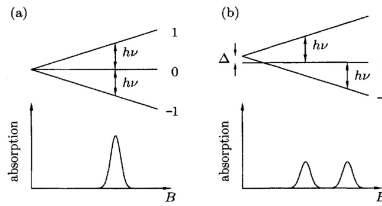


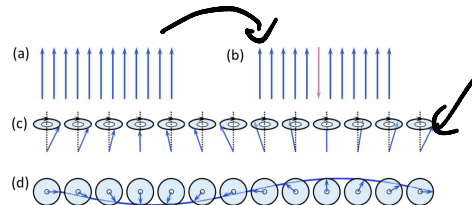
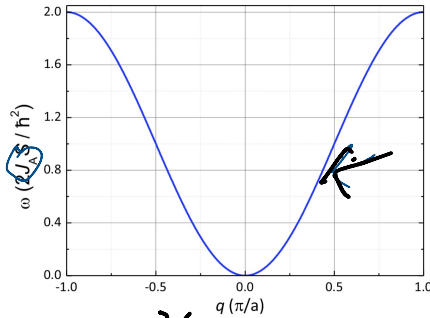
Lecture 28

Review

ESR:



Spin waves:



Bloch $T^{3/2}$ law

$$\frac{\Delta M}{M_s(T=0)} \propto \left(\frac{k_B T}{\lambda_s} \right)^{3/2} \quad \text{Bloch } T^{3/2} \text{ law}$$

• Describes the LT-dependence of a ferromagnet well

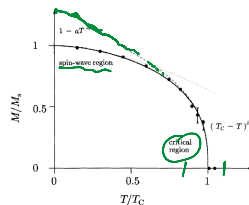
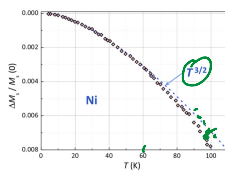


Fig. 6.15 The spontaneous magnetization in a ferromagnet. At low temperatures this can be fitted using the spin-wave model and follows the Bloch $T^{3/2}$ law. Near the critical temperature, the magnetization is proportional to $(T - T_c)^{\beta}$ where β is a critical exponent. Neither behaviour fits the real data across the whole temperature range. The data are for an organic ferromagnet which has $T_c = 0.67$ K for which $\beta = 0.36$, appropriate for the three-dimensional Heisenberg model.

Elastic neutron scattering

- neutron is a spin-1/2 particle, no charge
- non-zero magnetic moment. !
- produced in great quantities by fission reactions inside the fuel elements of nuclear reactors.
- The beam of neutrons which emerges from a reactor has a spectrum of energies determined by the temperature T of the moderator

→ slows down your neutrons (H_2O)

$$n(v) \propto v^3 \exp\left(-\frac{1}{2} m_n v^2\right)$$

The maximum of this distribution is at

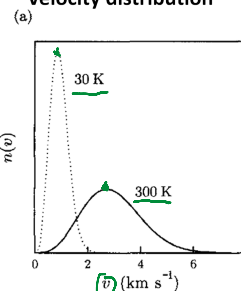
$$v = \sqrt{\frac{3k_B T}{m_n}}$$

The de Broglie wavelength λ of a neutron with velocity v is

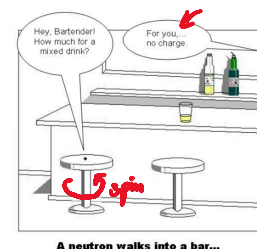
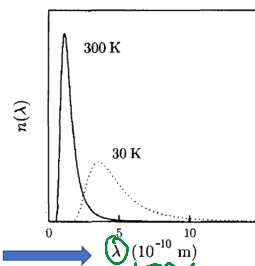
$$\lambda = \frac{h}{m_n v}$$

On the order of atomic lattices

Velocity distribution



wavelength distribution



A neutron walks into a bar...

Elastic neutron scattering

Neutrons scatter:

1. with nucleus via the strong nuclear force
2. NOT with electron clouds (no charge)
3. by variations in magnetic field within a crystal via the electromagnetic interaction

→ neutron couples to the magnetic moment of the electrons

1. nucleus via the strong nuclear force

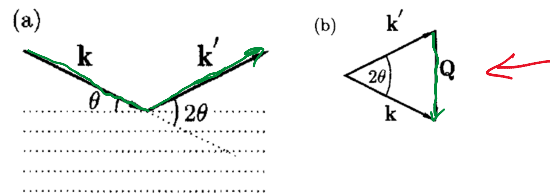
- incident neutron wave produces a spherically symmetric elastically scattered wave
- elastically scattered neutrons can produce strong Bragg reflections

Setups: • reactor (e)

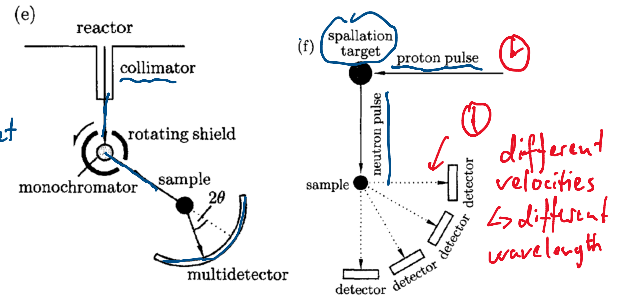
spallation source pulse of neutrons is produced by spallation (f) from a target. proton (high energy) → spallation target
 Aufspaltung Determine neutron energy by time-of-flight measurements

2. Contrast to X-ray and electron scattering:

- Interaction with the nucleus, not the electron cloud
- Element-sensitive, isotope-sensitive
- highly penetrating probe
- does not damage bio-samples



Bragg reflections when scattering vector $\vec{Q}$ = reciprocal lattice vector $\vec{G}$



Elastic neutron scattering

3. But Neutron is also magnetic: magnetic scattering.

→ spin-up and spin-down electronic moments 'look' different

Example: magnetic structure of the antiferromagnet MnO.

$T_N = 116 \text{ K}$

Amplitude of the magnetic Bragg peaks can be used as a measure of the strength of the magnetic order, and hence the magnetic order can be followed as a function of temperature.

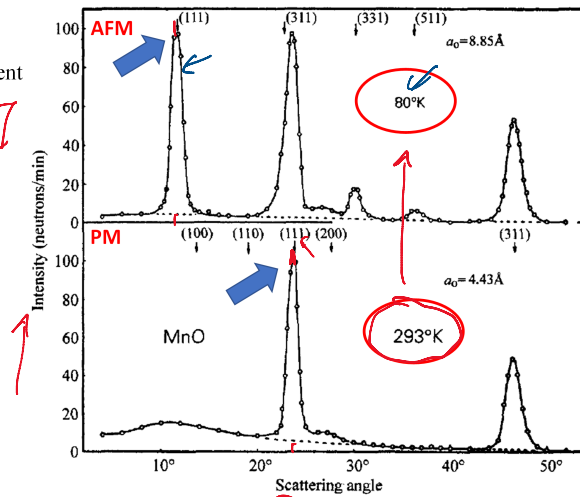
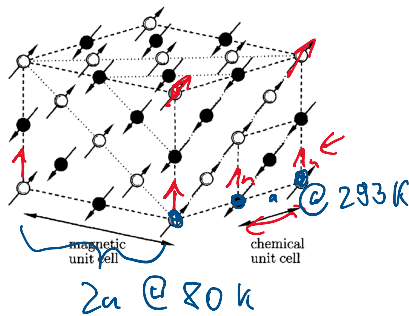


Fig. 5.19 Neutron diffraction patterns for MnO below and above T_N . After C. G. Shull, W. A. Strauser and E. O. Wollan, *Phys. Rev.*, **83**, 333 (1951).

Inelastic neutron scattering

The magnitude of the incident neutron wave vector k is now no longer equal to the magnitude of the scattered neutron wave vector k' .

$$E = \frac{\hbar^2 k^2}{2m_n} \quad E' = \frac{\hbar^2 k'^2}{2m_n}$$

Conservation of energy and momentum implies that

$$\underline{E} = \underline{E'} + \hbar\omega \quad \text{phonon [boring]}$$

$$\underline{k} = \underline{k'} + \underline{q} + \underline{G}, \quad \text{spin waves (not boring)}$$

- measurement of k , k' , E and E' allows a determination of ω and q .

- Neutrons have energies similar to the energies of atomic and electronic processes, i.e. in the meV to eV range

- magnon energies are typically in the range 1-10 meV

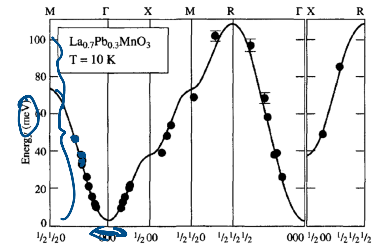
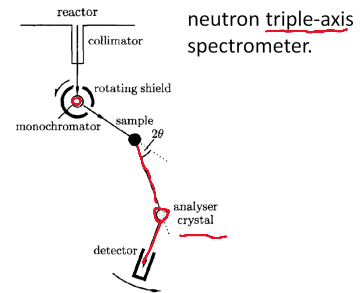
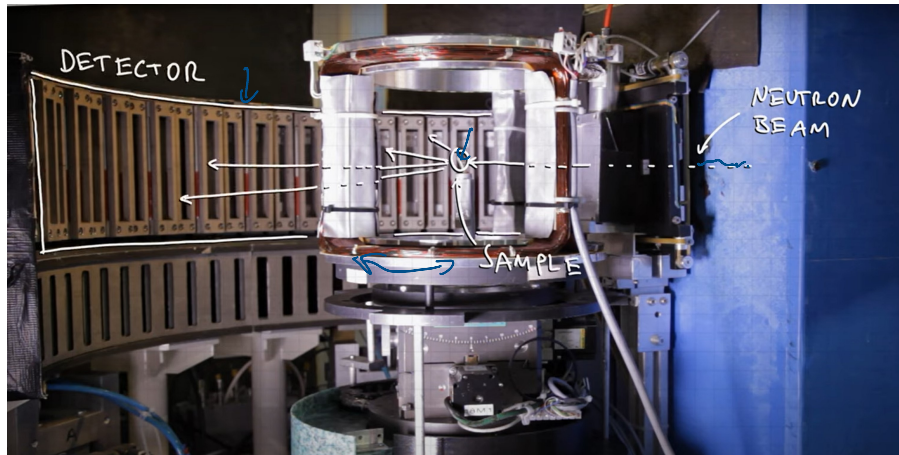
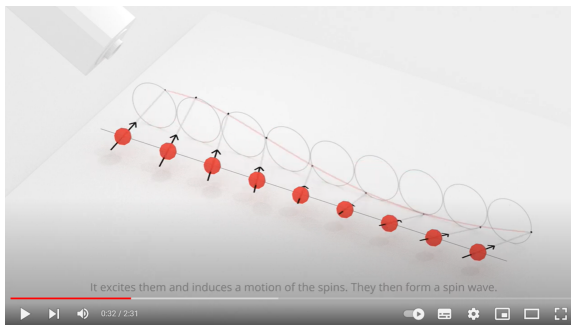


Fig. 6.18 Spin wave dispersion in the ferromagnetic oxide $\text{La}_{0.7}\text{Pb}_{0.3}\text{MnO}_3$ measured at 10 K by inelastic neutron scattering. The horizontal axis corresponds to the magnon wave vector. After Perring et al. 1996.

Jülich Centre for Neutron Science



Quantum Mechanics and Neutron Scattering 2 / 2



Neutron Inelastic Scattering

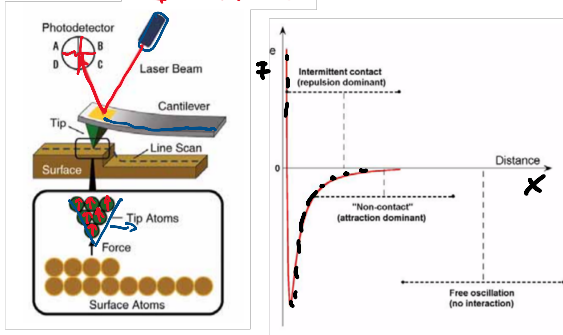
← CNRS

Scanning Probe Methods

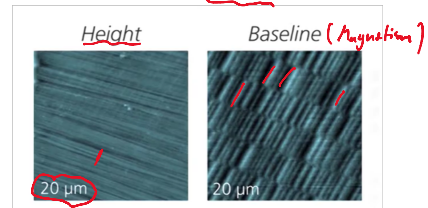
Magnetic Force Microscopy

- Atomic Force Microscope: Probes the topography (height) of a surface using the force interaction with a probe tip
- Using a magnetic tip, magnetic signals can also be detected, due to an additional magnetic force

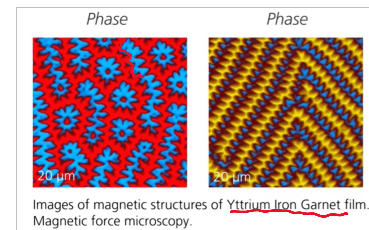
$$\vec{F} = \mu_0 (\vec{m} \cdot \nabla) \vec{H}$$



Topography and magnetic structure of a hard disc



Domain structure
Yttrium Iron Garnet (YIG) film



Scanning Probe Methods

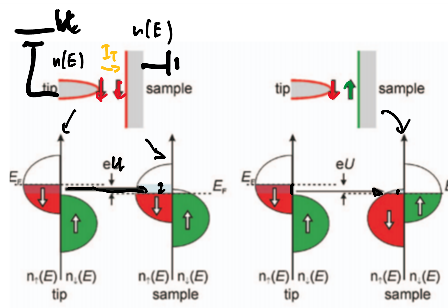
Spin-polarized scanning tunneling microscopy

Spin-dependent conductance of a ferromagnet-tunnelbarrier-ferromagnet interface

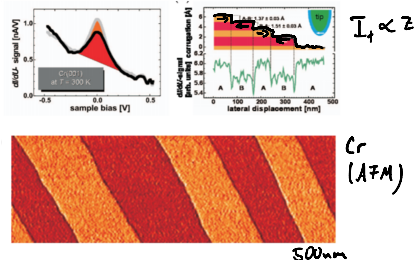
$$G_{\uparrow\uparrow} = G_{\text{fbt}}(1 + P_{\text{fb}}P_{\text{fb}}),$$

$$G_{\uparrow\downarrow} = G_{\text{fbt}}(1 - P_{\text{fb}}P_{\text{fb}}),$$

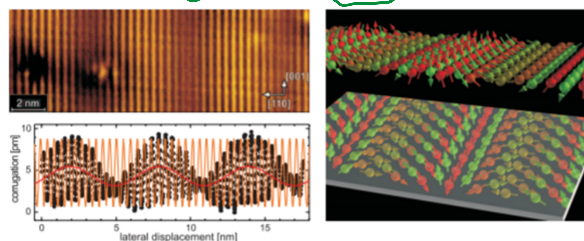
$$\frac{G_{\uparrow\uparrow} - G_{\uparrow\downarrow}}{G_{\uparrow\uparrow} + G_{\uparrow\downarrow}} = P_{\text{fb}}P_{\text{fb}} = P_{\text{fbt}}$$



Fe-coated W tip above differently magnetized terraces of an antiferromagnetic CrO₀₁ surface



Spin spiral state: Mn grown on a W(110) substrate DM

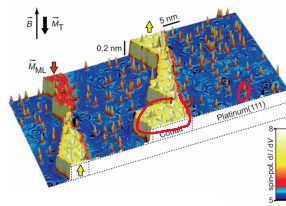


Roland Wiesendanger: Spin mapping at the nanoscale and atomic scale, Rev. Mod. Phys. 81 (2009)

Spin-polarized scanning tunneling microscopy

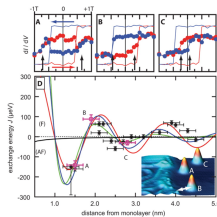
Revealing Magnetic Interactions from Single-Atom Magnetization Curves

Focko Meier,* Lihui Zhou, Jens Wiebe,† Roland Wiesendanger



RKky

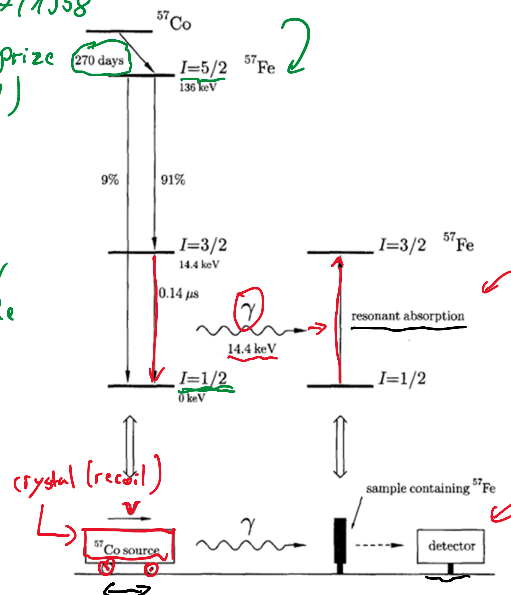
SCIENCE VOL 320 4 APRIL 2008



Mößbauer Spectroscopy

Rudolf Mößner 1957/1958

- Also magnetic resonance technique, but a little bit different
- Recoil-free absorption of gamma rays emitted by one nucleus that is absorbed by a sample containing the same isotope
- Ingredients: a source of ^{57}Co $\rightarrow$ ^{57}Fe ($I=5/2$)
 $\rightarrow$ decays to excited ^{57}Fe ($I=3/2$)
 $\rightarrow$ decays to ^{57}Fe ($I=1/2$)
- Emits a 14.4 keV gamma ray ($f = 3.5 \times 10^{18} \text{ Hz}$)
- To sweep frequency the Doppler effect is used ($v = 1 \text{ mm/s}$ corresponds to 12 MHz)
- Use ^{57}Fe in the sample as a resonant absorber
- Other elements are also possible, but not all
 $(^{119}\text{Sn}, ^{127}\text{I} \dots)$

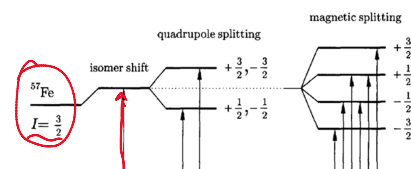


H	Element, bei dem der Mößbauer- effekt beobachtet wurde																He					
Li	Be															B	C	N	O	F	Ne	
Na	Mg															Al	Si	P	S	Cl	Ar	
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr					
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe					
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn					
Fr	Ra	Ac																				
			Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu						
			Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lw						

Mößbauer Spectroscopy

What can we measure with this?

1. Isomer shift (Comparable to Fermi contact basically)
→ shift of the resonant absorption due to differences

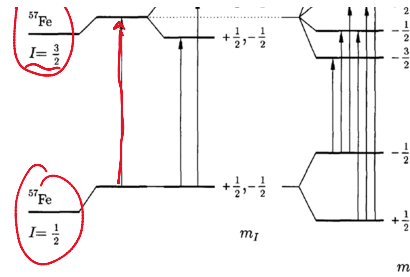


What can we measure with this?

1. **Isomer shift** (Comparable to Fermi contact basically)
→ shift of the resonant absorption due to differences in charge and Coulomb interaction (Oxidation state, valency, electron shielding)

2. **Quadrupole splitting**

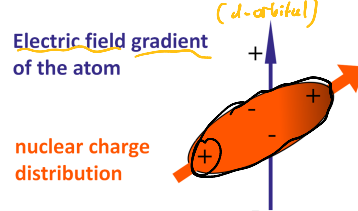
$$H_{NQI} = P \cdot I_z^2$$



Coupling of the nuclear quadrupole moment to the charge gradient (e.g. d-orbitals)
(Oxidation State, Spin state, site symmetry and arrangement of ligands)

3. "Local" magnetic field
 - Exchange interaction
 - Hyperfine interaction

Nuclear quadrupole interaction



Mössbauer Spectroscopy

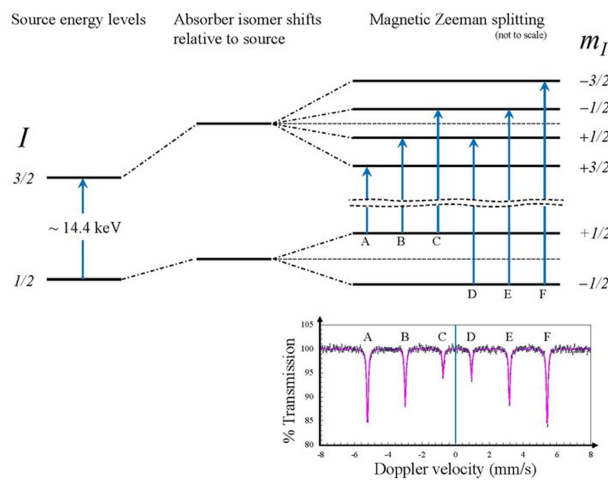


Fig. 4: Mossbauer spectrum and diagram illustrating magnetic Zeeman splitting in ^{57}Fe .

Mössbauer Spectroscopy

