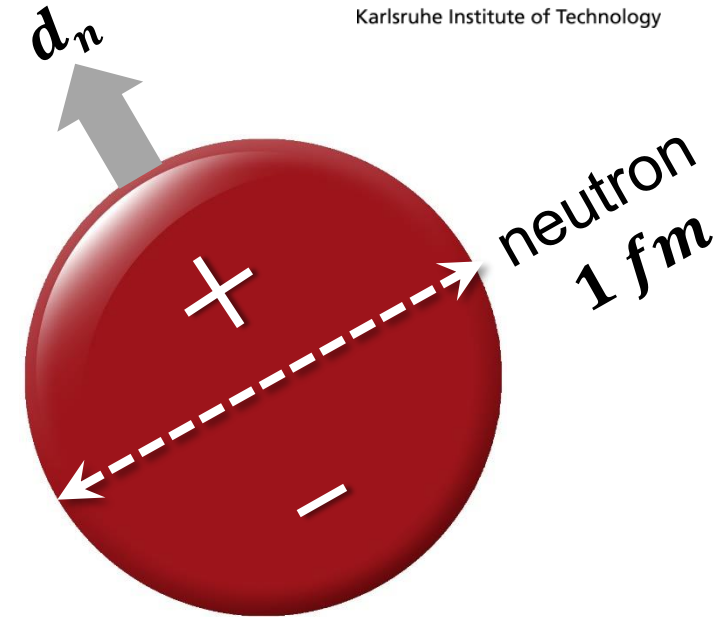
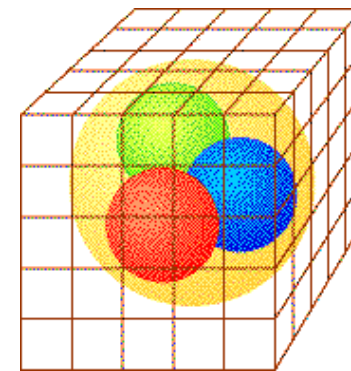
Axions and the symmetry CP in QCD

■ A key observable of the ‘**strong CP – problem**’:
the $n - EDM$

- QCD – **Lagrangian** contains CP – violating terms:
⇒ how can we detect them experimentally?
- we then expect a non-zero value of the **Electric Dipole Moment (EDM)** of the neutron: $d_n \neq 0$

theoretically allowed value (QCD):

$$d_{n,theo} \sim 3.6 \cdot 10^{-16} e \cdot cm$$



Axions and the symmetry CP in QCD

■ A key observable of the '**strong CP – problem**':
the $n - EDM$ in a '**back of the envelope**' ansatz

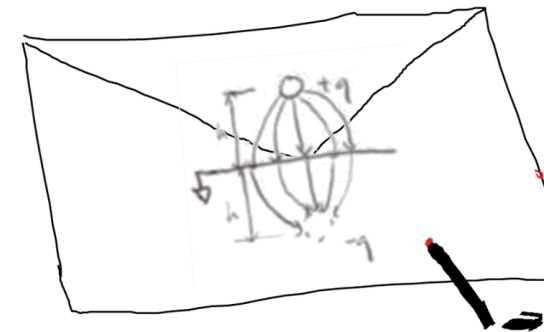
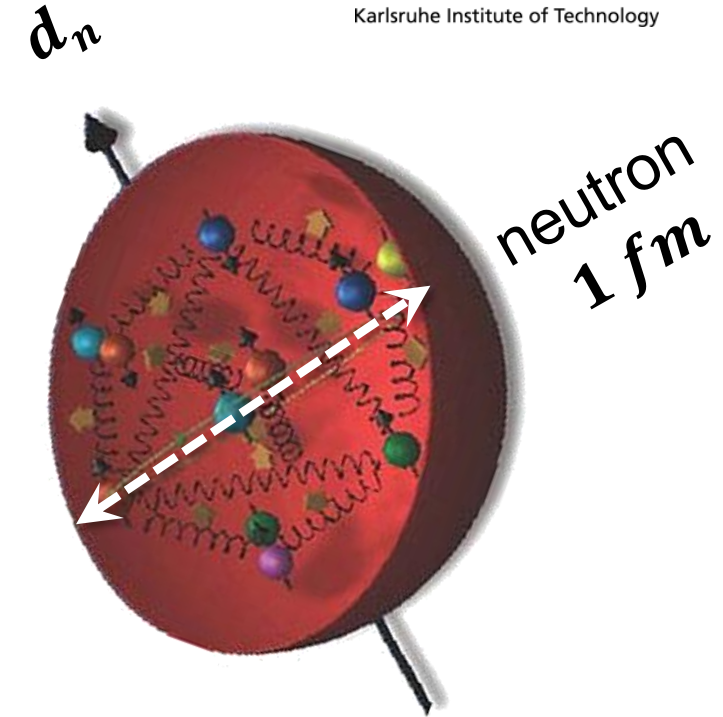
- we estimate a maximum value for EDM of the neutron
- 'naive' model: one quark ($q = 1/3$) over neutron size

$$d_{n,naive} \sim 1/3 \, e \cdot 1 \cdot 10^{-13} \, cm$$

$$d_{n,naive} \sim 3 \cdot 10^{-14} \, e \cdot cm$$

theoretically allowed value (QCD):

$$d_{n,theo} \sim 3.6 \cdot 10^{-16} \, e \cdot cm$$



'back of
the envelope'
calculation

Axions and the symmetry CP in QCD

■ A key observable of the ‘strong CP – problem’:
the $n - EDM$ in experimental searches

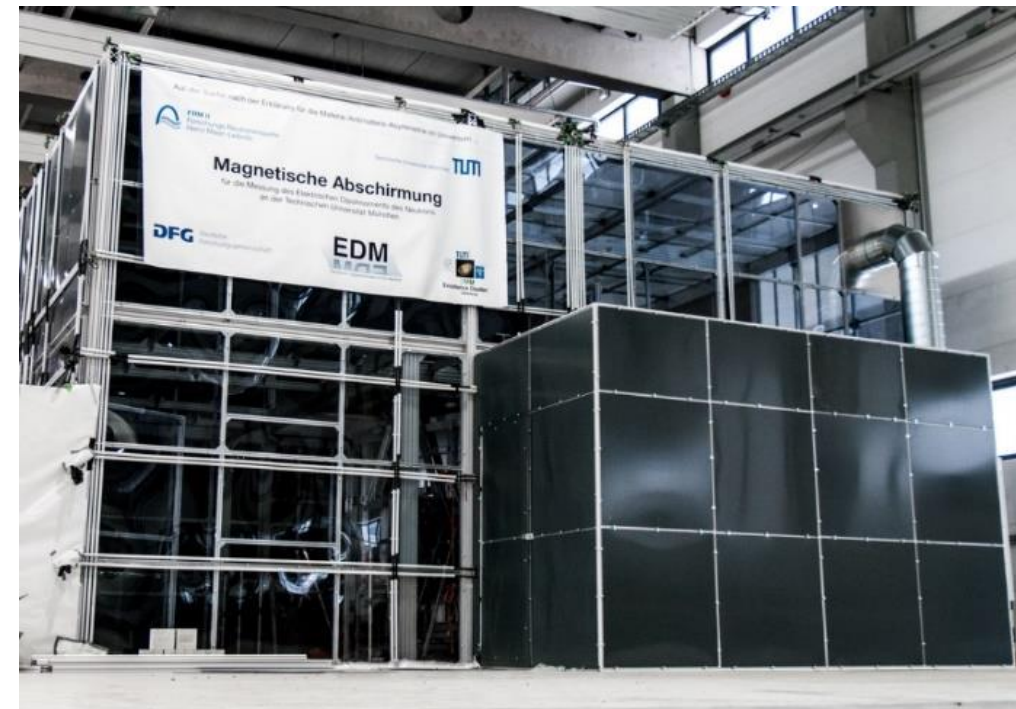
- many experiments looking for EDM of the neutron
- only upper limits published so far:
latest (2020) limit at *Paul Scherrer Institute*



→ $d_{n,exp} < 1.8 \cdot 10^{-26} e \cdot cm \text{ (90\% CL)}$

theoretically allowed value (QCD):

→ $d_{n,theo} \sim 3.6 \cdot 10^{-16} e \cdot cm$



Axions and the symmetry CP in QCD

■ A key observable of the ‘strong CP – problem’:
the $n - EDM$ in our theory understanding today

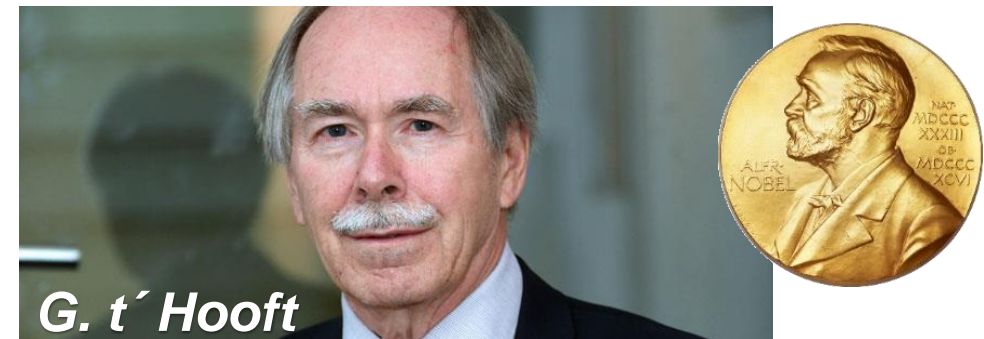
- introduction of an **angle** θ_{QCD} , which parameterizes the amount of CP – violating effects in QCD (or strong interactions)
- vacuum state of QCD is CP –conserving with $|\theta_{QCD}| < 10^{-10}$

θ_{QCD}

$$d_{n,exp} < 1.8 \cdot 10^{-26} \text{ e} \cdot \text{cm} \text{ (90\% CL)}$$

theoretically allowed value (QCD):

$$d_{n,theo} \sim 3.6 \cdot 10^{-16} \text{ e} \cdot \text{cm} \times \theta_{QCD}$$



G. 't Hooft

Axions and the symmetry CP in QCD

■ A key observable of the ‘strong CP – problem’:
the $n - EDM$ in our modern theoretical understanding today

- introduction of an **angle** θ_{QCD} , with a ‘natural’ expectation value in the range of $\theta_{QCD} = [0 \dots 2\pi]$
- extreme fine tuning: why is $|\theta_{QCD}| < 10^{-10}$

θ_{QCD}

$$d_{n,exp} < 1.8 \cdot 10^{-26} e \cdot cm \text{ (90\% CL)}$$

theoretically allowed value (QCD):

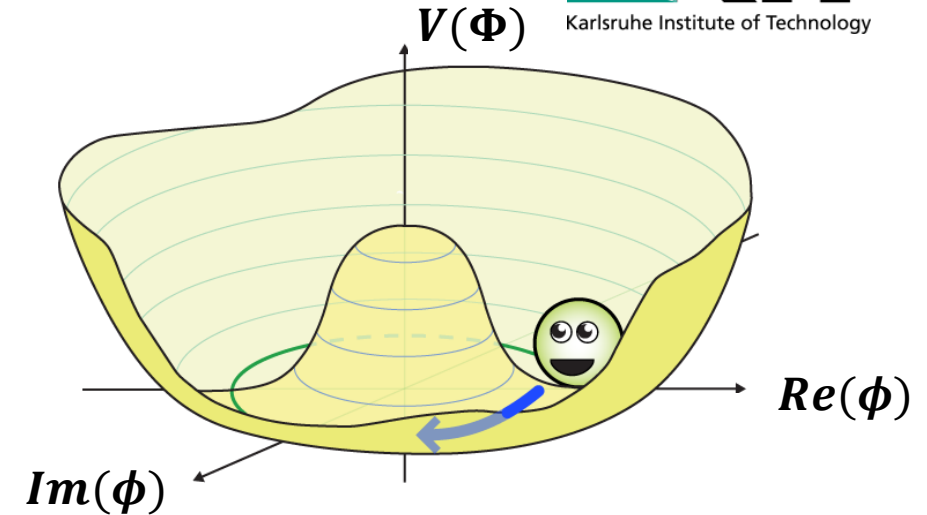
$$d_{n,theo} \sim 3.6 \cdot 10^{-16} e \cdot cm \times \theta_{QCD}$$



Peccei and Quinn: a new symmetry

■ A new $U(1)$ – symmetry to solve the strong CP – problem

- enter a new global (chiral) symmetry $U(1)_{PC}$
- if unbroken, $U(1)_{PC}$ guarantees $\theta_{QCD} \rightarrow 0$
- however, **spontaneous symmetry breaking** of $U(1)_{PC}$ may occur at an (unknown) very high energy scale $f_a = (10^6 \dots 10^{19}) \text{ GeV}$
- **Goldstone-theorem:**
 - ⇒ from this we get a strictly massless scalar gauge-(Goldstone-) boson



Roberto Peccei

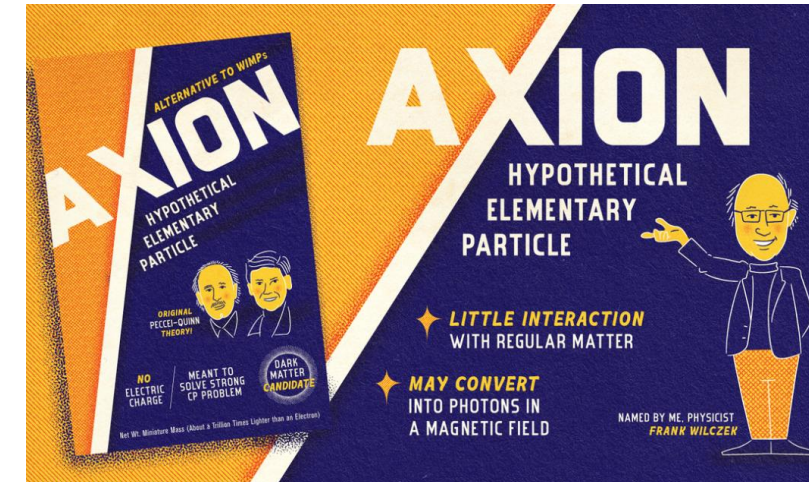


Helen Quinn

Wilczek and Weinberg: explicit breaking of $U(1)_{PC}$

- The **axion** emerges as a very light but massive particle (could it serve as our *DM* –particle?)
 - the new global (chiral) symmetry $U(1)_{PC}$ is not only broken spontaneously, but **explicitly** at the **energy scale of QCD** ('**axial anomaly**')
 - from this we get a **massive new gauge boson α**
 - the new particle, the **axion a** , with its vacuum-expectation-value (**VEV**) explicitly breaks the former symmetry $U(1)_{PC}$

resulting angle: $\theta_{QCD} = a/f_a \Rightarrow 0$



Frank Wilczek



Steven Weinberg

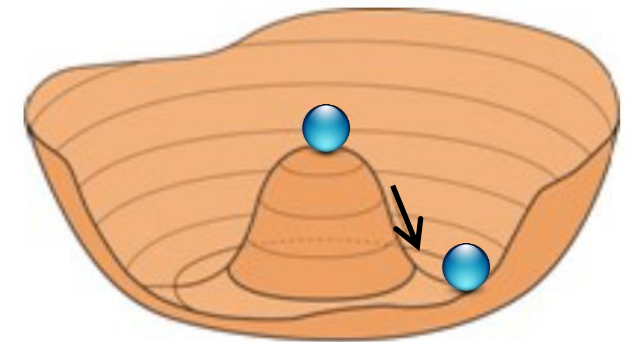
Axion as DM – candidate: history & a bit of theory

■ Axions arise from a broken symmetry: a **non-thermal pathway to DM**

- a close analogy to the very massive Higgs-boson

very early universe: $T \sim f_a$, $T = (10^6 \dots 10^{19}) \text{ GeV}$

- $U(1)_{PC}$ symmetry is broken **spontaneously**
- axion field a rolls down 'Mexican Hat'* potential
 \Rightarrow **massless axions** (Goldstone bosons)
- CP – violating phase θ is in interval $\theta = [0, 2\pi]$
 \Rightarrow CP – violating interactions occur



$$\theta = [0, 2\pi]$$

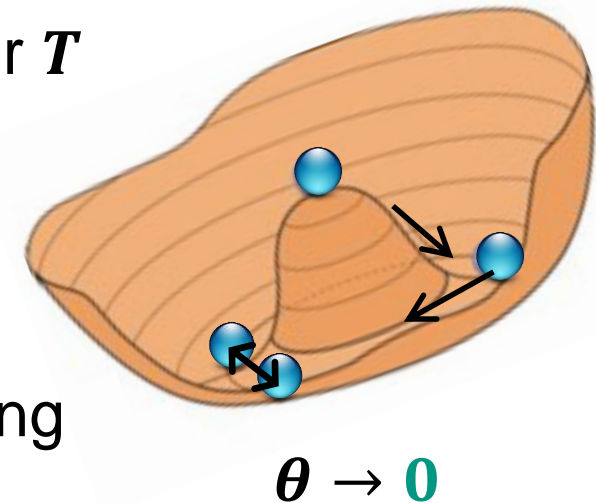
Axion as DM – candidate: history & a bit of theory

■ Axions arise from a broken symmetry: a non-thermal pathway to DM

- a close analogy to the very massive Higgs-boson

very early universe: $T \sim 1 \text{ GeV}$ we have massive DM axions

- $U(1)_{PC}$ symmetry is broken **explicitly** at much lower T
- this occurs due to QCD – vacuum effects ('instantons'): 'Mexican Hat' potential is tilted
- CP – violating phase $\theta = \alpha/f_a \Rightarrow 0 \Rightarrow CP$ – violating interactions stop, **axions as field oscillations**

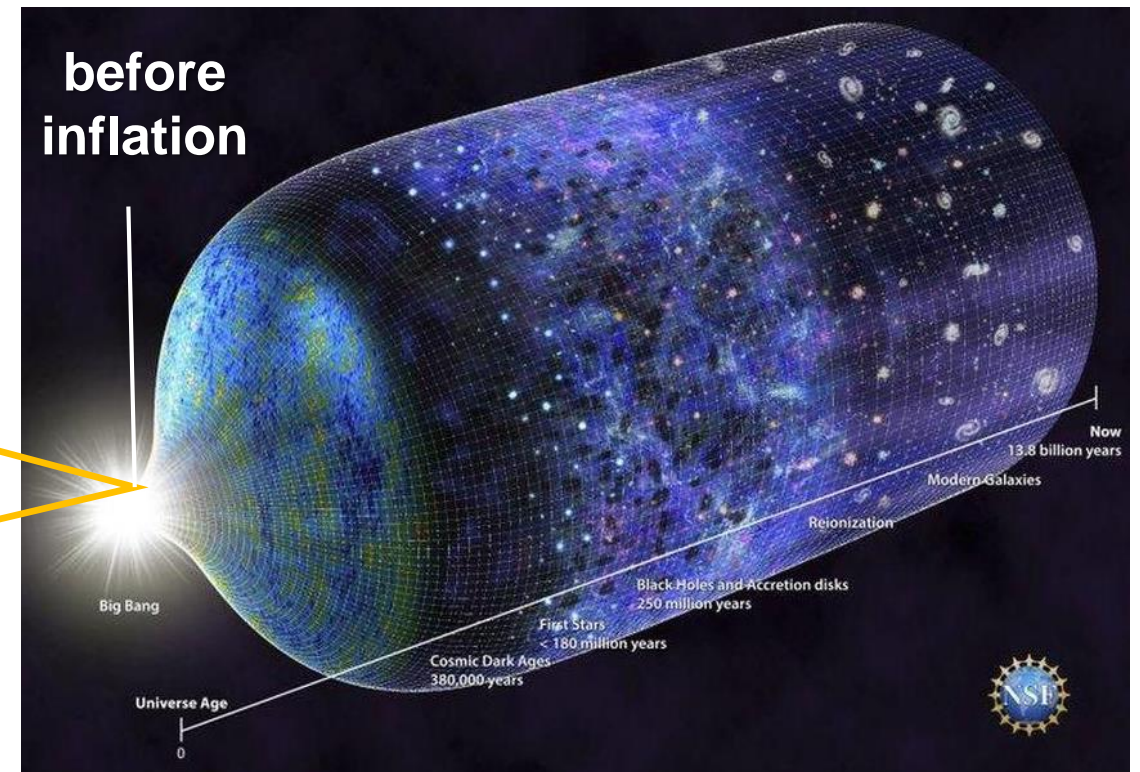
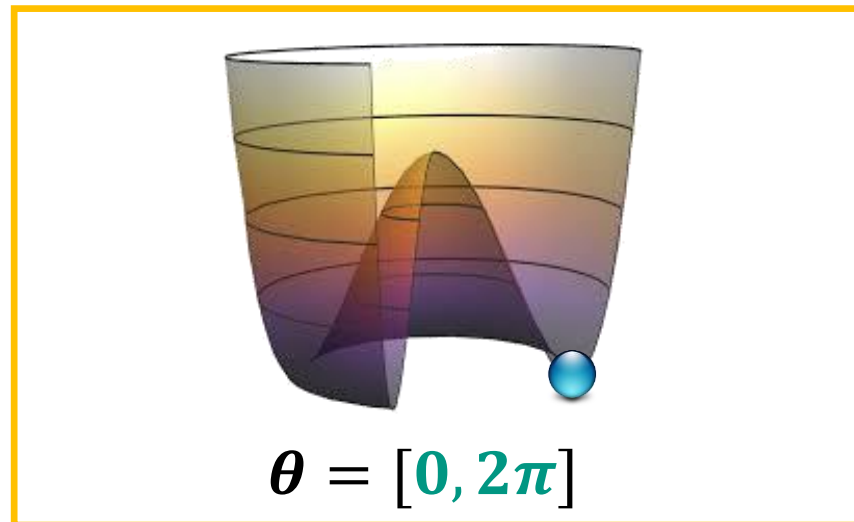


Axion as DM – candidate: history & a bit of theory

■ Spontaneous breaking of PC – symmetry: before or after inflationary phase?

- energy scale f_a is **larger** than GUT – scale relevant for inflation:

only one PQ – phase* in the entire universe, thus: same axion physics everywhere



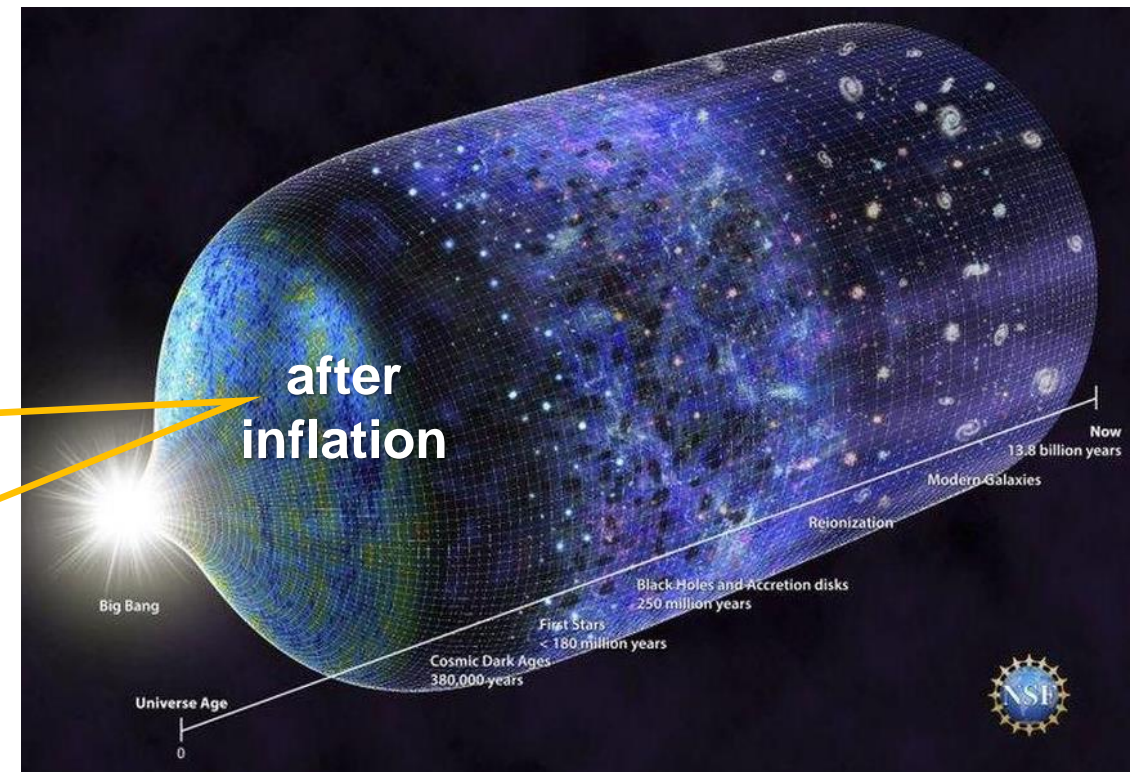
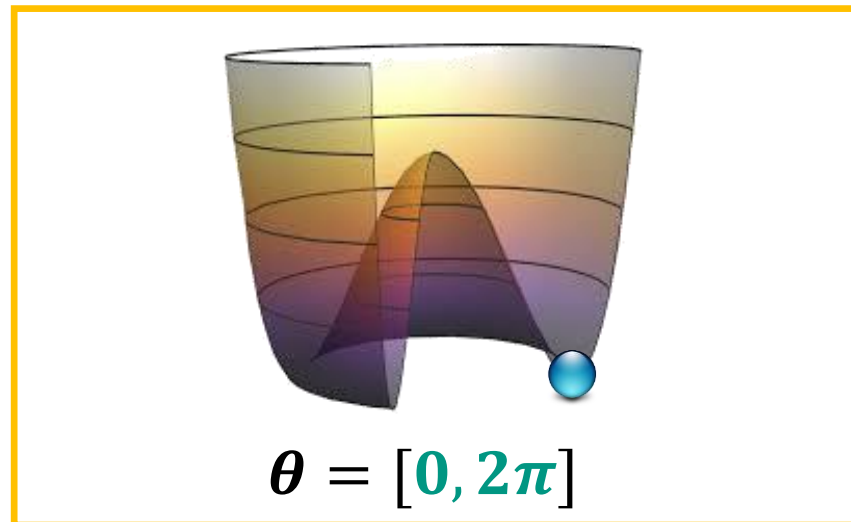
inflationary phase & the physics of axions

Axion as DM – candidate: history & a bit of theory

■ Spontaneous breaking of PC – symmetry: before or after inflationary phase?

- energy scale f_a is **smaller** than GUT – scale relevant for inflation

many PQ – phases in the entire universe, labelled ‘patches’ in between: topological defects



inflationary phase & the physics of axions

Axion as DM – candidate: Wilczeks' 'formula'

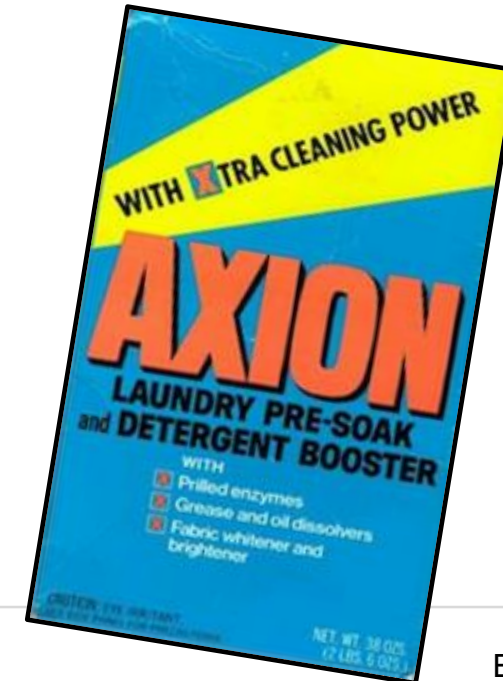
■ Explicitly breaking the Peccei-Quinn symmetry $U(1)_{PC}$

- what does this all mean for DM ?
- we have one particle to solve two issues in physics:

*„I named it **axion**, after the laundry detergent, since it removes a stain“*

a) we cure the 'strong CP – problem'

b) we have a 'well motivated' DM – candidate

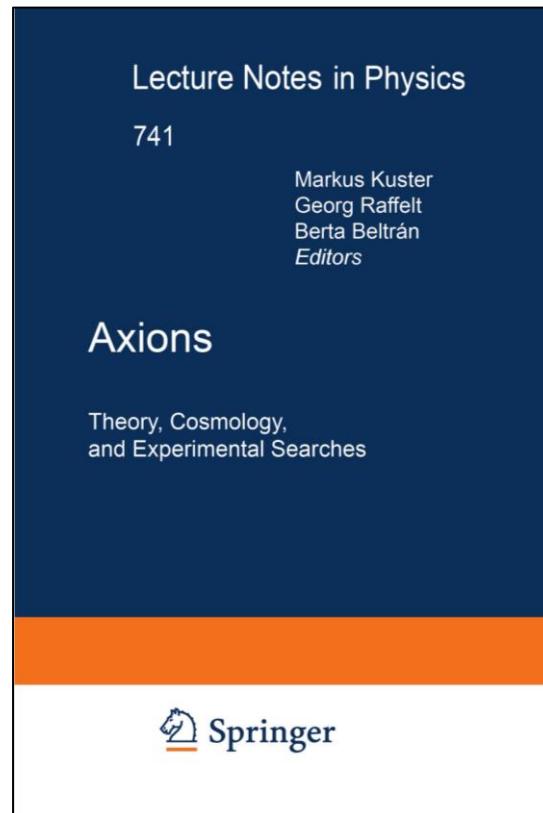


Frank Wilczek

Axion as DM – candidate: Wilczeks' 'formula'

■ Explicitly breaking the Peccei-Quinn symmetry $U(1)_{PC}$

- looking at these axions from all sides...



[10.1007/978-3-540-73518-2.pdf](https://doi.org/10.1007/978-3-540-73518-2.pdf)
([springer.com](https://www.springer.com))



...have a look,
if you like...

*„I named it axion, after
the laundry detergent,
since it removes a stain“*



Frank Wilczek

Axion as DM – candidate: properties at a glance

■ Axions in a nutshell: a light **pseudo-scalar** with $J^P = 0^-$

- **properties of axions**: determined by fundamental **very high energy scale** f_a
- very light axion mass, as : $m_a \sim 1/f_a$
 $10^{-9} \text{ eV} \dots 1 \text{ eV}$
- very small axion coupling strength*: $g_{a\gamma\gamma} \sim m_a$
'the lighter the more difficult to detect...,'
'the invisible axion'
- very long-lived axions, decay typically via $a \rightarrow \gamma\gamma$
rate fixed by $f_a \Rightarrow$ for $m_a < 20 \text{ eV}$: $\tau_a > t_{\text{Hubble}}$



Axion as DM – candidate: comparison to $WIMPs$

■ Axions in our local galactic DM – halo with $\rho_{DM,loc} = 0.3 \text{ GeV}/\text{cm}^3$

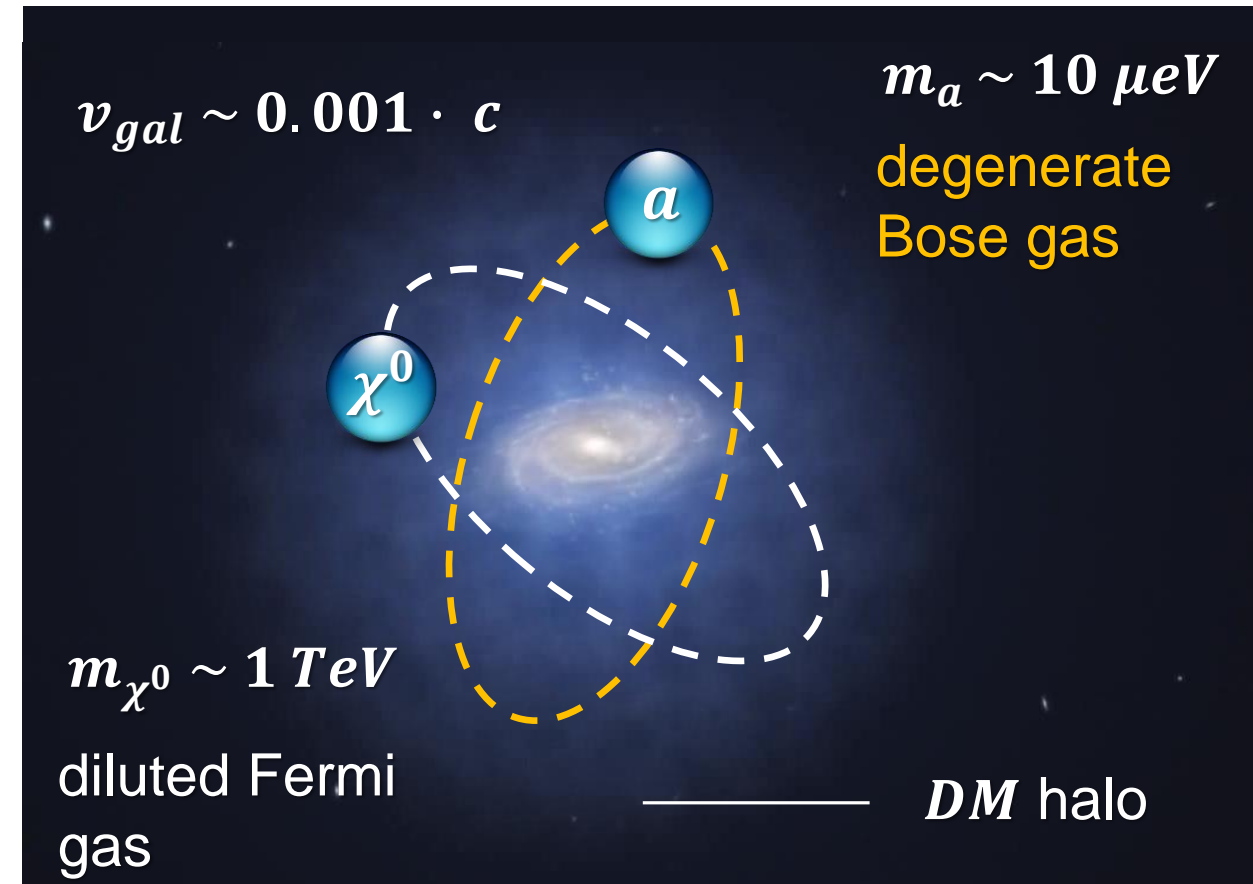
- local **axion** number density:

$$N = 3 \cdot 10^{13} / \text{cm}^3 \quad (\text{for } m_a = 10 \mu\text{eV})$$

- local **WIMP** number density:

$$N = 3 \cdot 10^{-4} / \text{cm}^3 \quad (\text{for } m_{\chi^0} = 1 \text{ TeV})$$

- comparable mean velocities in the DM – halo: $v_{gal} \sim 0.001 \cdot c$



local halo: comparing neutralinos to axions

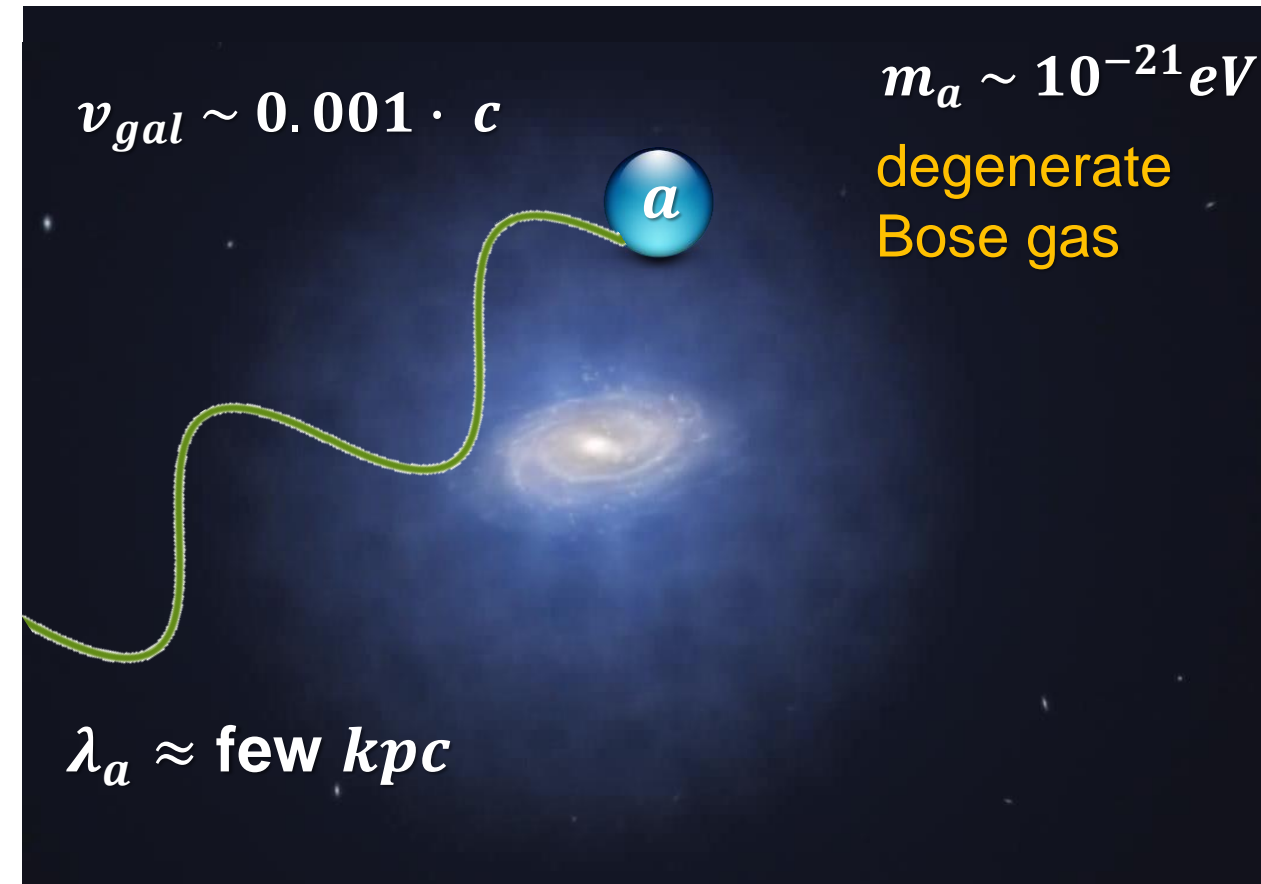
Axion as *DM* – candidate: *de Broglie* wavelength

■ Axions in *DM* – halos: do they fit in even in case of dwarf galaxies?

- definition of *de Broglie* wavelength λ_a :

$$\lambda_a \approx \frac{2\pi}{m_a \cdot v_{gal}} = 100 \text{ m} \cdot \frac{10 \mu\text{eV}}{m_a}$$

- for extremely tiny axion masses of $m_a \approx 10^{-21} \text{ eV}$ we thus reach a value of $\lambda_a \approx \text{few kpc}$, the size of a typical dwarf galaxy (\equiv a **lower** bound on m_a)



local halo: axion de Broglie wavelength...

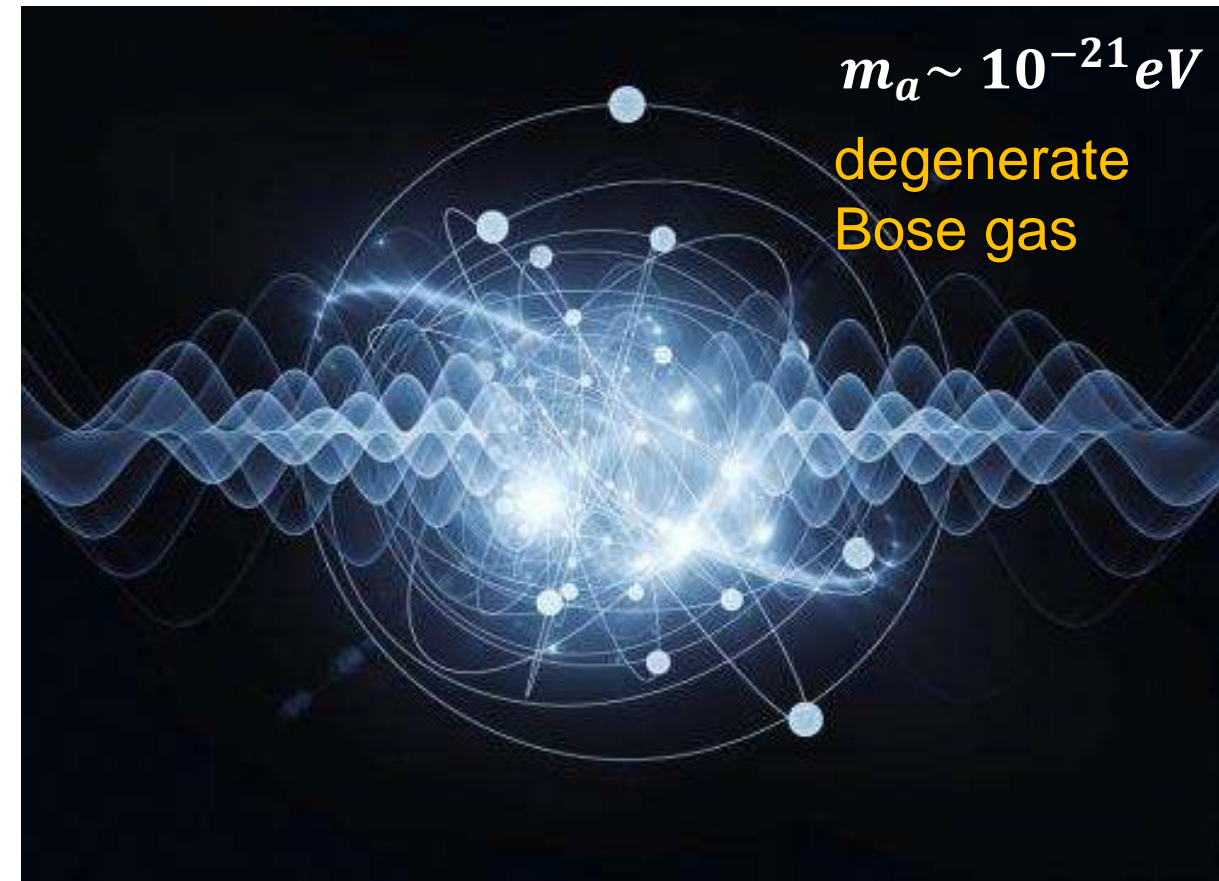
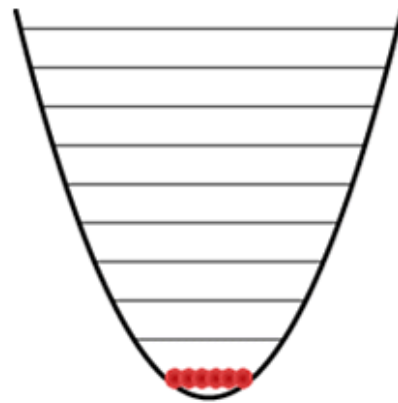
Axion as *DM* – candidate: a Bose condensate

■ Axions in *DM* – halos: they can form a Bose-Einstein condensate

- typical occupation numbers:

$$n_a \approx 10^{25} \cdot \left(\frac{10 \mu\text{eV}}{m_a} \right)^4$$

- thermalised axions can form a **Bose-Einstein condensate** in the galactic halo



local halo: how to visualize a condensate?

Axion as *DM*: scale m_a

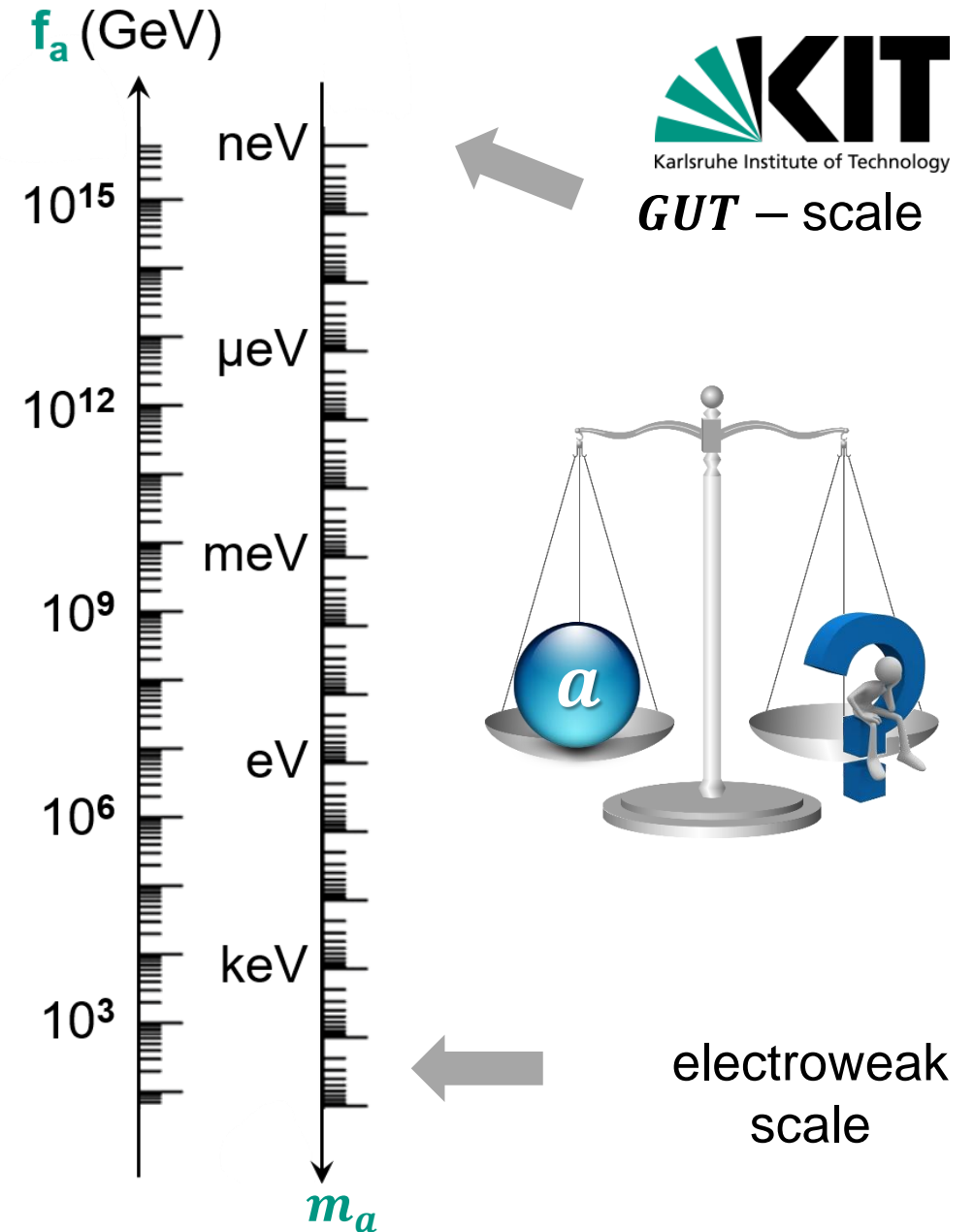
■ Comparing the energy scale f_a with the mass m_a of axions

- axion mass scale m_a is given by the energy scale f_a where the Peccei-Quinn symmetry $U(1)_{PQ}$ is broken

$$m_a \approx 6 \text{ eV} \cdot \frac{10^6 \text{ GeV}}{f_a}$$

small $m_a \Leftrightarrow$ high scale f_a

large $m_a \Leftrightarrow$ low scale f_a



Axion as DM : scale Ω_a

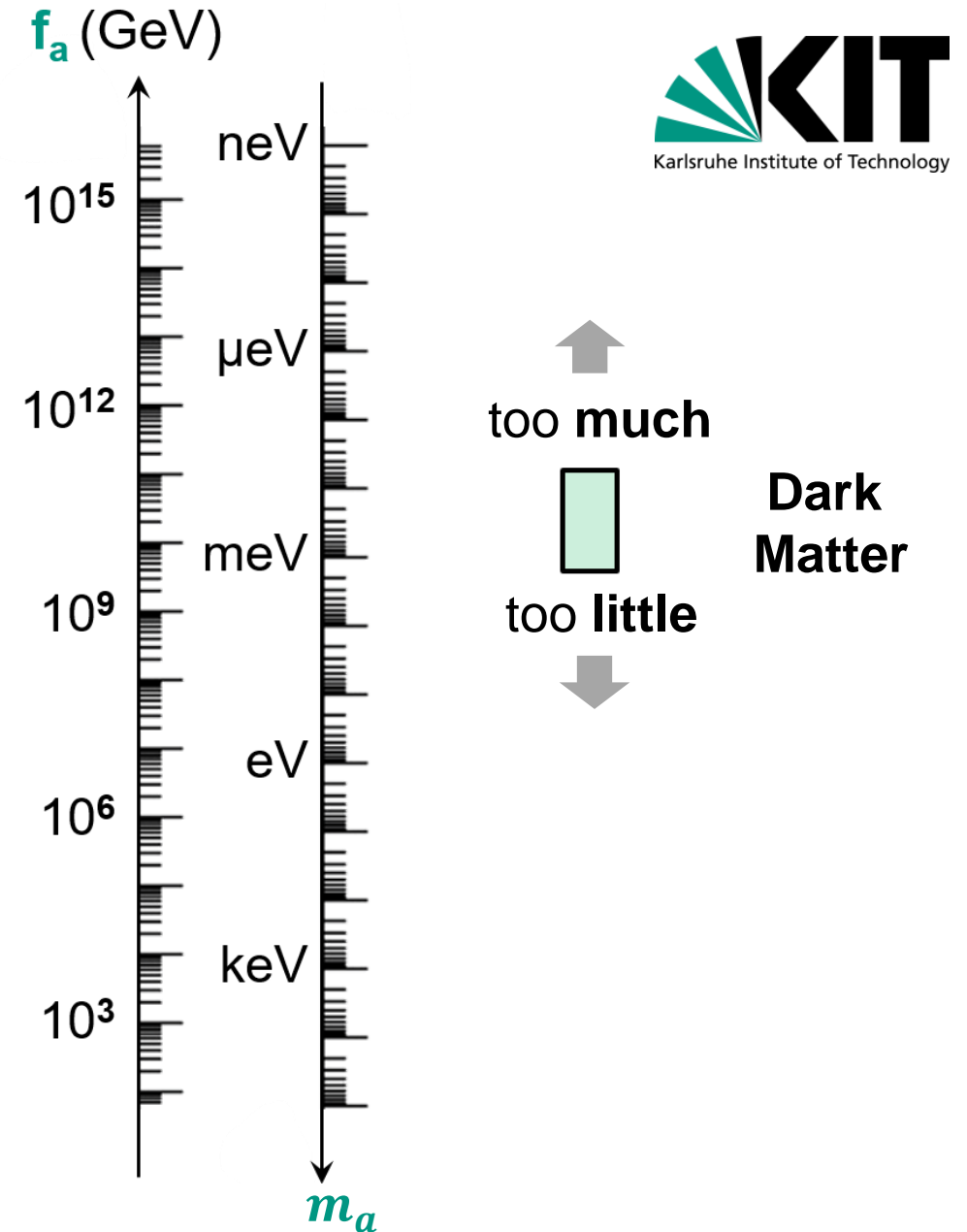
■ Comparing the mass scale m_a & the DM – contribution Ω_a of axions

- axion mass scale m_a is strongly model-dependent, but there is a region where m_a ideally fits to obtain a value $\Omega_{DM} \approx 0.27$

$$\Omega_a \approx \left(\frac{6 \mu eV}{m_a} \right)^{7/6} \quad (\text{popular 'vacuum misalignment model'})$$

small $m_a \Leftrightarrow$ (too?) high fraction of Ω_a

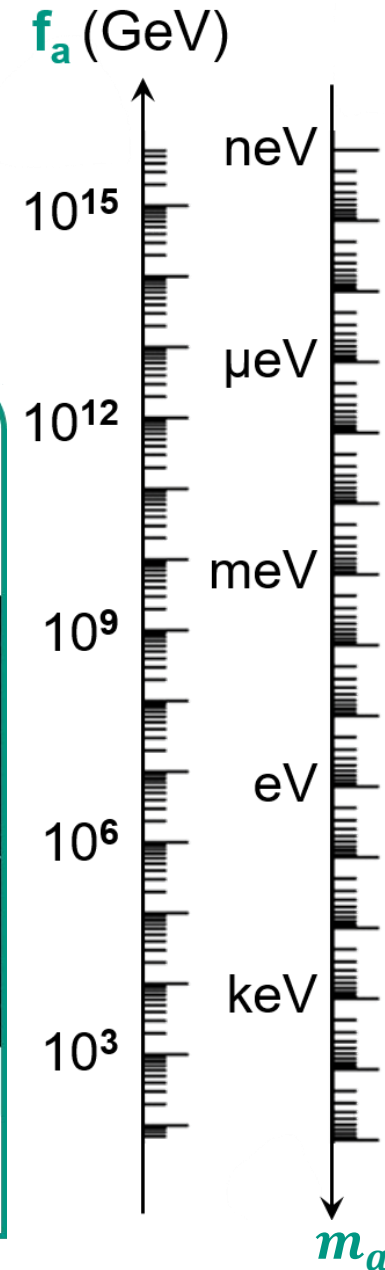
large $m_a \Leftrightarrow$ (too?) small fraction of Ω_a



Axion as *DM*: *QCD* calculations

- Calculating the **mass scale m_a**
& the ***DM* – contribution Ω_a** of axions

- 2016: new **lattice-*QCD* results** seem to point to a **very interesting m_a**



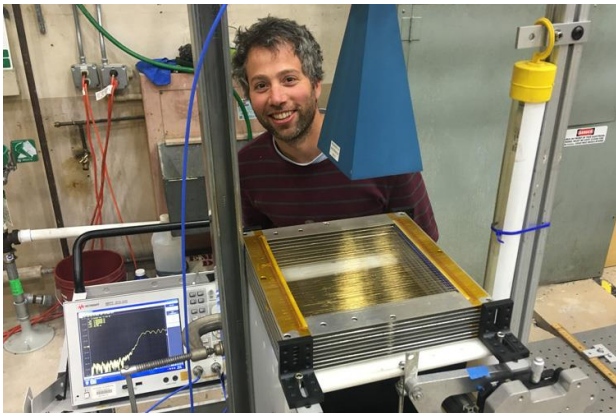
most probable
QCD axion
 $m_a = 50 \dots 1500 \mu eV$

local axion density
 $N_a \approx 10^9 / cm^3$

Axion as *DM*: *QCD* calculations

- Calculating the mass scale m_a & the *DM* – contribution Ω_a of axions

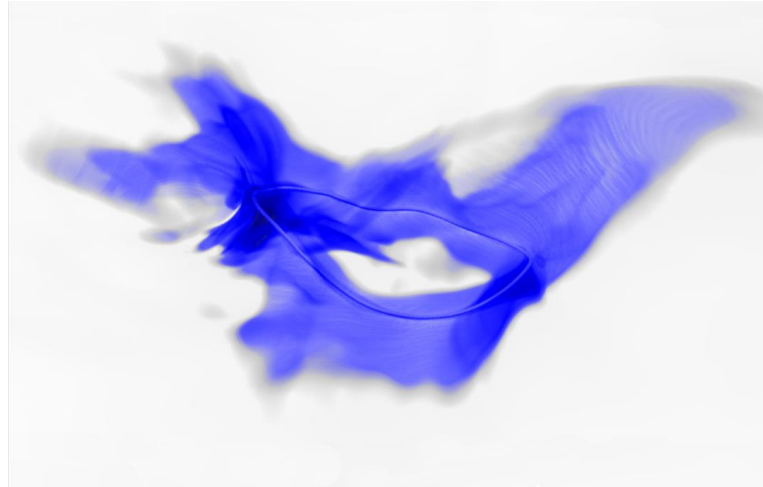
- 2022: new **lattice-*QCD* results** seem to point to an even more interesting $m_a \approx 65 \mu\text{eV}$



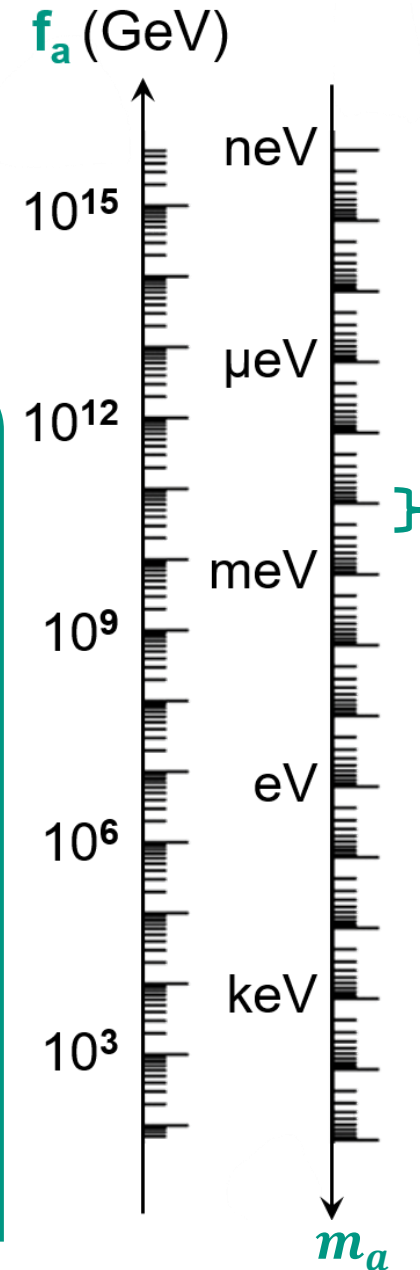
Berkeley News

RESEARCH, SCIENCE & ENVIRONMENT, TECHNOLOGY & ENGINEERING

New simulations refine axion mass, refocusing dark matter search



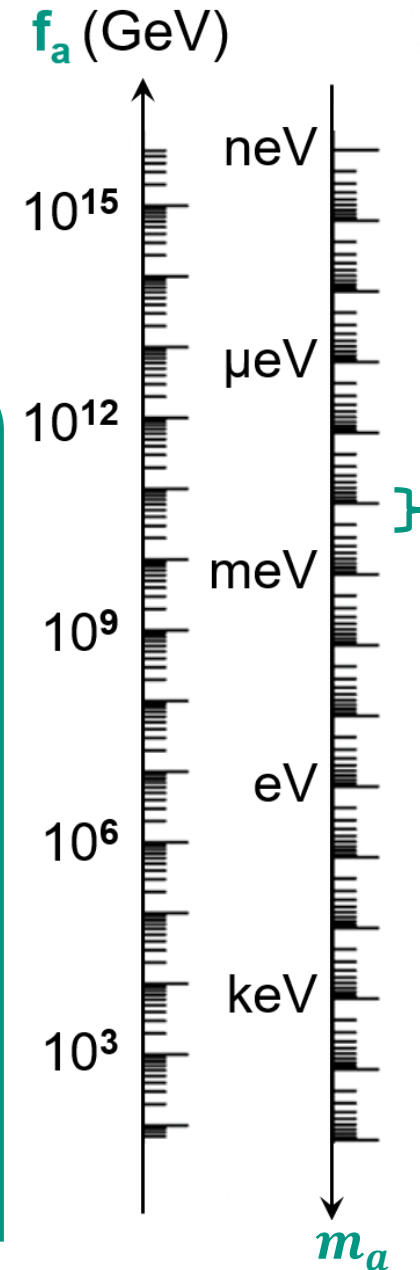
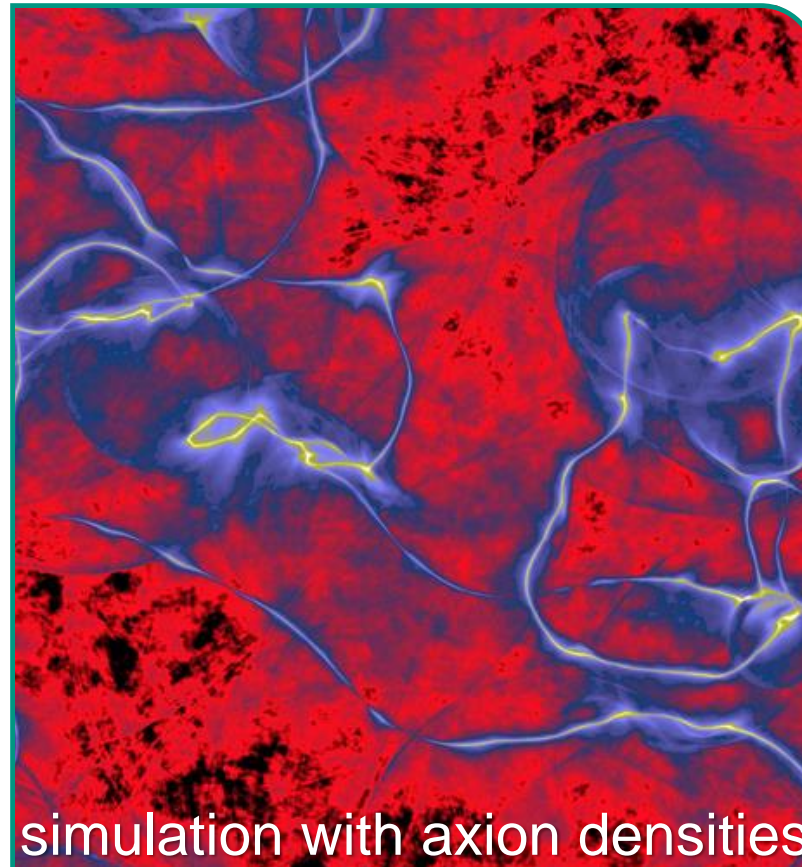
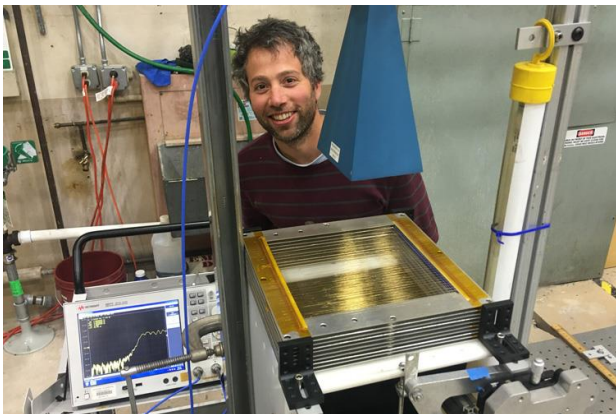
In a simulation of the early universe, shortly after the Big Bang, tornado-like strings (dark blue loop) throw off axion particles. These axions should still be around today, and could be the dark matter that astrophysicists have been searching for. (Credit: Malte Buschmann, Princeton University)



Axion as *DM*: *QCD* calculations

- Calculating the mass scale m_a & the *DM* – contribution Ω_a of axions

- 2022: new **lattice-*QCD* results** seem to point to an even more interesting $m_a \approx 65 \mu\text{eV}$



most probable
QCD axion
 $m_a = 40 \dots 180 \mu\text{eV}$

Axion as *DM*: cosmological limits

■ Cosmology requests light axions on the *sub – eV* scale

- axions have to act as **Cold Dark Matter**

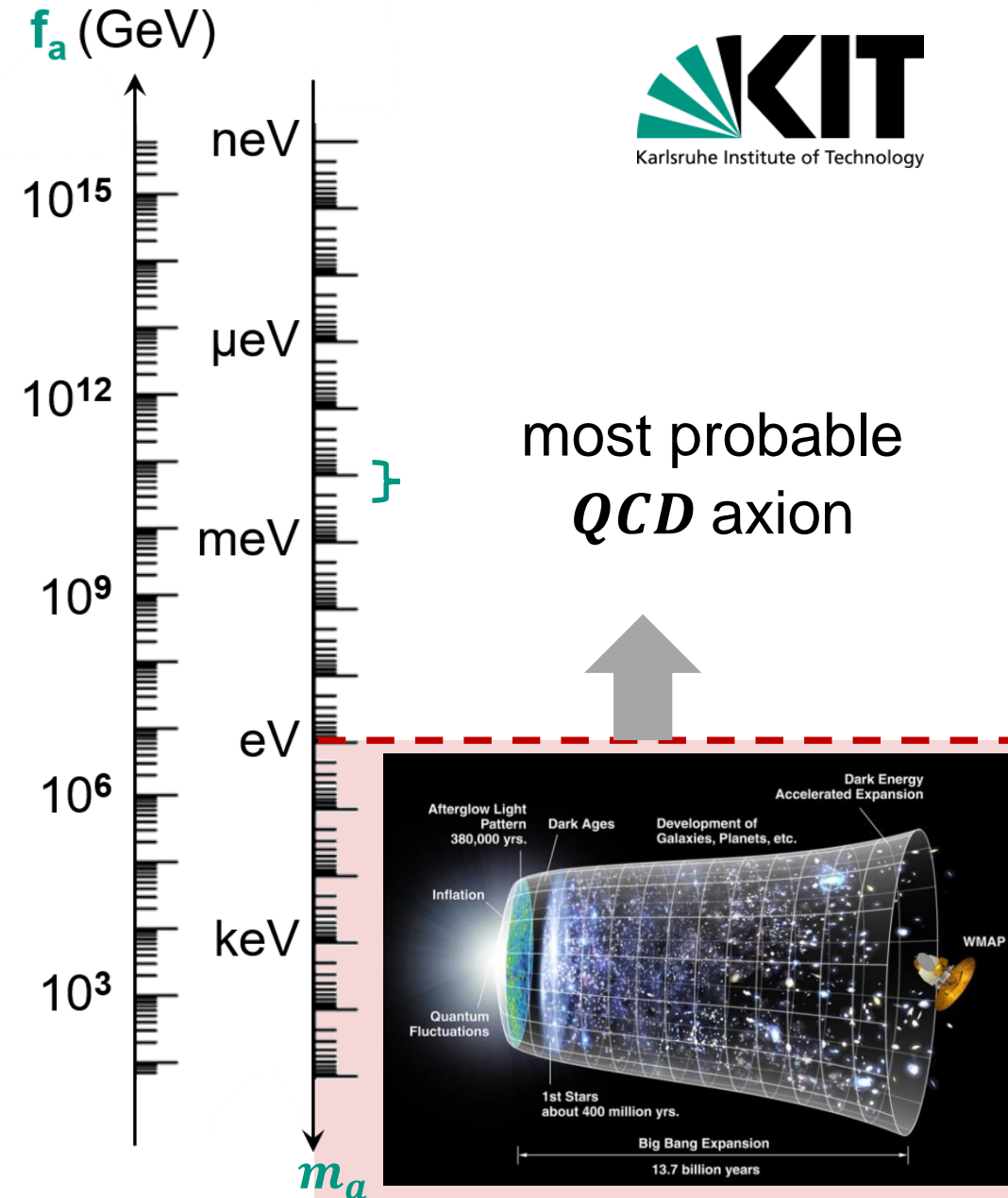
$$m_a < 1 \text{ eV}$$

for larger masses m_a : axions would be **Hot Dark Matter**, in contrast to the Λ CDM concordance model of cosmology

- also: axion lifetime requirement: $\tau_a > t_H$

$$m_a < 20 \text{ eV}$$

no axion decays occur over Hubble time t_H



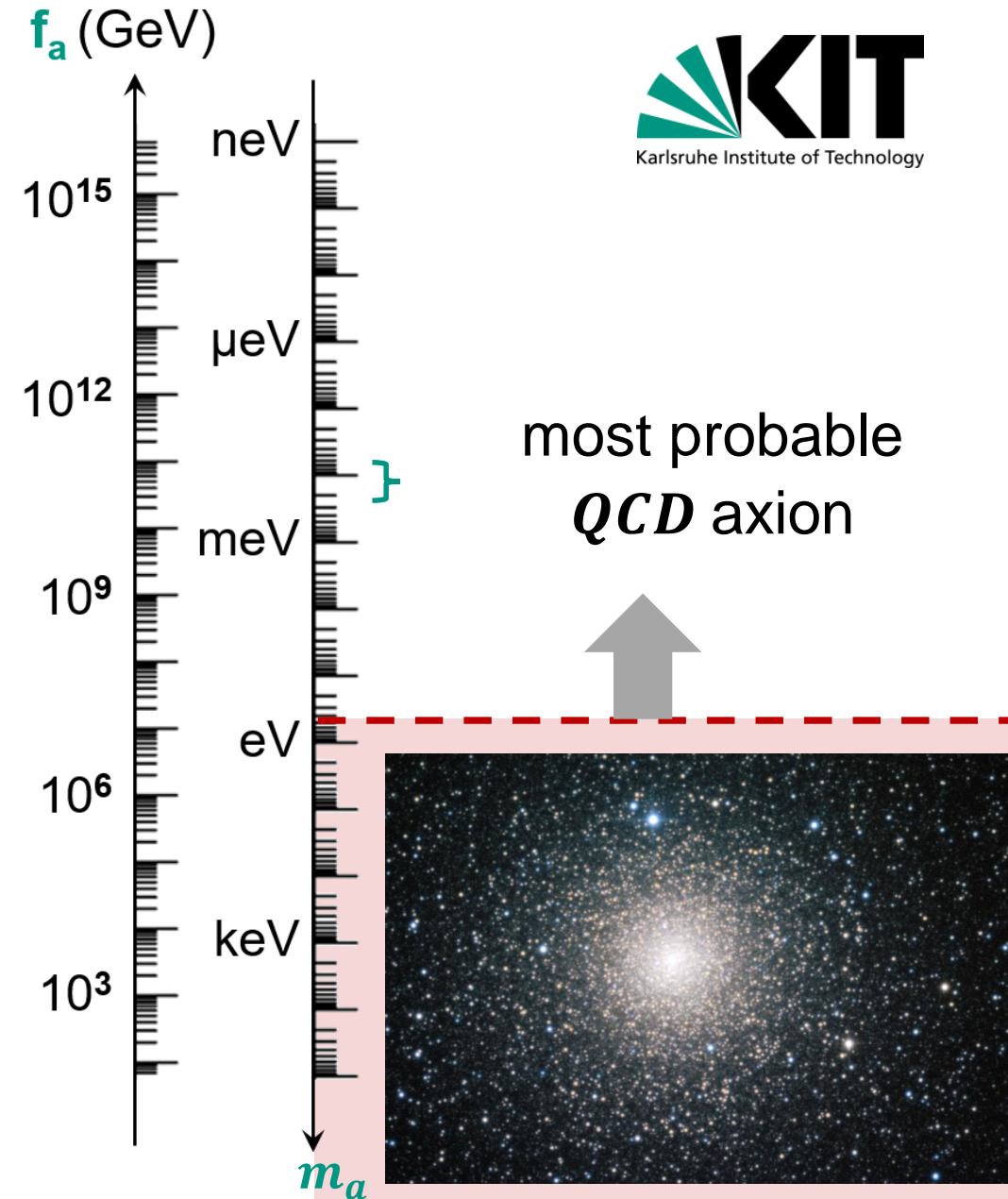
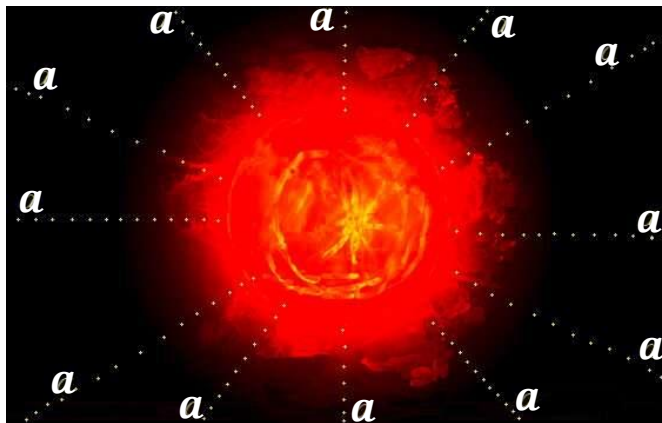
Axion as *DM*: astrophysical limits

■ Astrophysics requests light axions on the *sub – eV* scale

- no axion emission from **stars**

$$m_a < 0.5 \text{ eV}$$

from the evolution of globular clusters & long stellar lifetimes (*He* – burning phase)



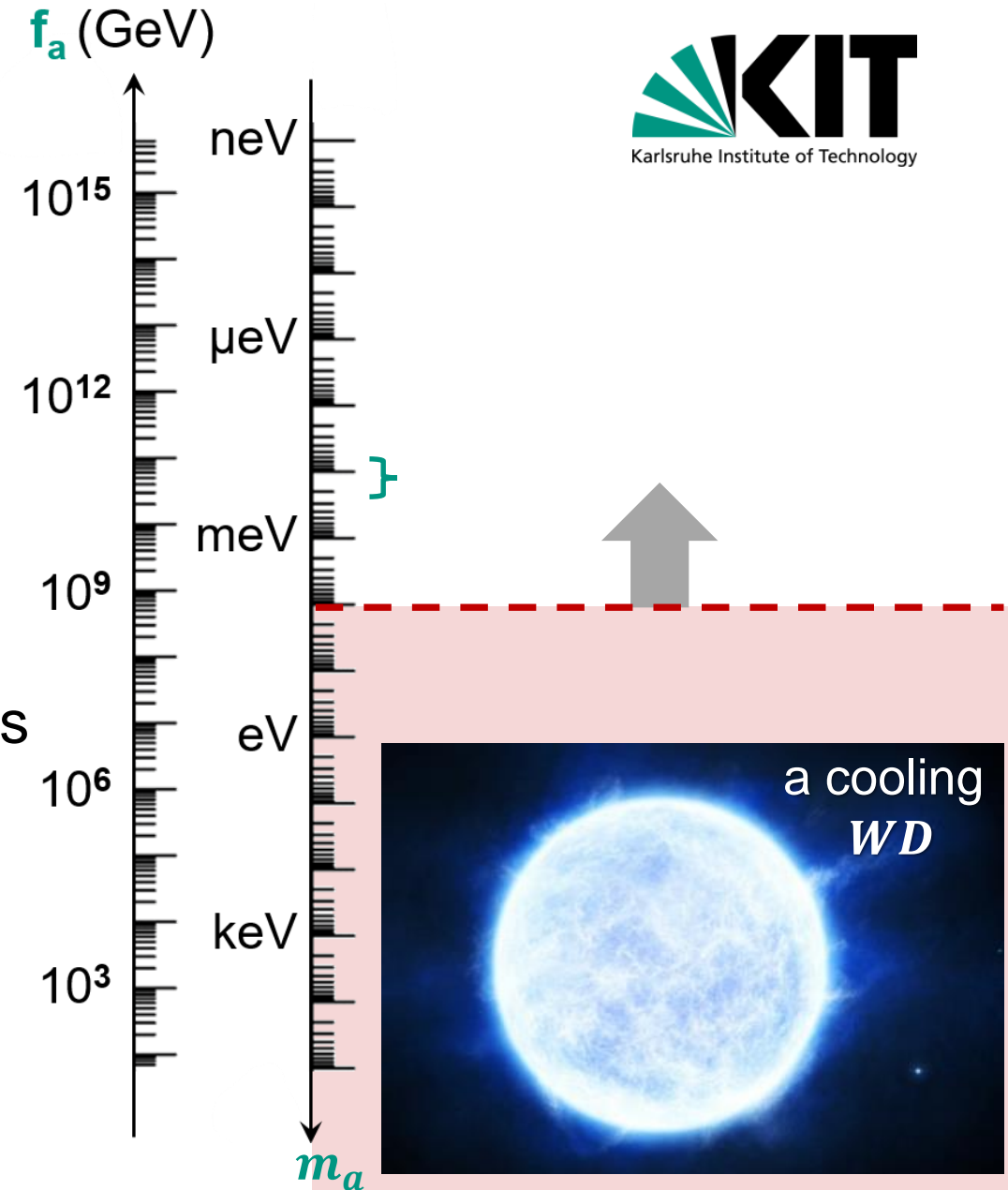
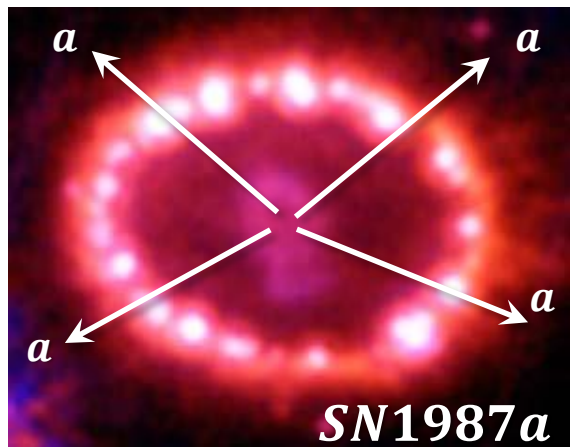
Axion as *DM*: astrophysical limits

- Astrophysics requests light axions on the *sub – eV* scale

- no axion emission from **supernovae, WDs***

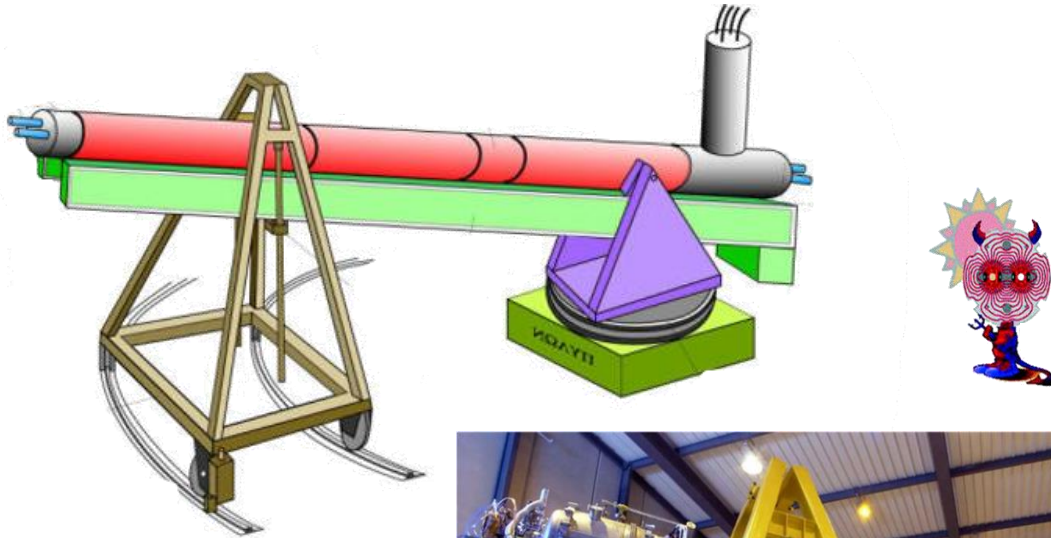
$$m_a < 16 \text{ meV}$$

from the 1987 observation of a 10 s ν -pulse in *SN1987a* & very long cooling times of *WDs*

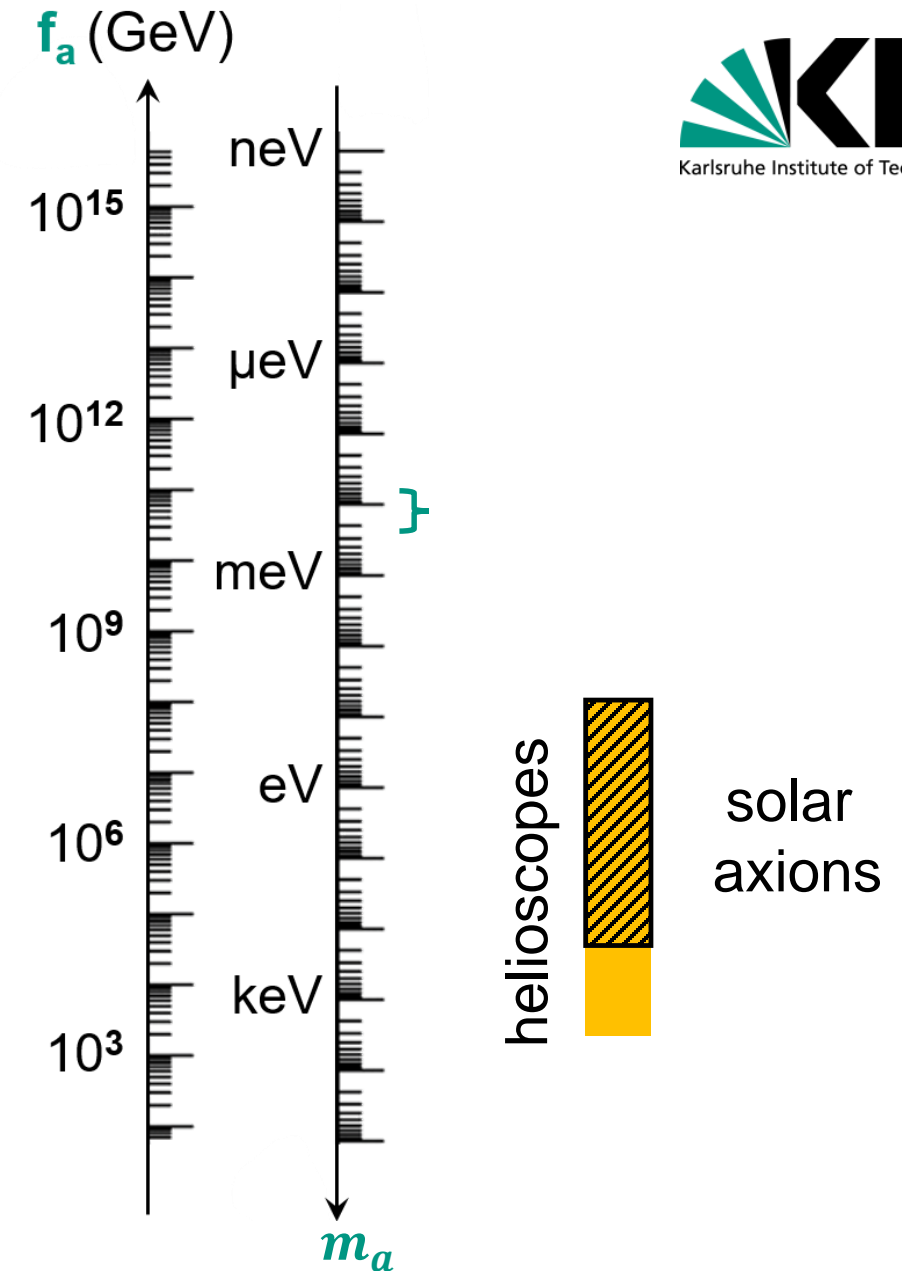


Axions: 'telescope' searches

■ Helioscopes: axions from the Sun?



- let's look into the heart of the Sun to see if axions are emitted there

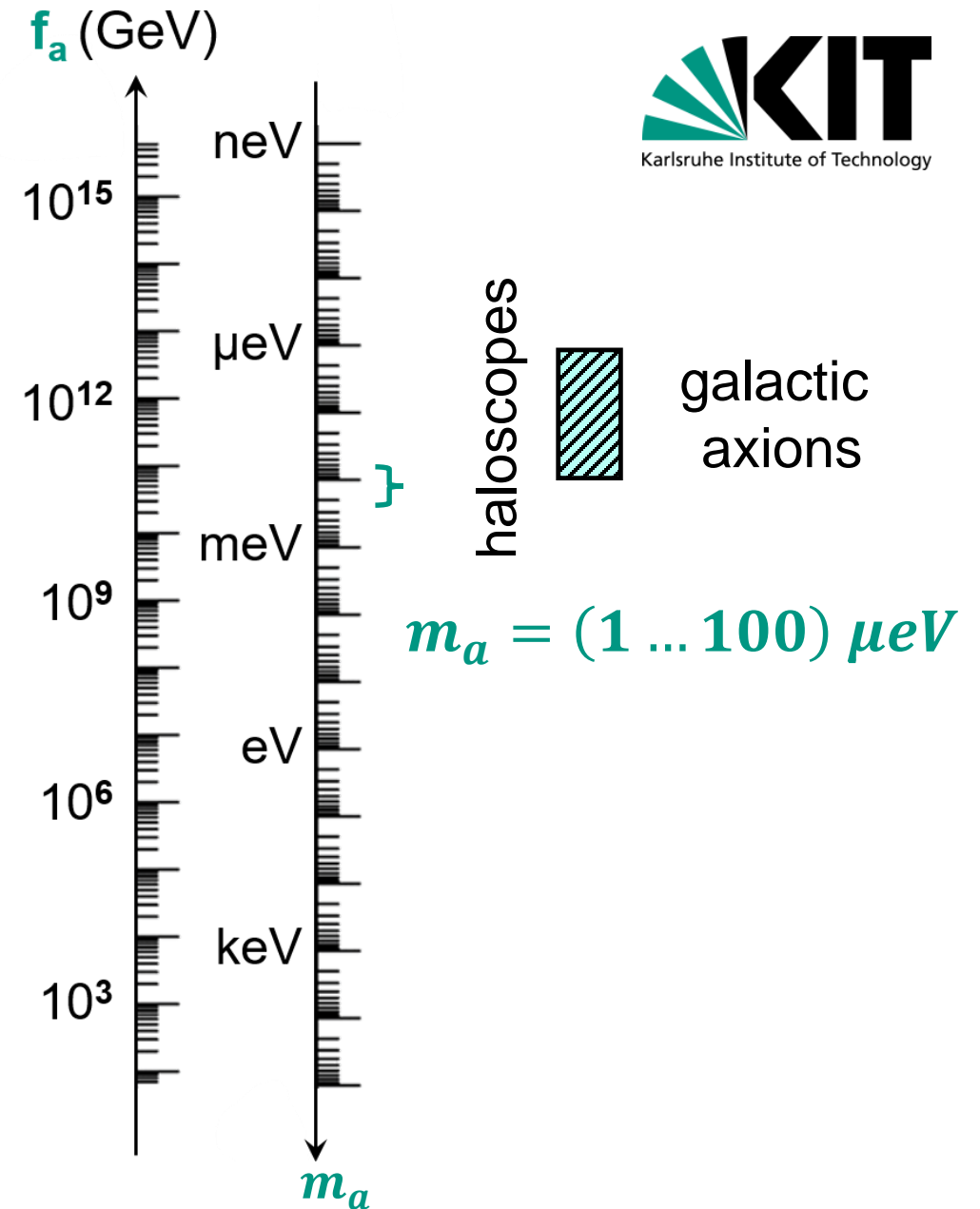
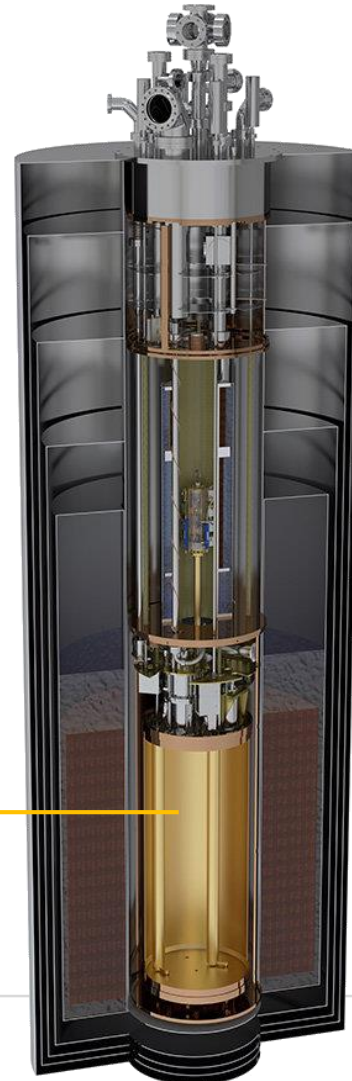


Axions: *MW*-cavity searches

■ Haloscopes: axions from the *DM* – halo?

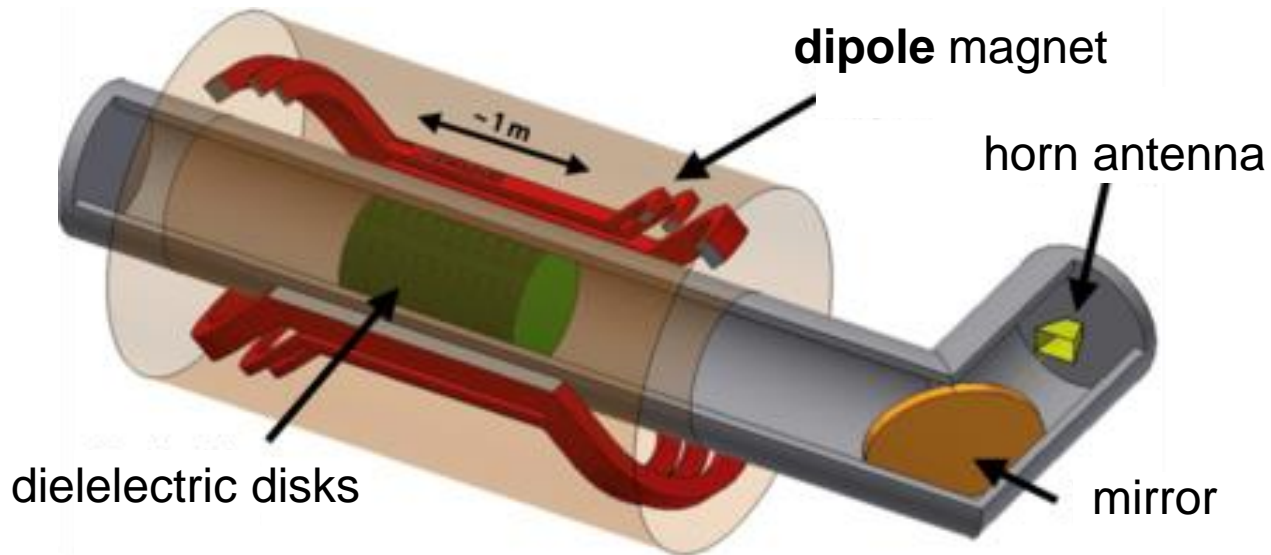


- let's look whether we can convert the galactic *DM* –axions into *EM* radiation in cavities

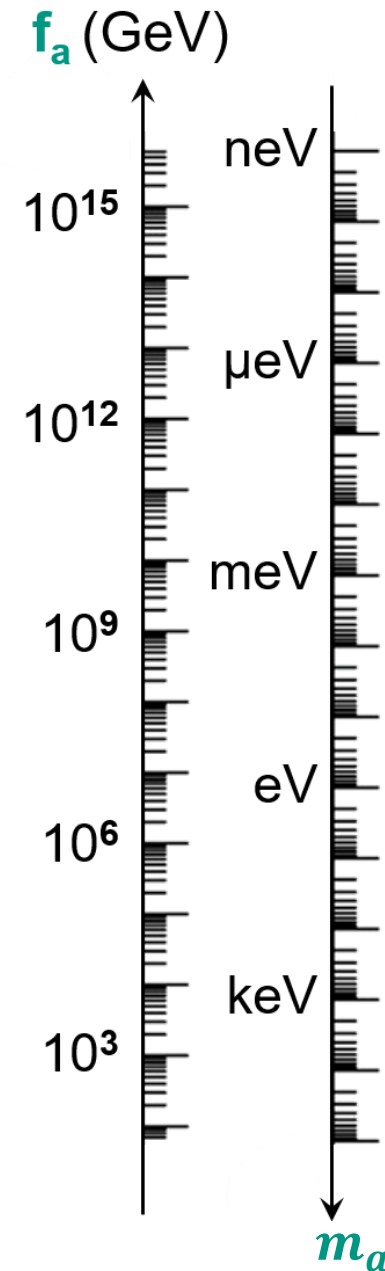


Axions: dielectric haloscopes

■ Haloscopes: axions from the DM – halo?



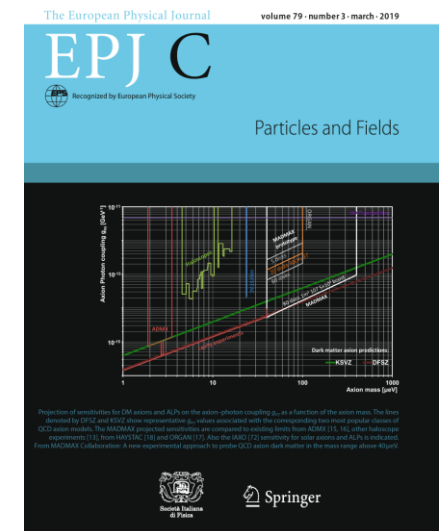
- let's look whether we can convert the galactic ***DM*** – axions via dielectric disks in a strong ***B*** – field



haloscopes

galactic
axions

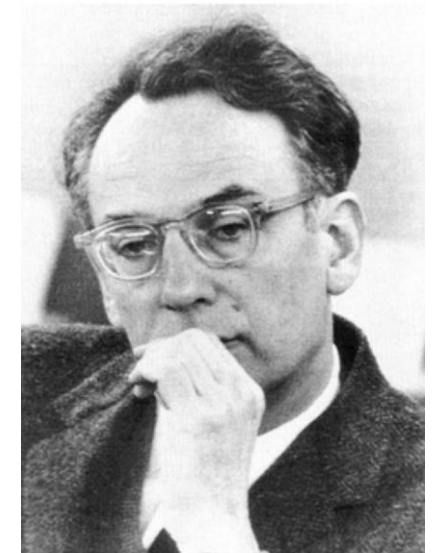
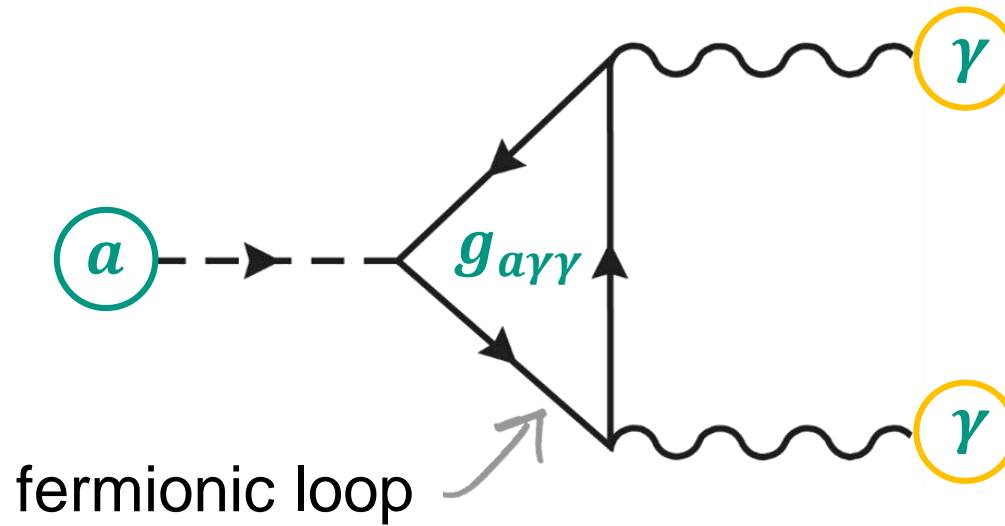
$$m_a = (40 \dots 400) \mu eV$$



Axions & their interactions: the Primakoff process

■ The fundamental Feynman loop diagram for interactions of axions

- axion a can couple to **two photons** via a **fermionic loop**: **Primakoff effect**
- coupling strength can be parameterized via the (a priori unknown) **axion-photon coupling constant** $g_{a\gamma\gamma}$

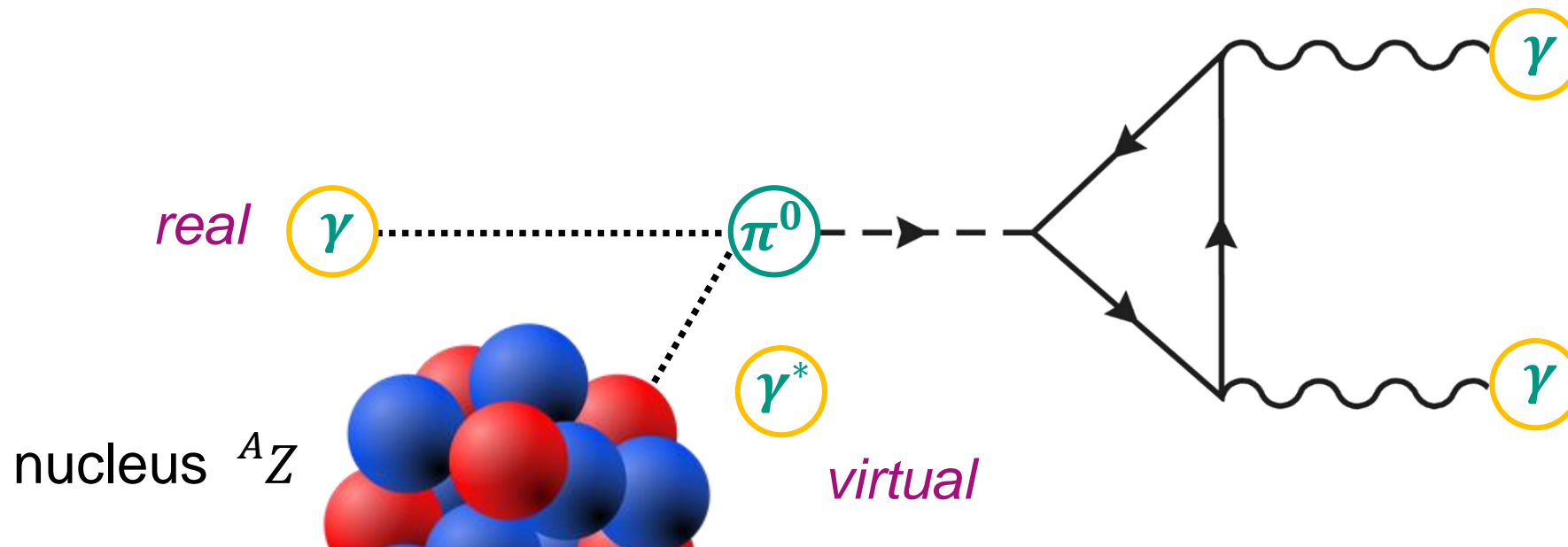


Henry Primakoff

Axions & their interactions: the Primakoff process

■ The fundamental Feynman diagram modelled **analog to decay** $\pi^0 \rightarrow \gamma\gamma$

- neutral pion π^0 generated & decay to **two photons**: (inverse) **Primakoff effect**
- **nuclear physics**: generation of the photo-nuclear resonance π^0 in the field of a nucleus via energetic gammas & subsequent π^0 decay to two photons



Henry Primakoff

Axions & their interactions: the coupling $g_{a\gamma\gamma}$

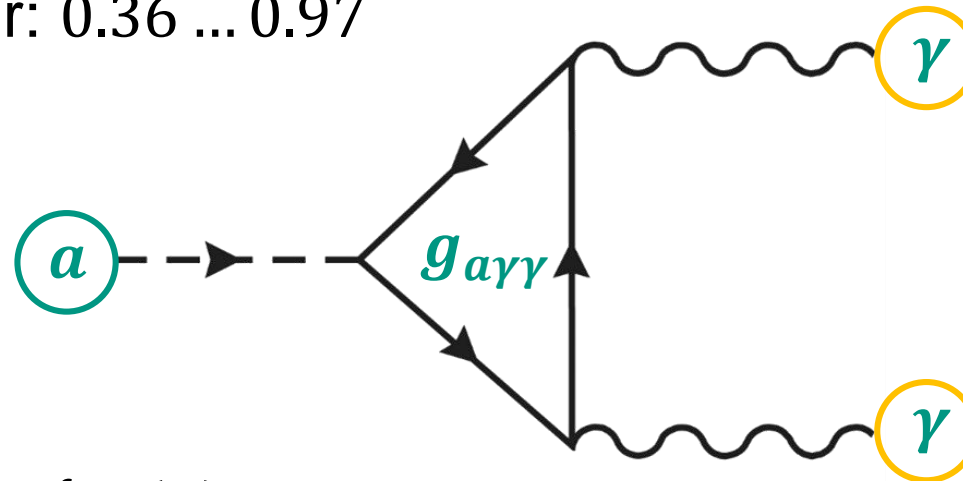
■ The axion coupling to matter is exceedingly weak – be warned!

- coupling constant $g_{a\gamma\gamma}$ is not known *a priori*, as it is related to the (unknown) very high energy scale f_a

α_s : coupling of strong interaction

g_γ : model-dependent *QCD* – parameter: 0.36 ... 0.97

$$g_{a\gamma\gamma} \sim \frac{\alpha_s}{\pi} \cdot \frac{1}{f_a} \cdot g_\gamma$$



f_a : energy scale of breaking of $U(1)_{PC}$

Axions & their interactions: the coupling $g_{a\gamma\gamma}$

■ The axion coupling to matter is exceedingly weak – be warned!

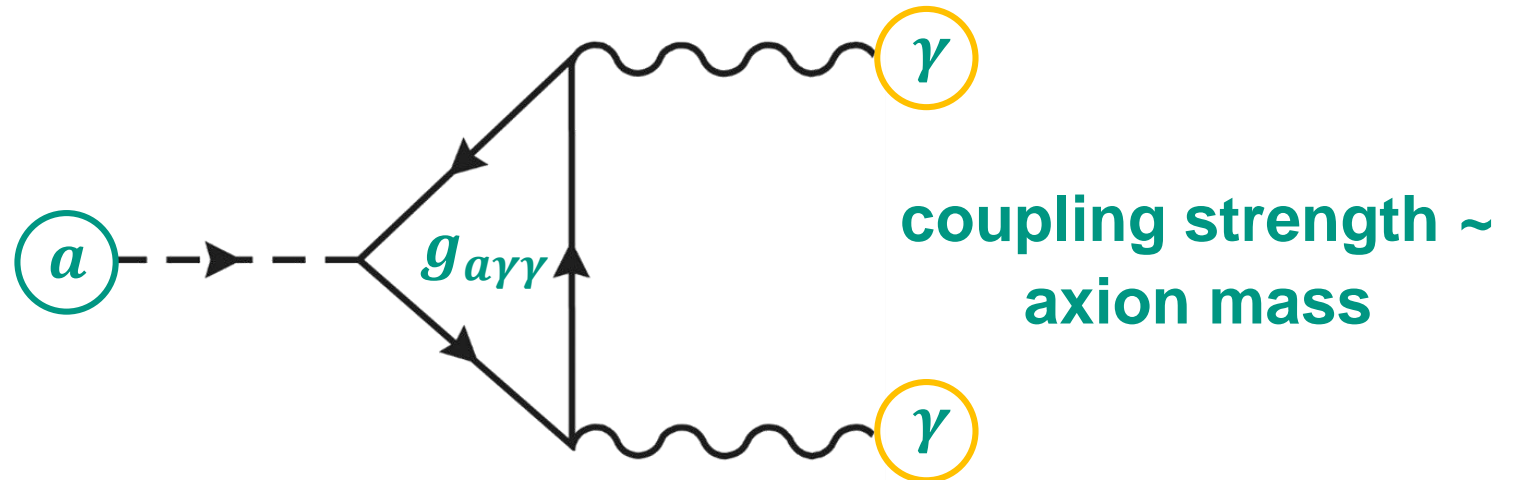
- coupling constant $g_{a\gamma\gamma}$ is not known *a priori*, as it is related to the (unknown) mass scale m_a

α_s : coupling of strong interaction

$$g_{a\gamma\gamma} \sim \frac{\alpha_s}{\pi} \cdot m_a$$

m_a : mass scale of axions

the smaller the axion mass,
the more difficult to detect it



coupling strength ~
axion mass

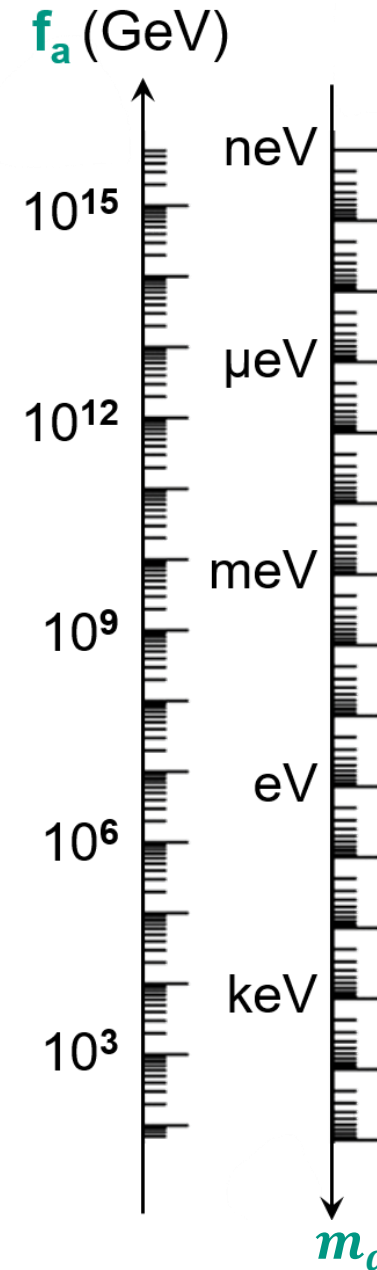
Axions & their interactions

■ The axion coupling to matter

- coupling constant $g_{a\gamma\gamma}$ has all the 'desired' properties of a **DM** – candidate
 - when the axion mass m_a **gets smaller**, we have **more axions** in the universe, but (non-gravity) **interaction rates drop**

$$g_{a\gamma\gamma} \sim \frac{\alpha_s}{\pi} \cdot m_a$$

m_a : mass scale of axions



↑
too much
↓
too little

Dark Matter

Axions & their interactions: *J.C. Maxwell, wake up!*

- The axion coupling to *EM* – fields: we have to **modify the Maxwell equations!**

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma} \mathbf{B} \cdot \nabla a$$

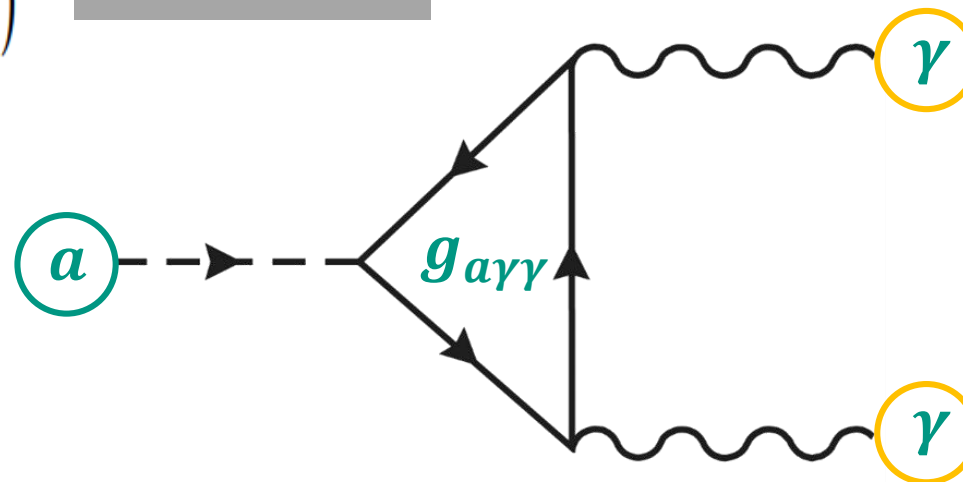
$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \times \mathbf{B} = \frac{\partial \mathbf{E}}{\partial t} + \mathbf{J} - g_{a\gamma\gamma} \left(\mathbf{E} \times \nabla a - \frac{\partial a}{\partial t} \mathbf{B} \right)$$

no changes here, great

can be used to reveal
the presence of axions



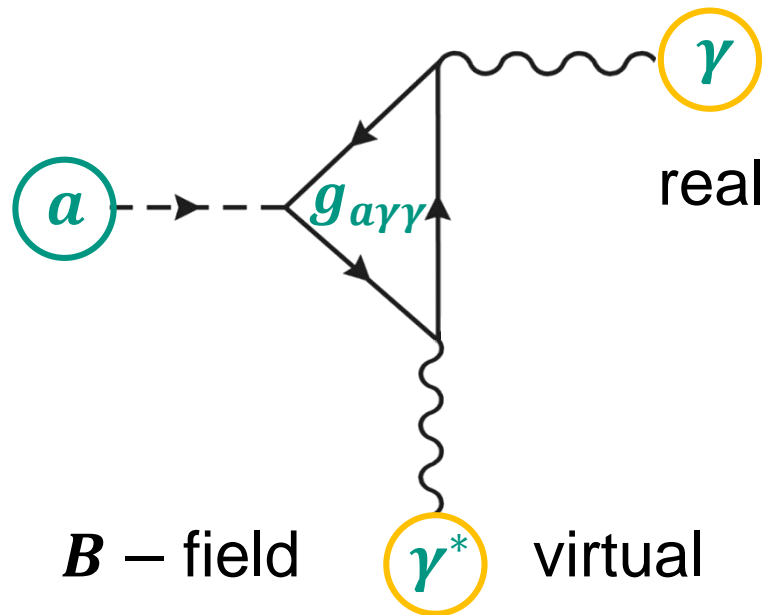
but ... **my**
equations...



Axion detection: making use of magnetic fields

■ A **coherent*** process (inverted Primakoff) to **convert axions in a B – field**

- a **very strong B – field** (in the lab: few T) is used to generate a **virtual photon γ^*** to initiate the conversion of an axion into a **real photon γ**



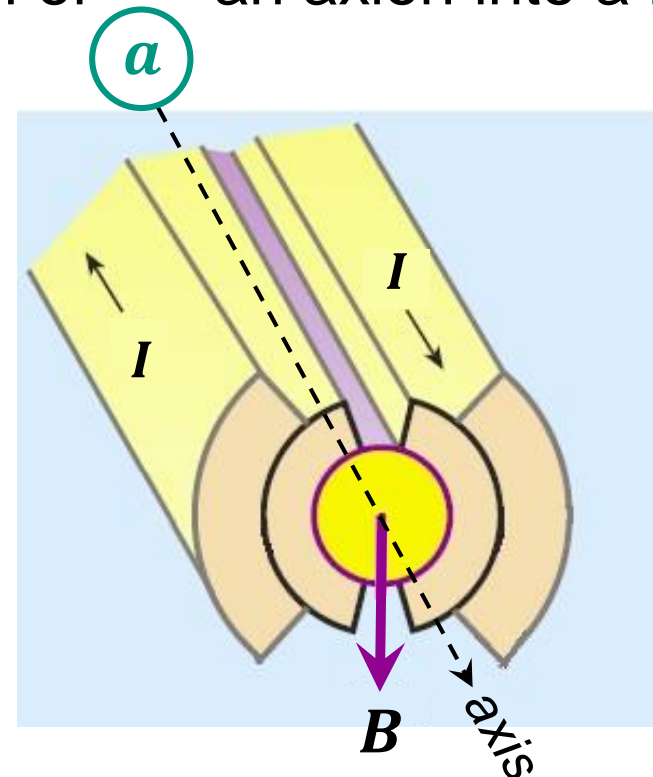
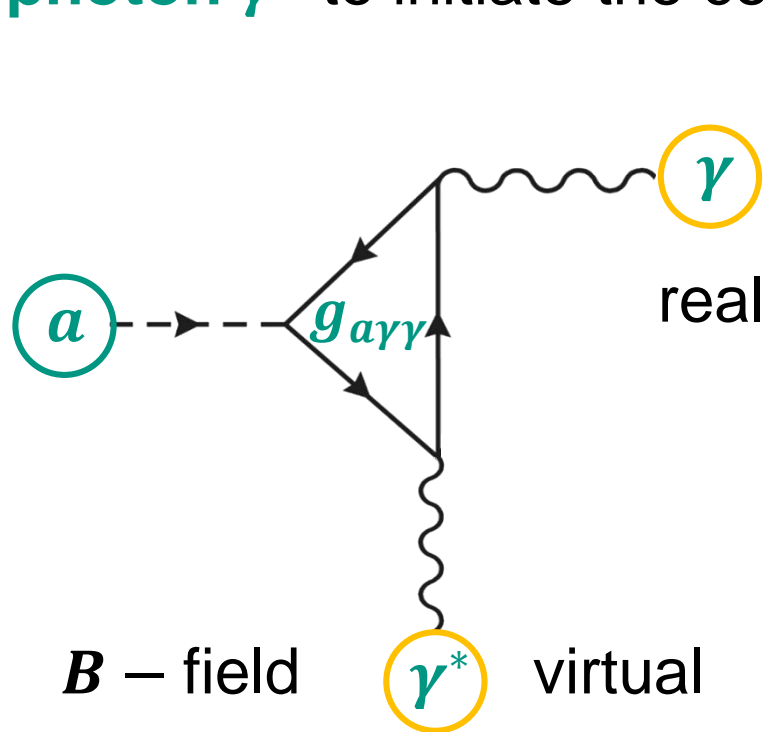
- there is a ‘mismatch’ of the spins of the axion (pseudoscalar, $S = 0$) and of the photon (vector, $S = 1$):

⇒ the external **B -field** has to be transversal, i.e. we need a typical **magnetic dipole field**

Axion detection: making use of magnetic fields

■ A coherent process (inverted Primakoff) to convert axions in a B – field

- a **very strong B – field** (in the lab*: few T) is used to generate a **virtual photon γ^*** to initiate the conversion of an axion into a **real photon γ**



dipole magnet

B is transversal
to axion flight path
which is travelling
along magnet axis
with its length L

Axion detection: making use of magnetic fields

■ A coherent process (inverted Primakoff) to **convert axions in a B – field**

- a **very strong B – field** (in the lab*: few T) is used to generate a **virtual photon γ^*** to initiate the conversion of an axion into a **real photon γ**

dipole magnets at LHC

