



Astroparticle physics I – Dark Matter

Winter term 23/24 Lecture 13 Dec. 20, 2023



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Recap of Lecture 12



Searches for $0\nu\beta\beta$ – decay and astrophysical evidences for *DM*

- 5 key parameters impact the sensitivity to half-life $t_{\frac{1}{2}}^{0\nu\beta\beta}$: $a, M, t, \Delta E, B$
- enrichment factor $a = 0 \dots 1$, exposure $M \cdot t$, energy resolution ΔE
- most important: extremely low background rate B at Q value
- current (*MAJORANA*, *GERDA*) & future (*LEGEND*) experiments: $\Rightarrow 10^{28} yr$
- *DM* evidences: velocity dispersion of clusters, galactic rotation curves
- local DM density: $\rho_{DM,local} = 0.3 \ GeV/cm^3 [1 WIMP(50 \ GeV) / coffee \ cup]$

4.2 Dark Matter: candidates

- A broad variety of candidates from ultra—light up to super—massive DM
- mass scale: from $10^{-21} ... 10^{25} eV$
- ❷ axions (strong CP problem)
- € light DM on sub GeV scale
- **Gev** ... TeV WIMPs: neutralinos
- primordial black holes (*MACHOs**)





Dark matter candidates & cosmology

Important cross-checks via impact of DM in early & present universe

- no particle in the *SM* can play the role of Dark Matter: \Rightarrow look beyond (*BSM*)
- stable over Hubble time $t_H = 13.8 \cdot 10^9 \ yr$ against decay: $\tau_{decay} \gg t_H$ or wrt. radiative emission (BH)
- current number density must reproduce the DM – density $\Omega_{DM} = 1 \ GeV \ m^{-3}$
- weak interactions only
 (Z⁰, h bosons,...), + gravity





Dark matter candidates & cosmology

Important cross-checks via impact of DM in early & present universe

- production in early universe: thermal (WIMPs) or non-thermal processes (axions)
- must be 'cold', i.e. moving non-relativistically
 - ⇒ 'bottom-up' formation of large-scale structures
- de-Broglie wavelength $\lambda_{deBroglie} < r_{dw \, gal}$ (radius of a dwarf galaxy, *few kpc*)
- reproduce observed <u>local</u>
 DM density (0.3 GeV cm⁻³)



Dark matter candidates: the case of neutrinos

- Massive neutrinos are part of the Dark Matter in the universe
- production in early universe: thermal processes via W^{\pm} , $Z^0 339 v's cm^{-3}$
- *v*´s are ´hot´, i.e. moving relativistically (*m_v* < 0.8 *eV*)
 ⇒ ´top−down´ formation of large−scale structures
- de-Broglie wavelength $\lambda_{deBroglie} > r_{dw \, gal}$ (radius of a dwarf galaxy, *few kpc*)





Dark matter candidates: the case of neutralinos



Weakly Interacting, Massive Particles: WIMPs or, specifically, neutralinos

- production in early universe: thermal processes via W^{\pm} , Z^0 bosons
- correct abundance if **weak interaction** *xsec*
- cosmologically **stable** due to new intrinsic quantum number (**R**_P)
- *CDM*: non-relativistic velocity distribution, allows bottom-up evolution of structures



Dark matter candidates: the case of axions



Weakly Interacting, Slim Particles: WISPs or, specifically, axions

- production in early universe: non-thermal processes via symmetry breaking
- correct abundance if mass
 & xsec within specific range
- cosmologically stable
 due to tiny mass (~μeV)
- *CDM*: non-relativistic velocity distribution, allows bottom-up evolution of structures





Dark matter candidates: heavy, cold DM

- Neutralinos & other WIMPs
- neutralino χ: prototype of a Weakly
 Interacting Massive Particle (WIMP)
- mass m = GeV ... TeV scale
 ⇒ determines its number density
- neutralinos are superpositions of 4 states: \Rightarrow mixing efffects reduce σ_{tot}
- electroweak χ cross section scale:

 $\sigma_{\chi,tot} = 10^{-12} \dots 10^{-6} \, pb$





11 Dec. 20, 2023 G. Drexlin – ATP-1 #13

Dark matter candidates: light, but cold DM

Axions & Axion-Like Particles (ALPs)

- axion a: prototype of a Weakly
 Interacting Slim Particle (WISP)
- mass *m* = *neV* ... *meV* scale
 ⇒ determines interaction rate
- axions 'solve' the strong CP problem of QCD
- interaction via 'Primakoff effect':
 - B field: conversion into/from $\gamma's$





Dark matter candidates: light, but cold DM



- axion a: prototype of a Weakly
 Interacting Slim Particle (WISP)
- a large parameter space to cover
- a message from *Richard Feynman*:

29.12.1959

There 's plenty of room at the bottom







Dark matter candidates: ultra-heavy DM

ultra-heavy particles: WIMPzilla

- *'WIMPzilla'*: prototype of an extremely massive particle
- mass $m = 10^{12} \dots 10^{12} \text{ GeV}$ scale \Rightarrow at GUT - scale (inflation!)
- a message from *Rock Kolb*:

Síze does matter





DM – related theories: *SU*per–*SY*mmetry (*SUSY*)

A new space-time symmetry between bosons fermions

- SUSY postulate: each SM particle has a heavy (TeV) SUSY superpartner
- SUSY & SM particles obey different
 spin statistics (fermions ⇔ bosons), as
 spin differs by Δs = ½
- *SUSY* operator *Q*:
 - $egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} boson
 ightarrow = |boson
 angle \end{aligned} \ egin{aligned} egin{aligne$

transforms bosons into fermions & v.v.



Dec. 20, 2023

15

- SUSY postulate: each SM particle has a heavy (TeV) SUSY superpartner
- SUSY & SM particles: identical properties, except mass & spin statistics

DM – related theories: SUSY name conventions

SUSY postulates heavy superpartners with $s = \frac{1}{2}$ and s = 0

- SUSY bosonic superpartners sfermion (\tilde{q} : squark, $\tilde{\ell}$: slepton)
- SUSY fermionic superpartners ... – *inos* ($\tilde{\gamma}$: *photino*, \tilde{g} : *gluino*, \tilde{H} : *Higgsino*,...)

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DM – related theories: SUSY origins at KIT



1973: Wess & Zumino postulate the first supersymmetric quantum theory

- Wess–Zumino model Julius Wess (KIT)

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16

Bruno Zumino (CERN)

director of the *KIT* institute for Theoretical Physics from **1968 – 1990**



Julius Wess (1934 – 2007)

- KCETA regularly awards the Julius Wess prize*

G. Drexlin – ATP-1 #13 * KIT - KCETA - Julius Wess Award

Nuclear Physics B70 (1974) 39-50. North-Holland Publishing Company

SUPERGAUGE TRANSFORMATIONS IN FOUR DIMENSIONS

J. WESS Karlsruhe University

B. ZUMINO CERN, Geneva

Received 5 October 1973

Abstract: Supergauge transformations are defined in four space-time dimensions. Their commutators are shown to generate γ_5 transformations and conformal transformations. Various kinds of multiplets are described and examples of their combinations to new representations are given. The relevance of supergauge transformations for Lagrangian field theory is explained. Finally, the abstract group theoretic structure is discussed.



SUSY: a spontaneously broken symmetry



Quantum vacuum not invariant under SUSY – transformations

- result:

masses of SM - particles & SUSY - particles not identical

- mass-relation: $m(SM) \ll m(SUSY) = 0.1 \dots 10 TeV$
- scale of SUSY symmetry breaking: expected at energies $E_{SUSY} = 0.1 \dots 10 TeV$
- **origin** of *SUSY* symmetry breaking: unknown, why the scale $E_{SUSY} < 10 TeV$? further hierarchy problem: why $E_{SUSY} \ll E_{GUT}$?



EXCURSION: what if ... SUSY was NOT broken?



- result:

masses of SM - particles & SUSY - particles are identical

Pauli exclusion principle not valid for bosonic superpartner selectron (*ẽ*) of electron (*e*): no extended Bohr orbitals possible...







Indirect hints for SUSY comes from the running of coupling constants α_i

- *GUT* (Grand Unified Theory) – based scenarios expect a unfication of forces at large scale $\Lambda_{GUT} \sim 10^{16} \text{ GeV}$ (S. Glashow, H. Georgi, 1974)





Indirect hints for SUSY comes from the running of coupling constants α_i

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SM: no gauge unification observed in running of coupling constants α_i

- *Wim de Boer (ETP) et al.* perform a **fit** to couplings: ´in the *SM* the couplings do NOT meet...!´ EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

CERN-PPE / 91-44 22 March 1991

ІЕКР-КА / 91-01

Comparison of Grand Unified Theories with electroweak and strong Coupling Constants measured at LEP





SM: no gauge unification observed in running of coupling constants α_i

Wim: 'we find: only in a SUSY – scenario all couplings meet at one energy scale!'



- Julius: ´my SUSY – scenario fits!´

J. Wess (KIT) & B. Zumino



U. Amaldi

SUSY and experimental verification at the LHC



LHC with cms – energy of $\sqrt{s} = 13.6 TeV$ allows dedicated SUSY – searches

- search for SUSY – superpartners at the TeV – scale in pp – collisions





Building a viable DM – candidate from SUSY – particles: a how-to approach

- search for SUSY – superpartners at the TeV – scale in pp – collisions



SUSY: a closer look at the superpartner properties

- Building a viable DM candidate from SUSY particles: a how-to approach
- SUSY superpartners: identical properties, except mass m & instrinsic spin s
- *squarks*: identical strong interaction as quarks (3 colours)
- *sleptons*: identical electromagnetic interaction as leptons e, μ, τ
- sneutrinos, neutral gauginos:
 mixing effects as in case of v´s
 ⇒ mass states for propagation
 ⇒ flavour states for interaction



SUSY: MSSM, the minimum extension of the SM



Building a viable DM – candidate from SUSY – particles: a how-to approach

- MSSM: Minimal Supersymmetric Standard Model: 105 new parameters particle masses, mixing angles, CP – phases, life-times,...
- minimal extension of new particles
 & interactions
- motivation: stabilisation of the light Higgs boson at 125 GeV against quantum—loop—corrections
- SUSY masses of MSSM expected in range M = 0.1 ... 1 TeV but: no signal at LHC so far...



SUSY: important properties with view to DM



R – parity: a key property of SUSY for DM & the stability of the proton p

- introduction of a new, multiplicative quantum number for all particles

-parity
$$R_P$$
: $R_P = (-1)^{3 \cdot B + L + 2S}$ or $R_P = (-1)^{3 \cdot (B-L) + 2S}$

B: baryon number L: lepton number S: spin

- SM particles: $R_P = +1$ (even) SUSY particles: $R_P = -1$ (odd)
- resulting superpartner properties:

a) production via SM - particles: only SUSY - pairs can be emitted

b) SUSY – superpartners only decay into superpartners (not SM – particles)

R

SUSY: important properties with view to DM

R – parity: a key property of SUSY for DM & the stability of the proton p





SUSY and the constrained MSSM (cMSSM)



cMSSM: the most 'economic' SUSY – model with only 5 new parameters

- all superpartner masses are assumed to be identical at the GUT scale



cMSSM: building of a viable *DM* – candidate

- A weakly interacting massive, mixed DM particle (which is also stable)
- neutral particles with weak interactions only, as no exotic isotopes were observed

S

 V_{e}

squarks

- \rightarrow **no** squarks (charge, colour)
- \rightarrow **no** charged sleptons (charge)
- \rightarrow **no** *gluinos* (colour)
- \rightarrow **no** *Winos* (charge)
- remaining **DM** candidates:
 - \rightarrow gauginos: photino $\tilde{\gamma}$, Zino \tilde{Z} Higgsino \tilde{H}
 - \rightarrow sneutrinos: $\tilde{\nu}_{e}, \tilde{\nu}_{\mu}, \tilde{\nu}_{\tau}$

Ζ

 V_{τ}

τ

sleptons

Higgsino

cMSSM: a closer look at sneutrinos

- Sneutrinos as superpartners of neutrinos: can they be a DM candidate?
- neutral particles with weak interactions only M
- heavy, scalar particles at the TeV mass scale (CDM) \checkmark
- but: weak interaction rates are **identical** to the ones of $v's \boxtimes$ \Rightarrow very early universe: **too large annihilation rate**!
 - \Rightarrow present density in the universe is much too small ($\Omega_{DM} \ll 0.27$)
- lesson: weak interaction rate of a successful DM candidate must be significantly smaller than the one of neutrinos!





cMSSM: a closer look at gauginos & Higgsinos

Neutral fermionic superpartners: can they be a DM – candidate?

- we have 4 interaction eigenstates : 1 photino $\tilde{\gamma}$ 1 Zino \tilde{Z} 2 Higgsinos \tilde{H}
- remember **neutrino oscillations**: strong mixing effects due to identical quantum numbers flavour states $v_e, v_\mu, v_\tau \Leftrightarrow$ mass states m_1, m_2, m_3
- we now mix the 4 flavour states photino $\tilde{\gamma}$, Zino \tilde{Z} and the 2 Higgsinos \tilde{H} to 4 mass eigenstates: neutralinos
- *WIMP* miracle: weak interaction rate of a mixed state $(\tilde{\gamma}, \tilde{Z}, 2 \tilde{H})$ possesses just the required (annihilation) interaction rate for $\Omega_{DM} \approx 0.27$ (!!!!)



Higgsi

cMSSM: an even closer look at Higgsinos

How many superpartners for the Higgs boson of the SM?

- we have 5 physical *Higgsino* states in the *MSSM*: \tilde{h} , \tilde{H}^0 , \tilde{A} , \tilde{H}^{\pm}
- 1 rather light (SM like) state : \tilde{h} , plus others (charged \tilde{H}^{\pm} do not mix, as well as pseudoscalar \tilde{A})
- in *SUSY* we have to consider 2 Higgsinos \tilde{H}^0 : for u – type particles \tilde{H}^0_u , for d – type particles \tilde{H}^0_d
- for mixing to mass states we thus have 4 states: *photino* $\tilde{\gamma}$ *Zino* \tilde{Z} 2 *Higgsinos* $\tilde{H}^0_u \tilde{H}^0_d$





SUPE

Exp. Particle Physics - ETP

cMSSM: comparing neutralinos & gauginos



Due to mixing: we have flavour eigenstates & mass eigenstates

- we have 4 flavour states:

gauginos photino $\tilde{\gamma}$ Zino \tilde{Z} 2 Higgsinos $\tilde{H}_{u}^{0} \tilde{H}_{d}^{0}$ these states do interact, but have no well-defined masses & thus do not propagate

- we have 4 mass states: *neutralinos* lightest ... heaviest $\tilde{\chi}_1^0 \tilde{\chi}_2^0 \tilde{\chi}_3^0 \tilde{\chi}_4^0$ these states **propagate in space** with well–defined masses, but have to mix to interact



And finally: the neutralino as DM candidate



- Stabilising the lightest neutralino $\tilde{\chi}_1^0$ via its intrinsic R parity R_P as DM
 - the *LSP* (*L*ightest *S*upersymmetric *P*article) is expected to be stable over cosmological time scales due to its intrinsic $R_P = -1$
 - accordingly, if the lightest *neutralino* $\tilde{\chi}_1^0$ is the *LSP* of *SUSY*, it is an excellent DM candidate at the TeV scale

- the (unknown) flavour ratios c_i determine interaction rates of the $\tilde{\chi}_1^0$

the lightest neutralino $\tilde{\chi}_1^0$ as WIMP - DM

Properties of *neutralinos* & searches for SUSY – WIMPs

- SUSY expects *neutralinos* to be Majorana-type* particles
- it can **annihilate** with itself (no anti-neutralinos)
- mass on TeV scale, very weakly interacting
- searches at LHC, galactic DM halo, direct DM detectors







*see lecture #11

Putting SUSY on the experimental testbed

- Feynman diagrams for WIMP searches at LHC, galactic halo & DM – detectors
- before we start to discuss *DM* searches, we quote *Richard Feynman* himself



It doesn't matter how beautiful your theory is, it doesn't matter how smart you are. If it doesn't agree with experiment, it's wrong.

— Richard P. Feynman —

AZQUOTES







Geprüfte SUSY

Putting SUSY on the experimental testbed

Feynman diagrams for WIMP interactions

- flavour components of the lightest neutralino $\tilde{\chi}_1^0$ will interact via **two** exchange bosons
 - a) neutral vector boson Z^0 = **spin**-dependent process
 - b) neutral Higgs bosons H, h = **spin**–**independent** process (scalar interaction)
- relative coupling strengths unknown, but very small in both cases



neutralinos

matter particle



Putting SUSY on the LHC testbed at CERN



Feynman diagram for WIMP production from partons inside a proton

direct production of neutralinos at a high–luminosity collider at the *TeV* – scale (chapter 4.3)





Putting SUSY on the testbed at the galactic halo



Feynman diagram for WIMP annihilation at the center of the galaxy

 - indirect searches for the annihilation reactions of *neutralinos* at the inner part of the galactic halo (chapter 4.4)





Putting SUSY on the testbed at a DM detector

Karlsruhe Institute of Technolo

Feynman diagram for *WIMP* **scattering in an underground** *DM* **– detector**

 direct searches for elastic scattering processes of *neutralinos* at large *DM* detectors (chapter 4.5)





4.3 WIMP search at the LHC



Direct production of WIMPs in pp – collisions at $\sqrt{s} = 13.6 TeV$



RCAP: *LHC* beam parameters



Search for rare SUSY – events is boosted by high collider luminosity L

- *LHC*: a huge step forward in increasing the luminosity of particle collisions – design value

$$L = 10^{34} \ cm^{-2} s^{-1}$$

#**p** /

bunch

transversal

beam size

- calculating the beam **luminosity** *L*:



bunches

 $\boldsymbol{L} = \boldsymbol{f} \cdot \boldsymbol{n} \cdot \frac{N^2}{4\pi \cdot \sigma_h^2}$

frequency



Transversal view of inner tracker, *ECAL*, *HCAL*, muon chambers



Outlook: hunting for signatures of *SUSY*



Signatures of *neutralinos*: missing energy / transversal momentum

