

# Introduction to Cosmology

Winter term 22/23

Lecture 1

Oct. 25, 2022



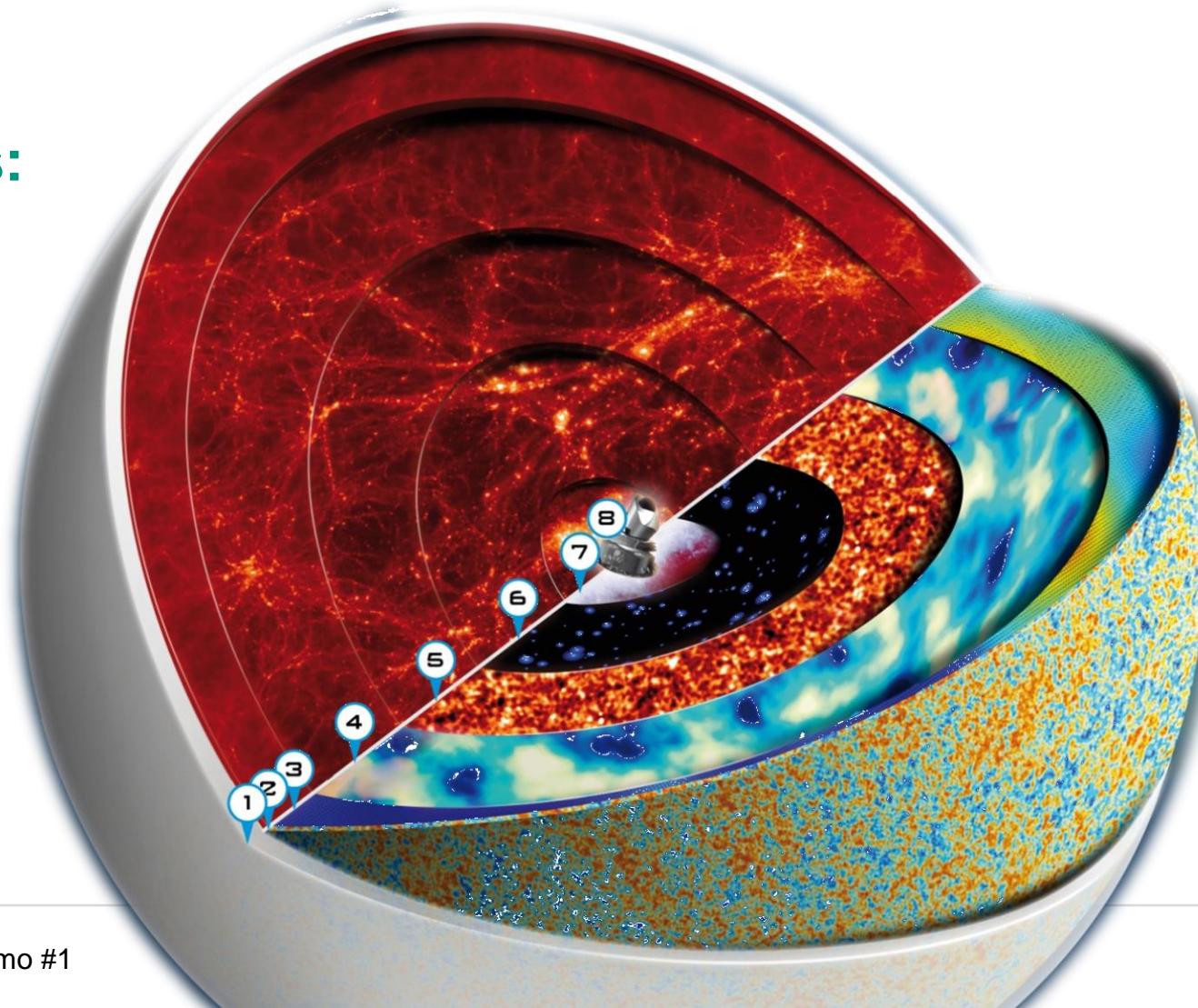
Evolution & Structure of the  
Universe from the Big Bang  
up to now

# Cosmology – Definition

## ■ Evolution & Structure of the Universe from the Big Bang to now

### important stopovers:

- 1 – Big Bang
- 2 – CMB (3K)
- 3 – reionisation
- 4 – dark ages
- 5 – first stars
- 6 – first galaxies
- 7 – Milky Way
- 8 – today



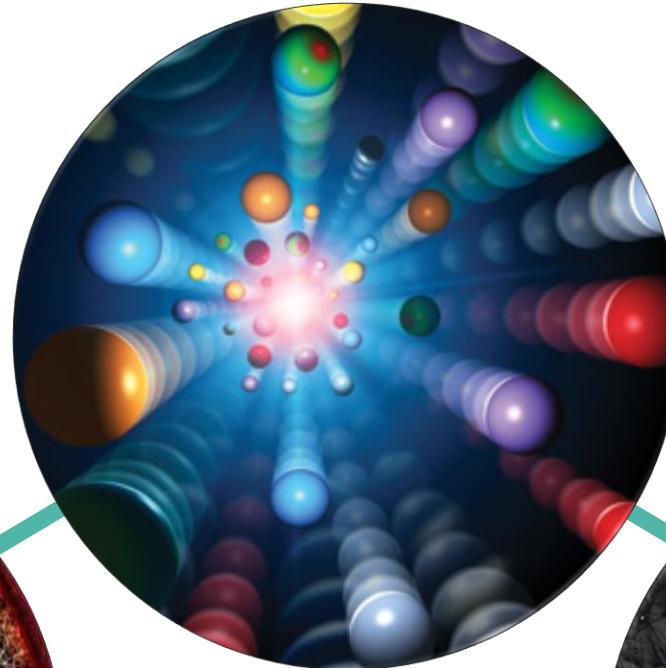
# Cosmology – range of subjects

## ■ subjects of cosmology

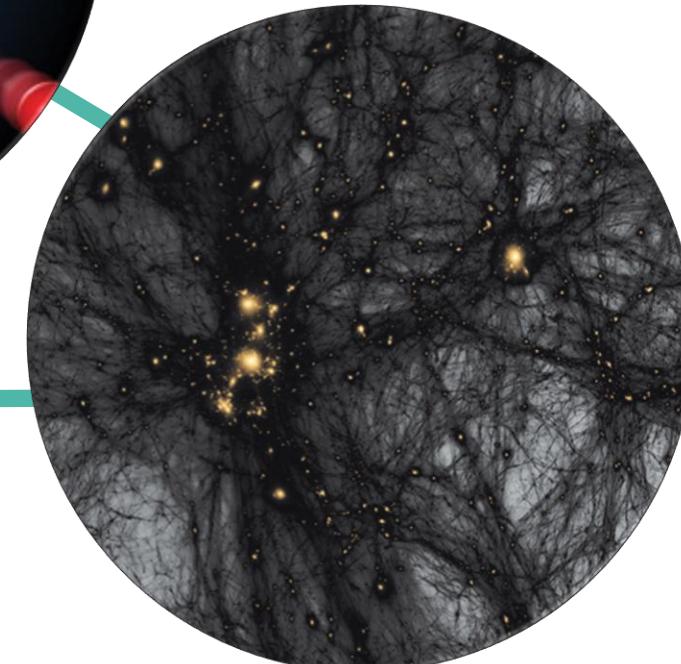
structure formation



processes in



the early universe

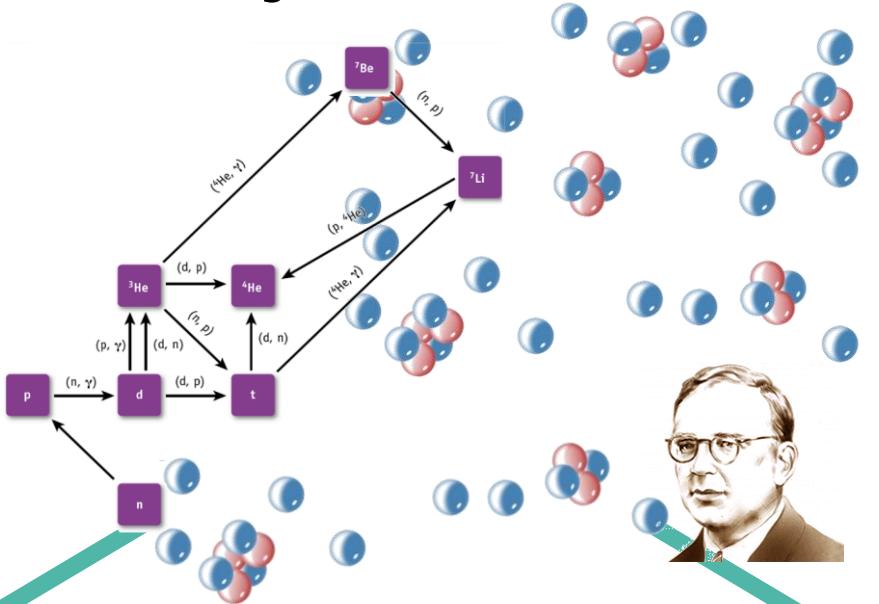
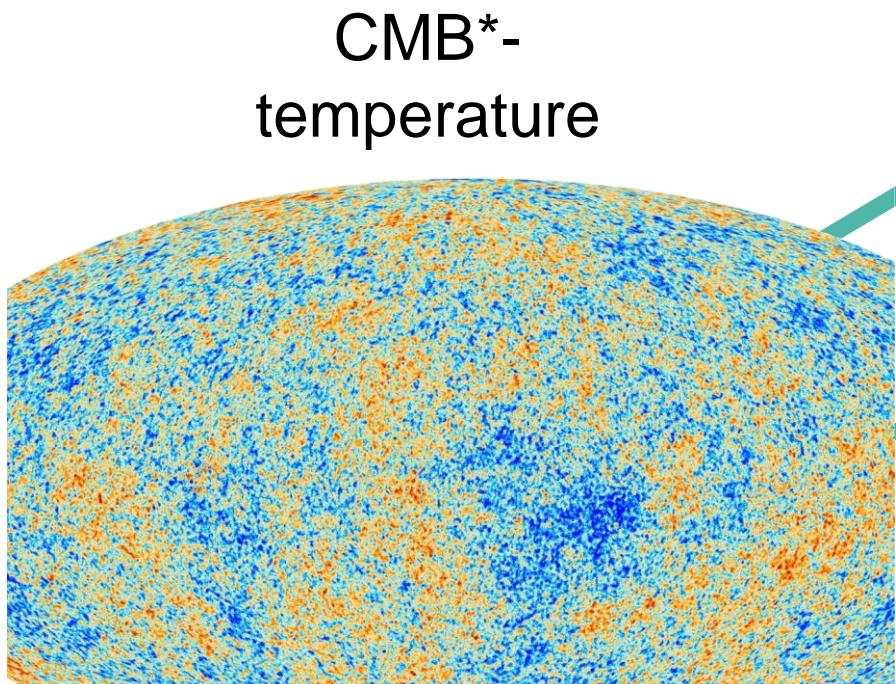


dark  
universe

three pillars  
of these lectures

# Cosmology – range of subjects

## ■ example: thermal processes



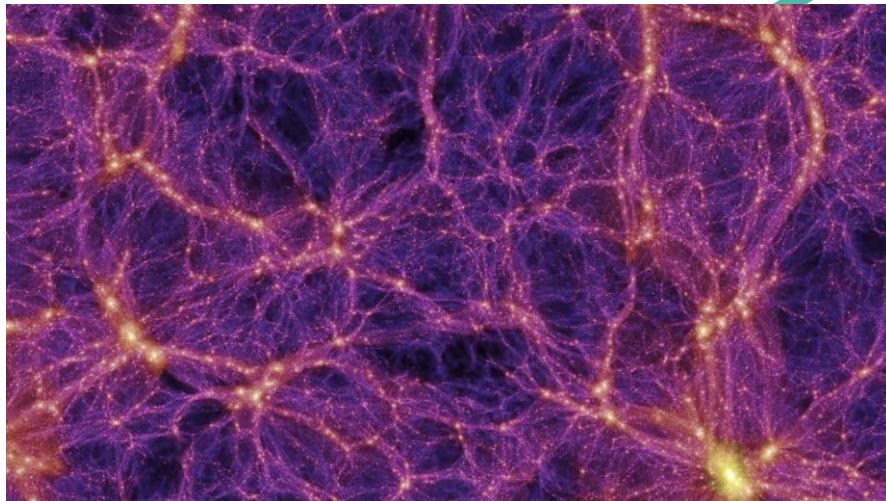
$\nu_e$   $\nu_\mu$   $\nu_\tau$

neutrino  
properties

# Cosmology – range of subjects

## ■ example: **Dark Matter (DM)**

DM in  
structure formation



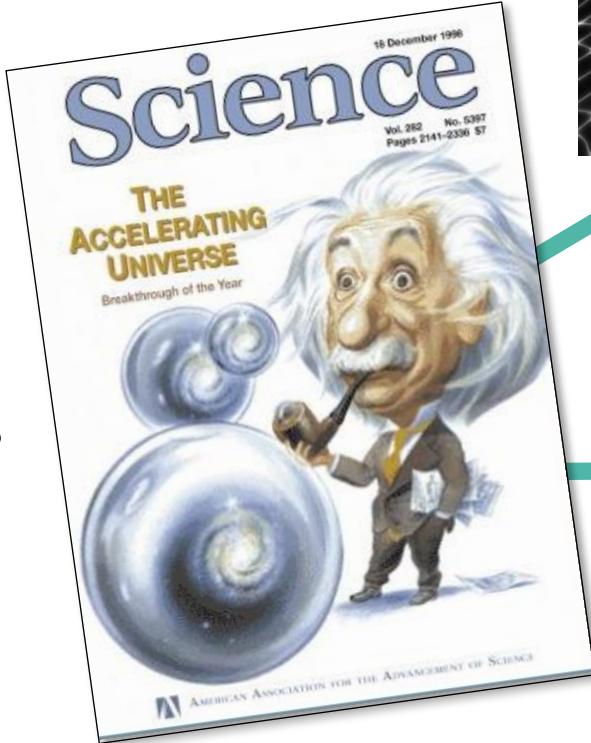
DM-particle candidates:  
HDM\*, WDM\*\*, CDM\*\*\*



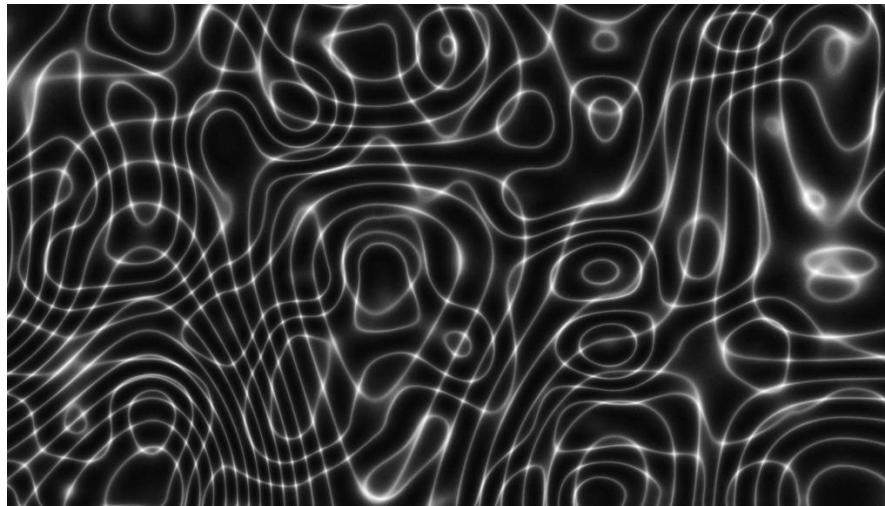
galactic  
DM-  
halos

# Cosmology – range of subjects

- example:  
**Dark Energy (DE)**



evidences  
for DE



nature of DE:  
**cosmological  
constant?**

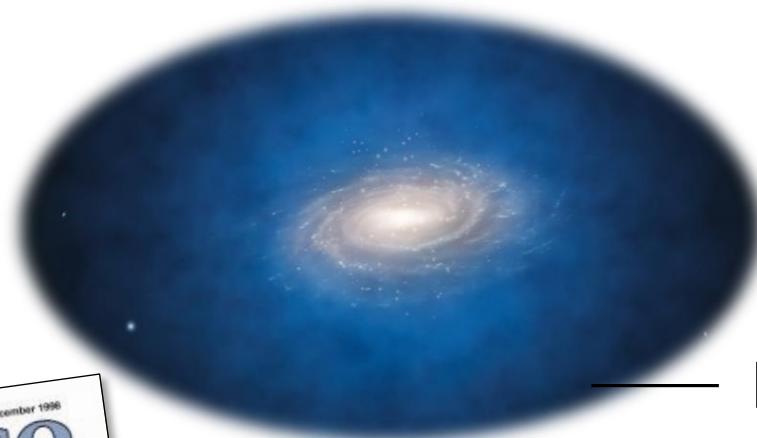
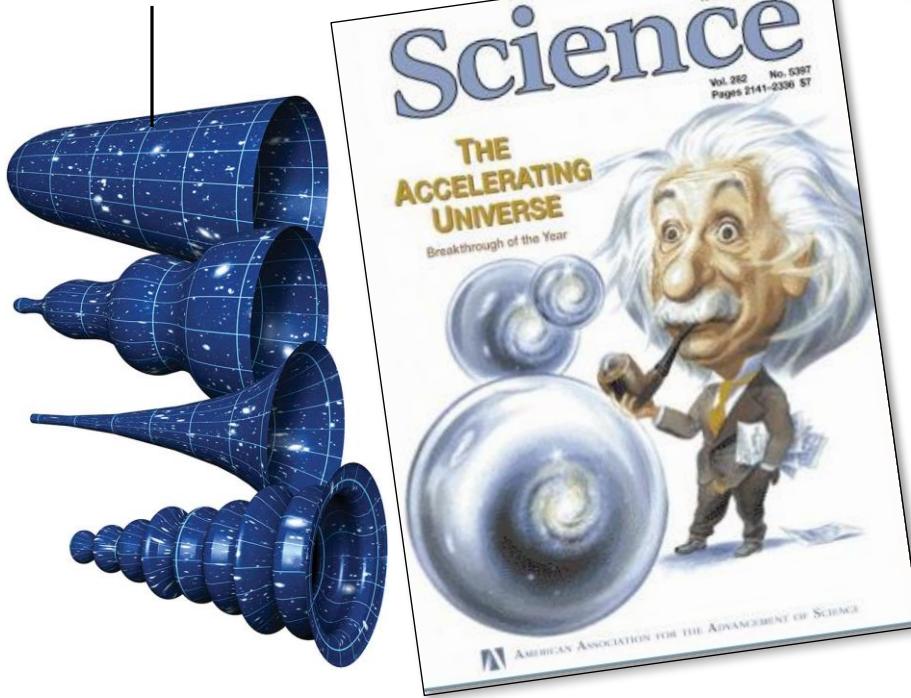


DE &  
expansion  
rate of the  
universe

# Cosmology – new concepts

## ■ classification

Antigravitation



Dark Matter



Bachelor  
Studies



gravitation

nuclear physics  
thermodynamics

optics

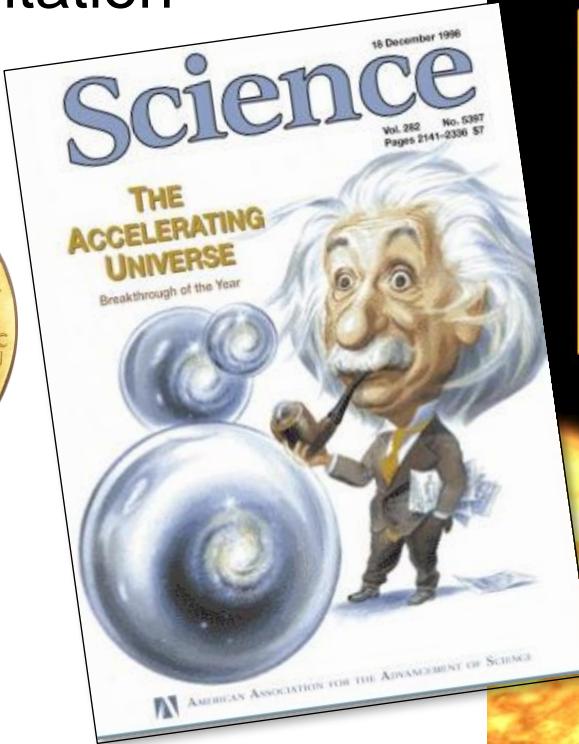
condensed  
matter, atoms,  
molecules

# Cosmology – modern observations

## ■ Nobel Prize 2011

*„for the discovery of the **accelerating expansion of the Universe** through observations of distant supernovae“*

### Antigravitation



Saul Perlmutter



Adam G. Riess



Brian P. Schmidt

# Cosmology – modern theories

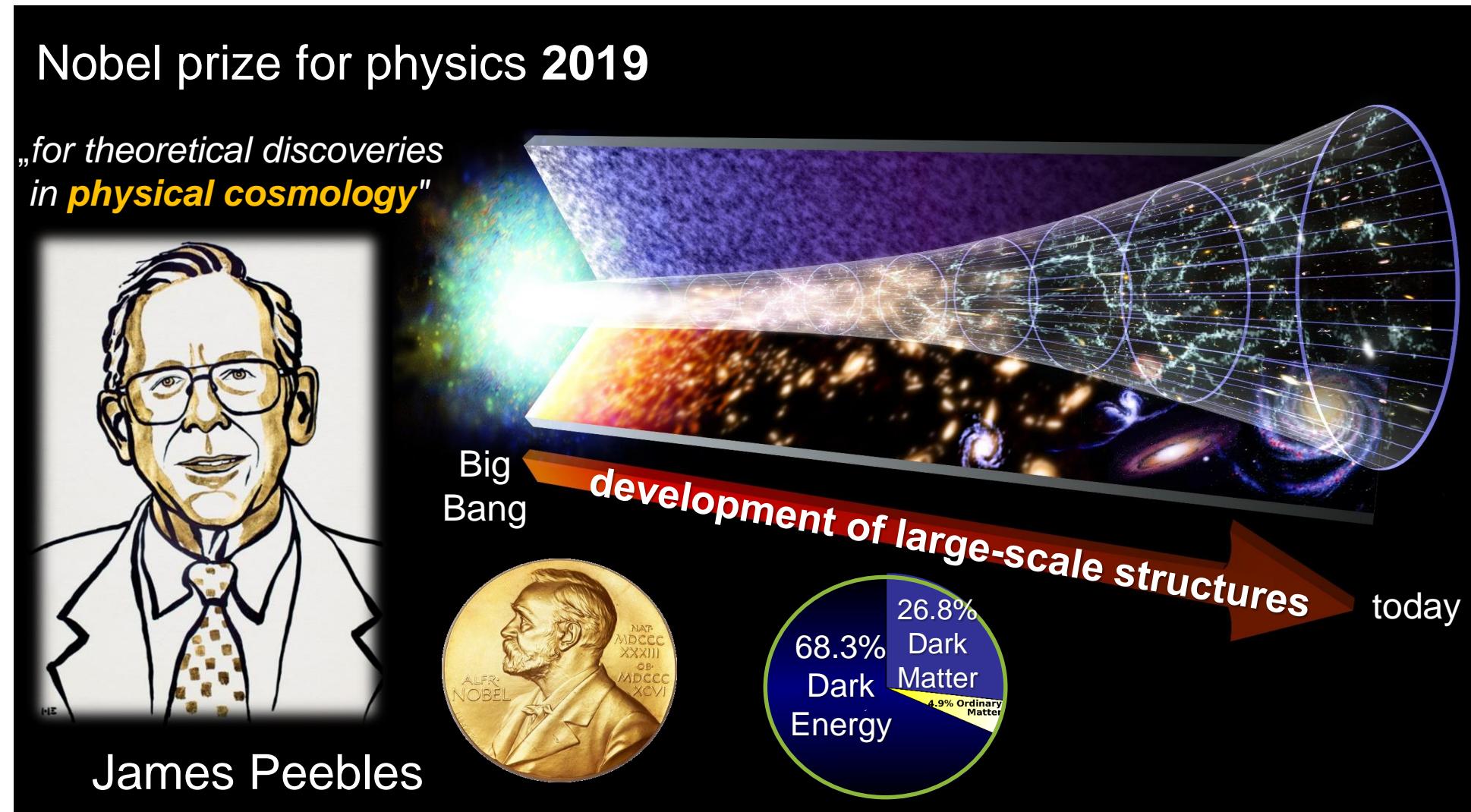
## ■ Nobel Prize 2019

structure formation



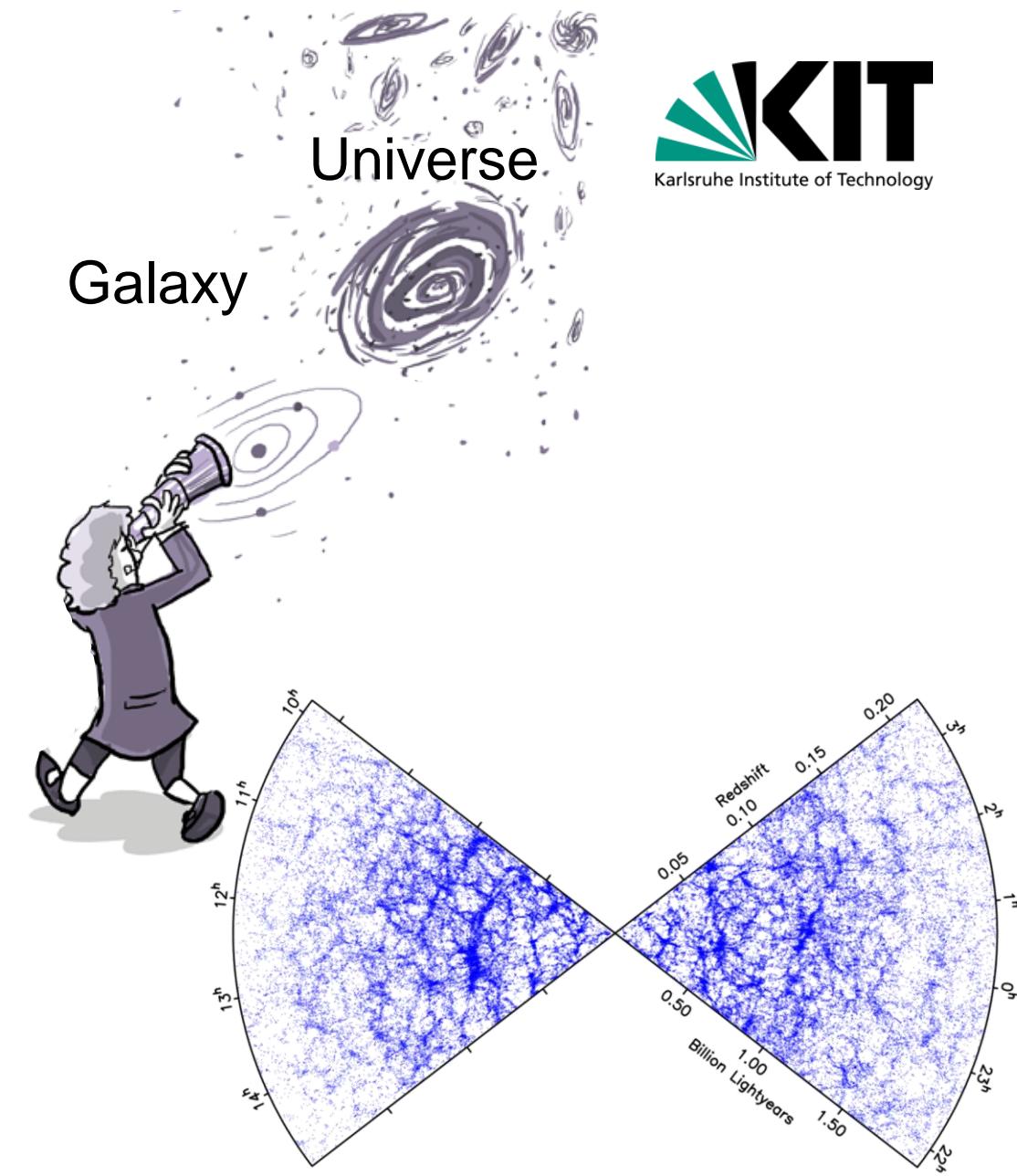
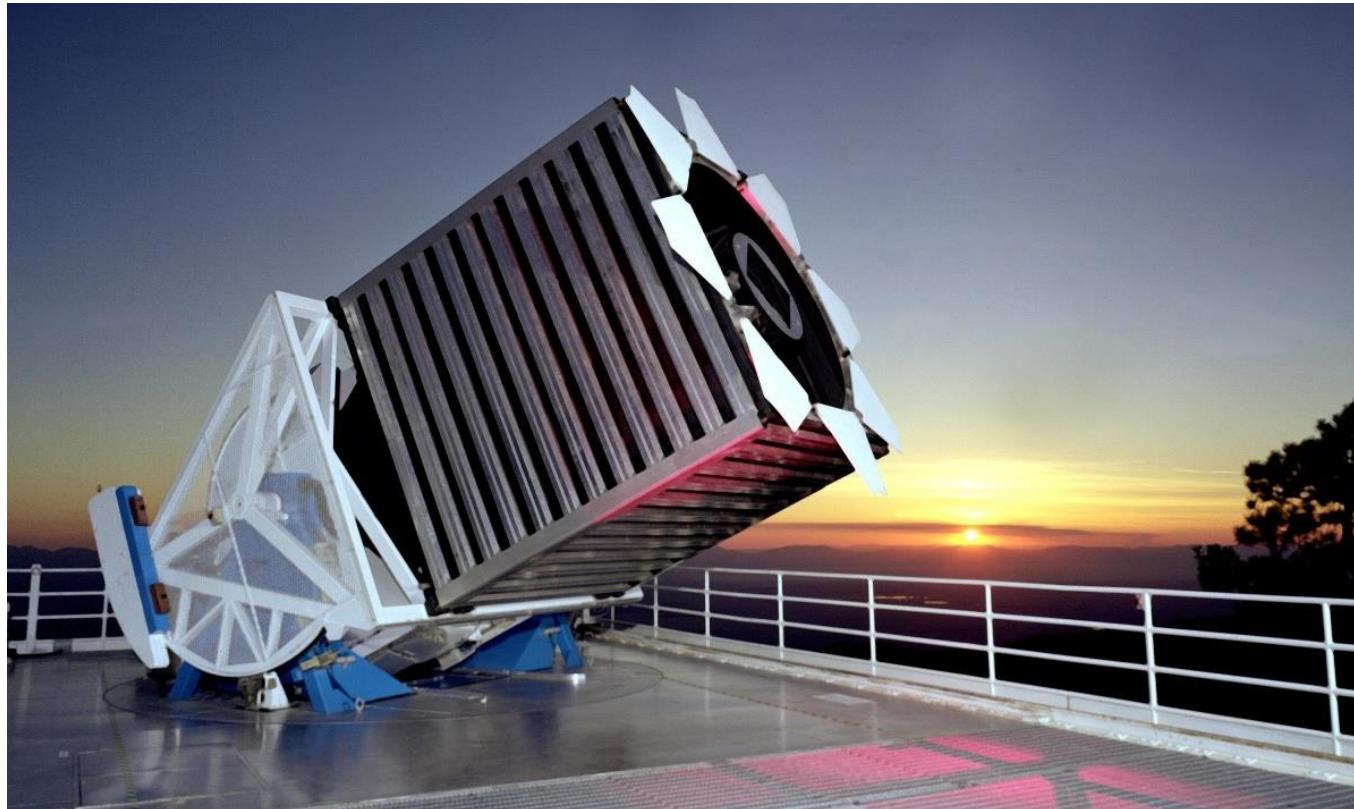
50%

$$\delta(\vec{r}) = \frac{\rho(\vec{r}) - \langle \rho \rangle}{\langle \rho \rangle}$$



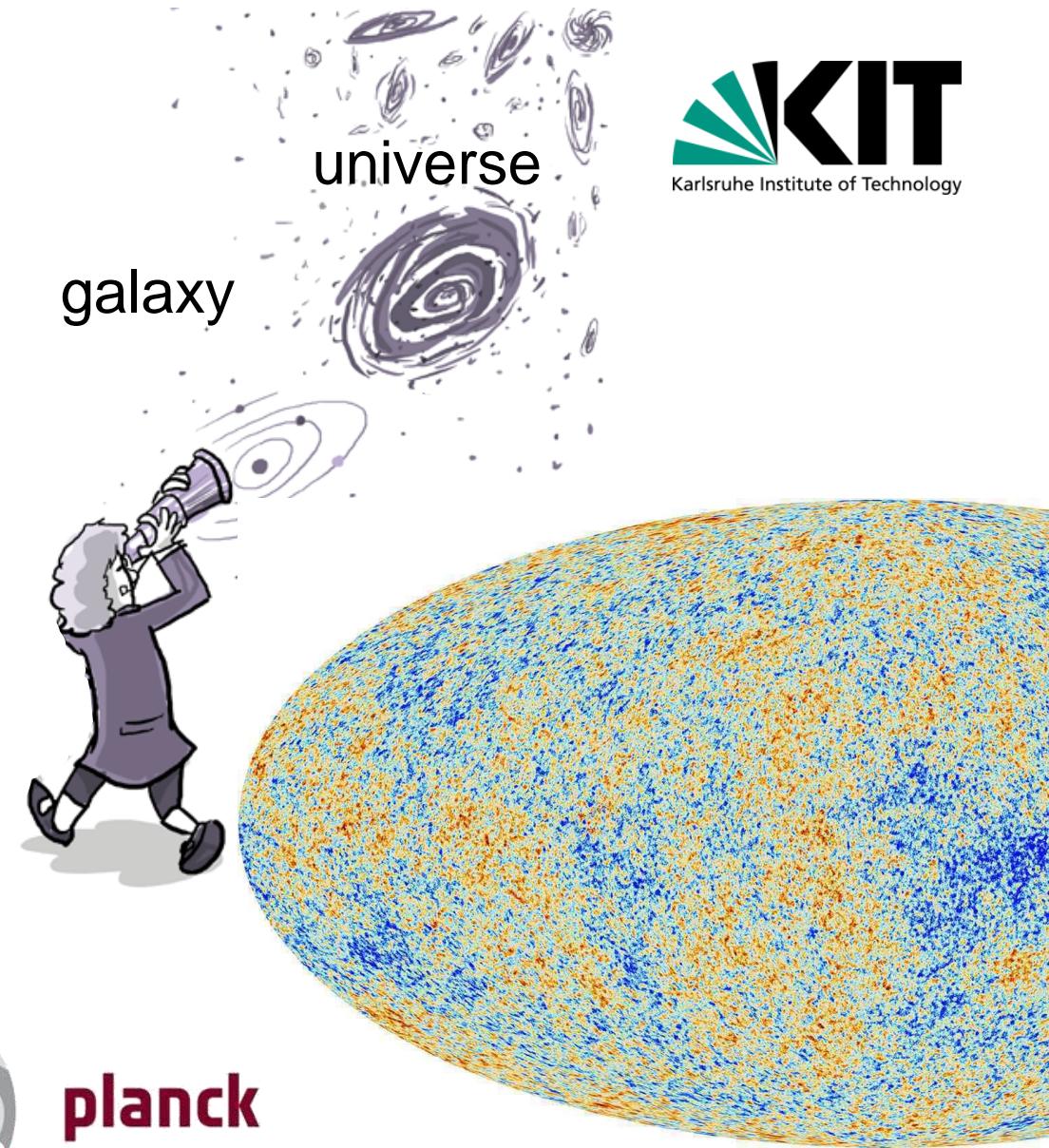
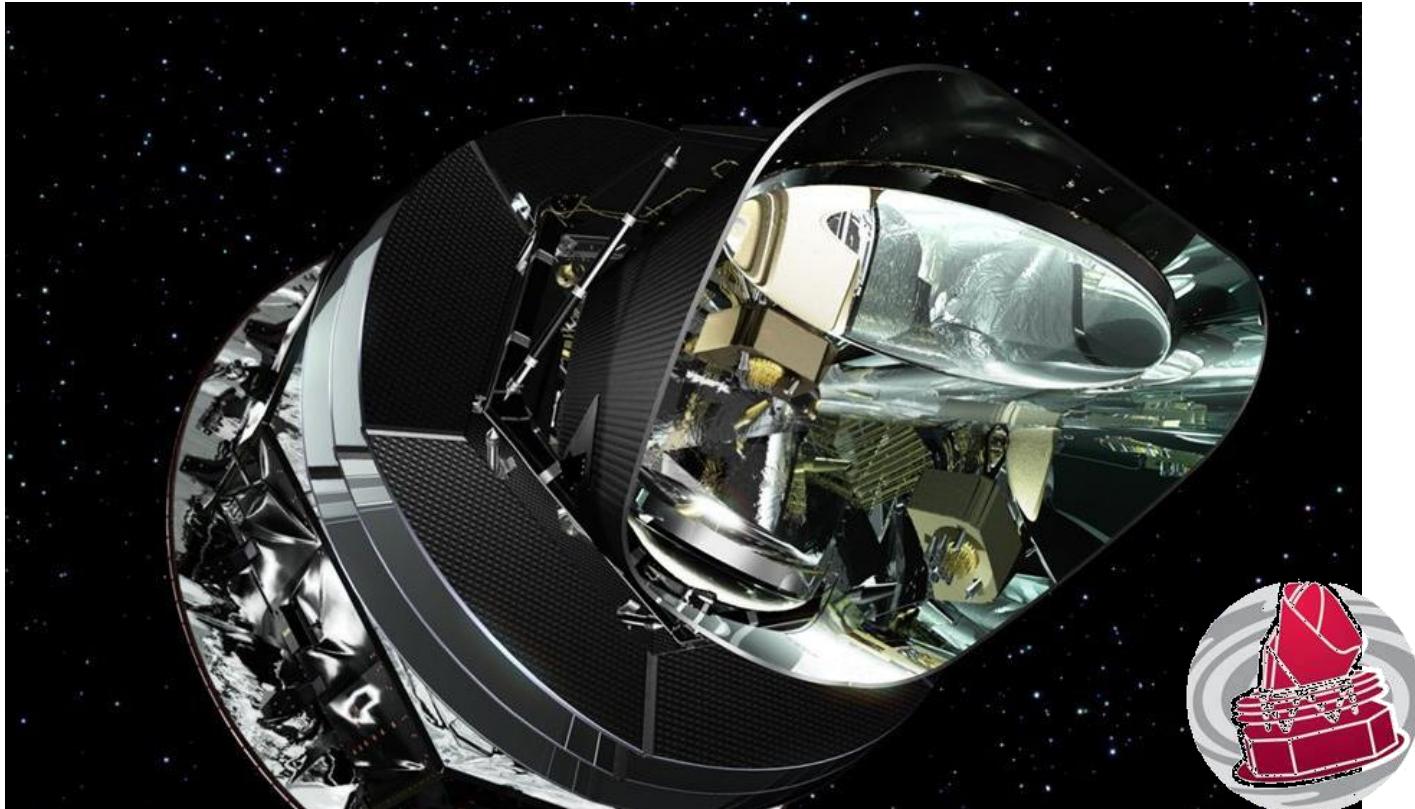
# Cosmology – observations

- example: **galaxy redshift surveys**



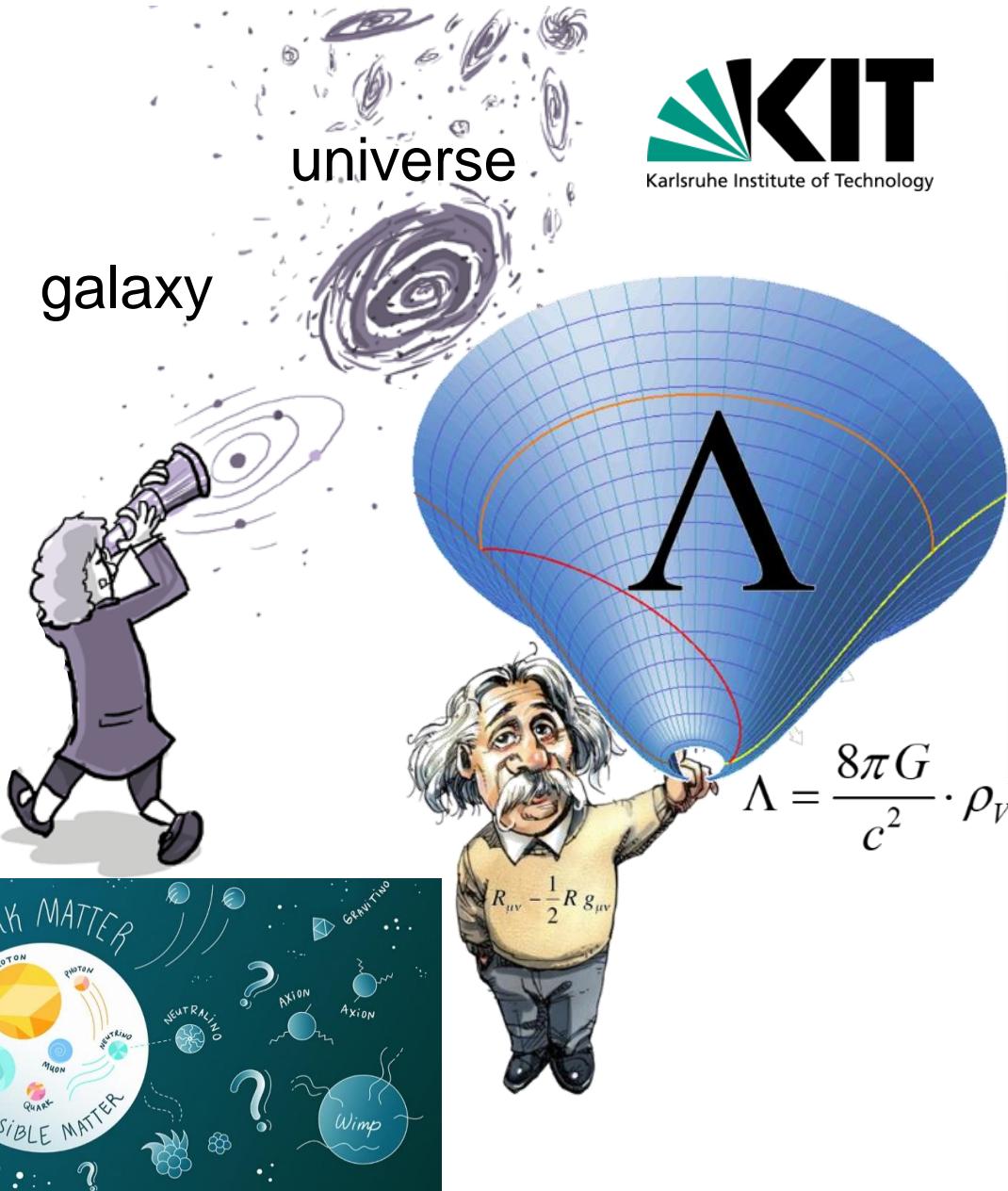
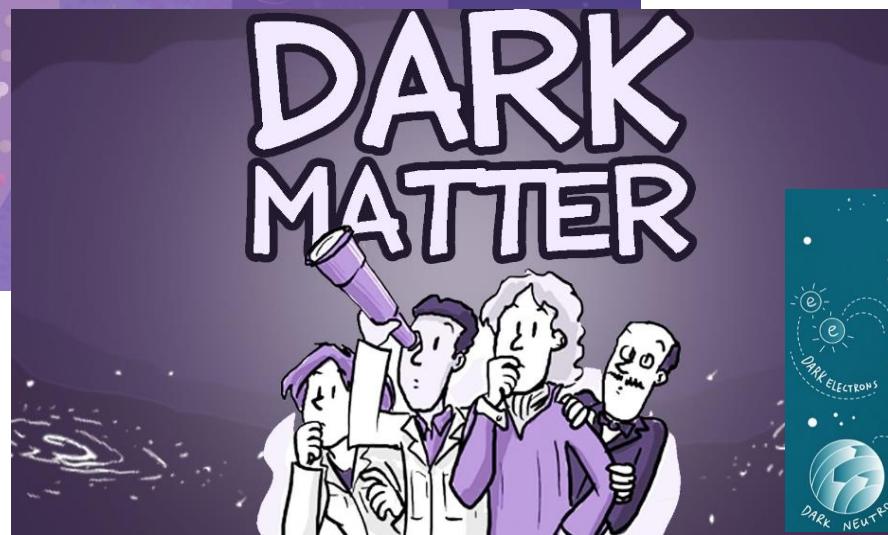
# Cosmology – observations

- example: temperature fluctuations of the CMB (cosmic microwave background radiation)



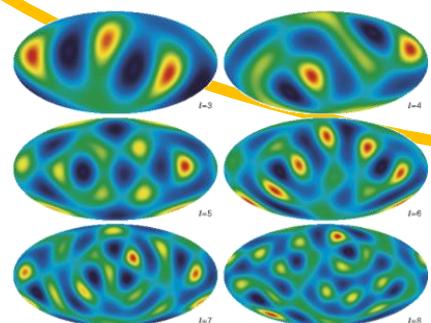
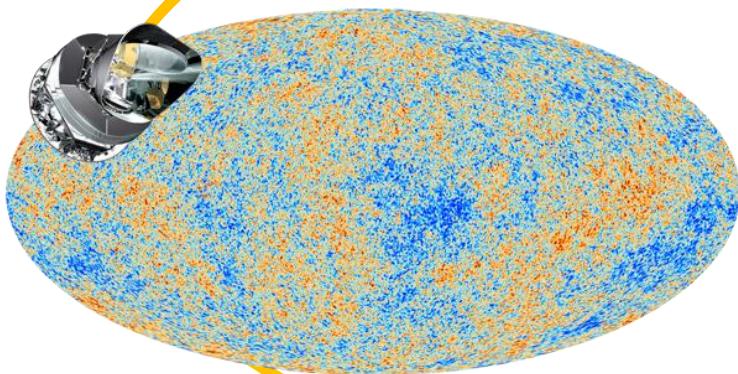
# Cosmology – open questions

- what is the intrinsic nature of Dark Matter & Dark Energy ?



# I can learn the following in this lecture series:

**BREAKING  
NEWS**

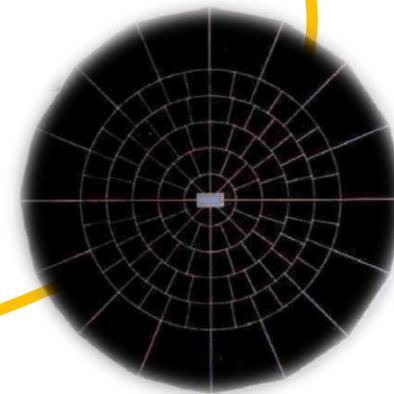


**...modern analysis methods...**



$$\left(\frac{\dot{H}(t)}{H(t)}\right)^2 \sim 1 + \frac{7\Delta N_\nu}{43}$$

**...new tools for discoveries...**



**...advanced experimental methods...**



# OUTLINE

## 1. Introduction

1.1 fundamental principles

1.2 distance ladders for the universe

## 2. Expanding Universe

2.1 Hubble Expansion

2.2 Friedmann-Lemaître equations

## 3. Thermal Universe

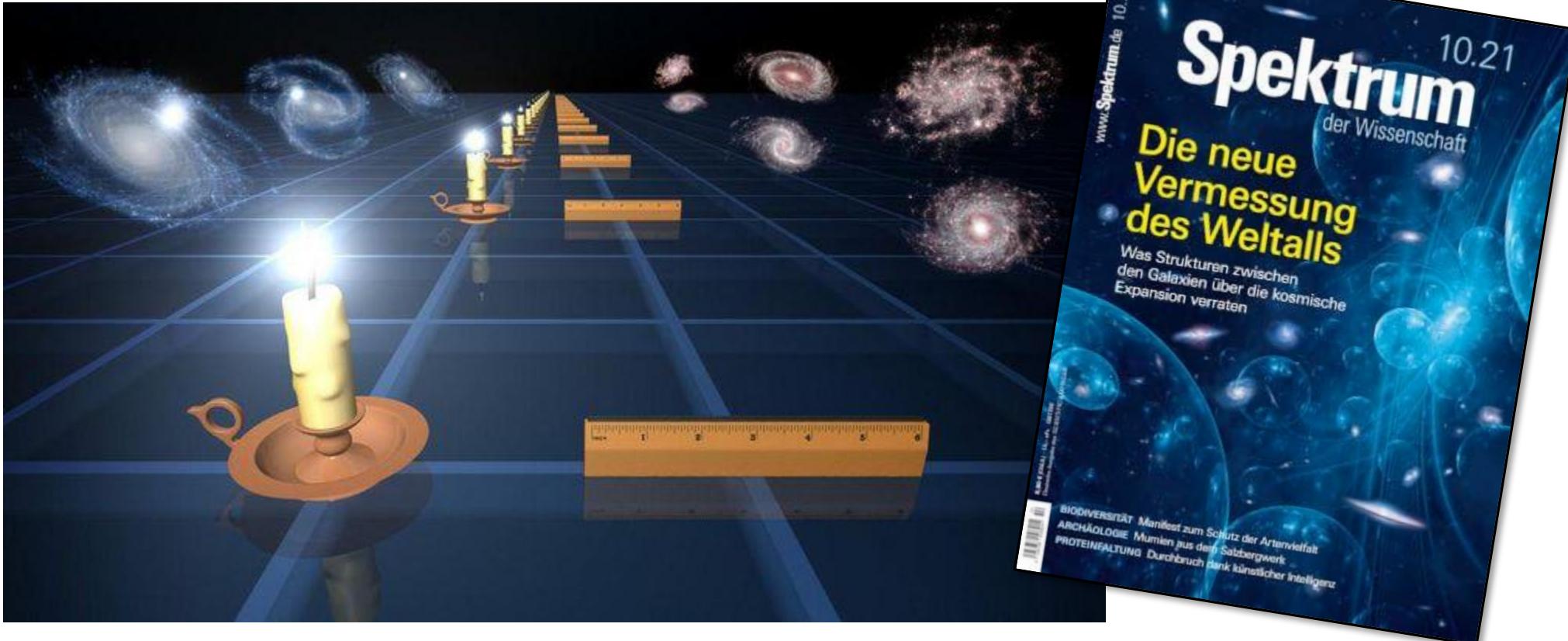
- 3.1      **primordial nucleosynthesis (BBN)**  
             the first three minutes
- 3.2      **cosmic microwave background radiation – essentials:**  
             formation, black body radiation, fluctuations
- 3.3      **cosmic microwave background radiation – experiments:**  
             COBE, WMAP & Planck
- 3.4      **cosmological  $\Lambda$ CDM concordance model**

## 4. Structure Formation in the Universe

- 4.1      **Inflation & Early Universe**
- 4.2      **BAO – Baryon Acoustic Oscillations :**  
              formation & relevance in the present universe
- 4.3      **Large-scale Galaxy Surveys:**  
              the matter power spectrum
- 4.4      **Evolution of Large-Scale Structures:**  
              hot, warm & cold Dark Matter

## 5. Dark Universe

- 5.1      **Evidences for Dark Matter:**  
from Vera Rubin & Fritz Zwicky to the Bullet-Cluster
- 5.2      **Gravitational Lenses for the Dark Universe:**  
strong & weak lensing
- 5.3      **Dark Matter Halos: the NFW-Profile**
- 5.4      **Dark Energy:**  
the future evolution of the universe



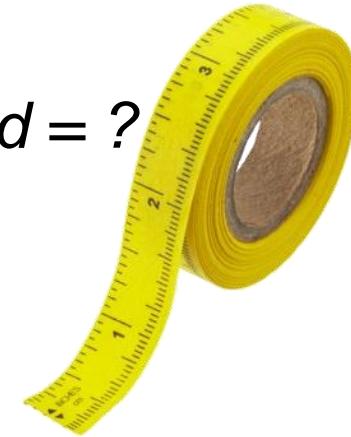
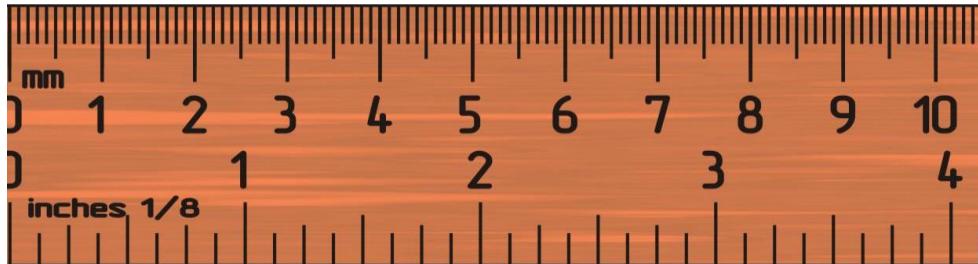
Q: NASA

# CHAPTER 1 - INTRODUCTION

# cosmological distances and time scales

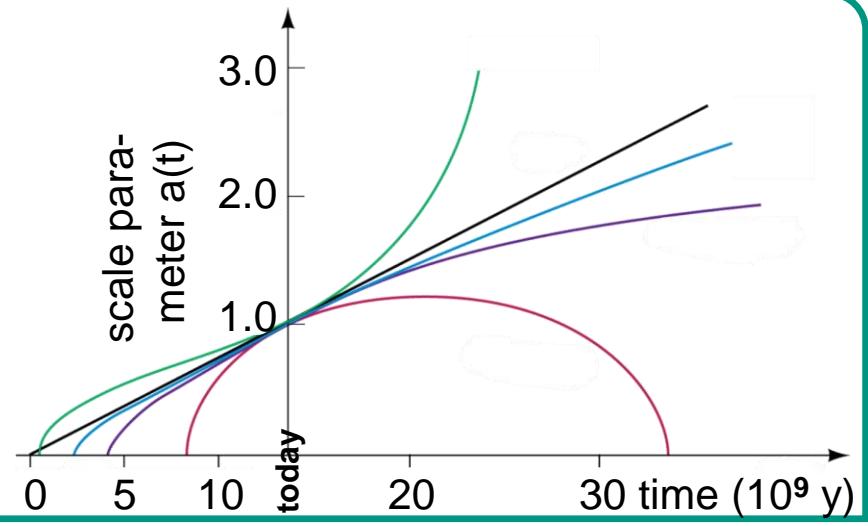
## ■ Measurement of distances

- cosmological standard candles up to  $d = ?$

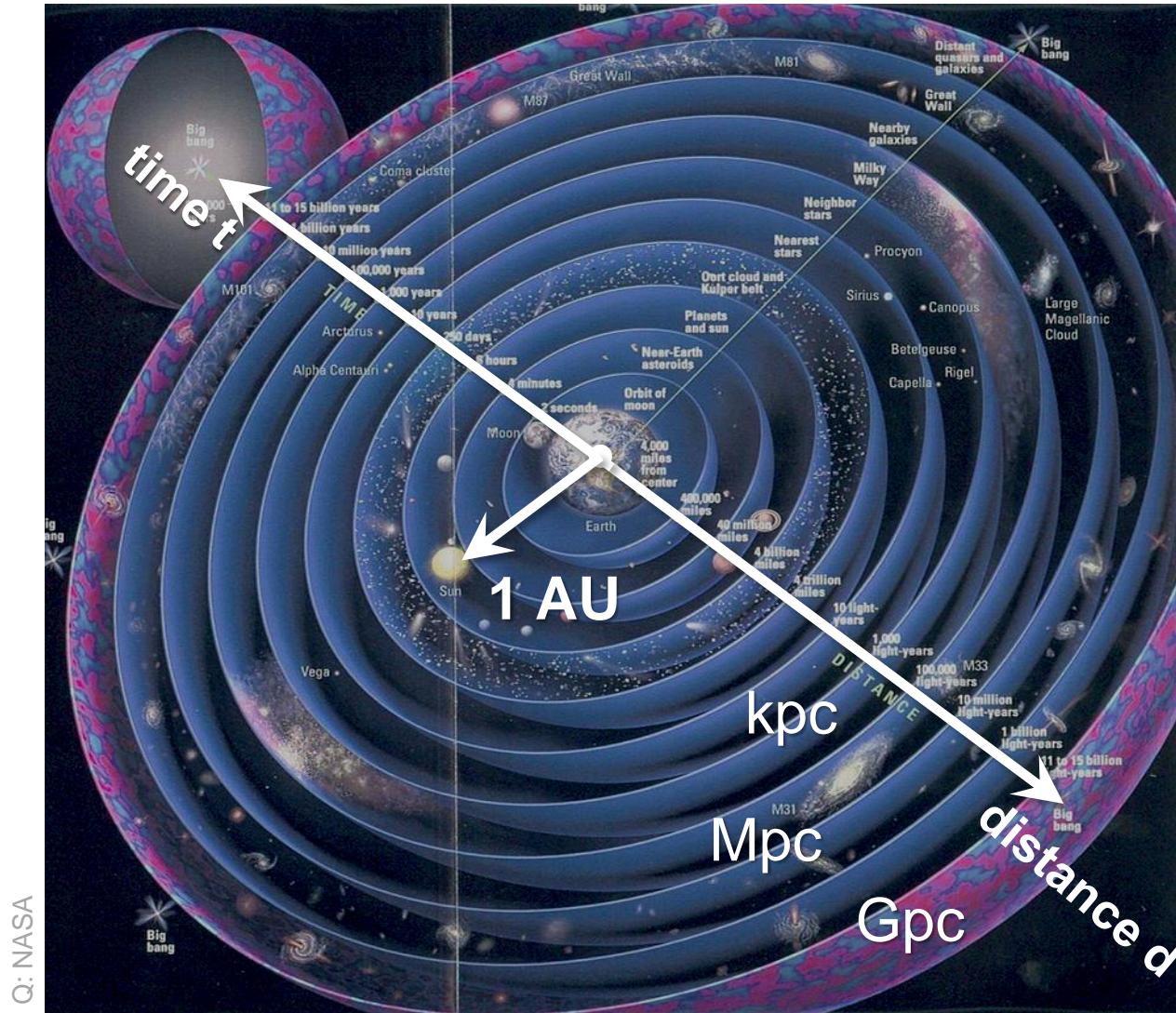


## ■ Measurement of cosmological time scales

- cosmological standard time scale up to  $t = ?$



# Cosmology: typical time- and distance-scales



astronomical scales	
<b>1 AU</b>	$1.496 \times 10^{11}$ m
<b>1 ly</b>	$9.461 \times 10^{15}$ m = 63 240 AU = 0.3066 pc
<b>1 pc</b>	$3.086 \times 10^{16}$ m = $2.06 \times 10^5$ AU = 3.262 ly

**AU: Astronomical Unit**

major semi-axis of Earth around Sun

**ly: light-year**

light trajectory in  $t = 1$  a

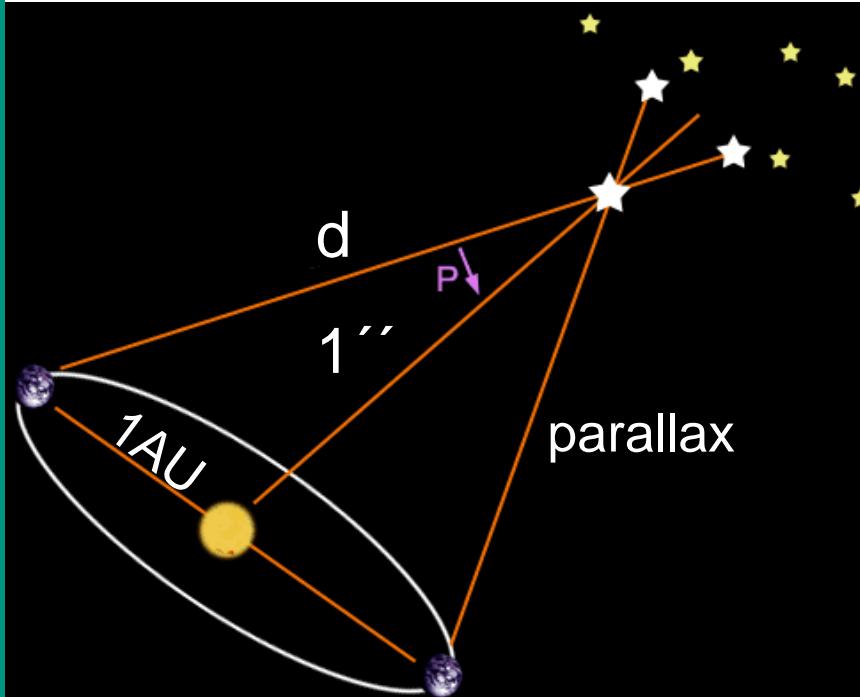
*distance d*

**pc: parsec**

parallax of 1 arc-sec

# Cosmology: typical time- and distance-scales

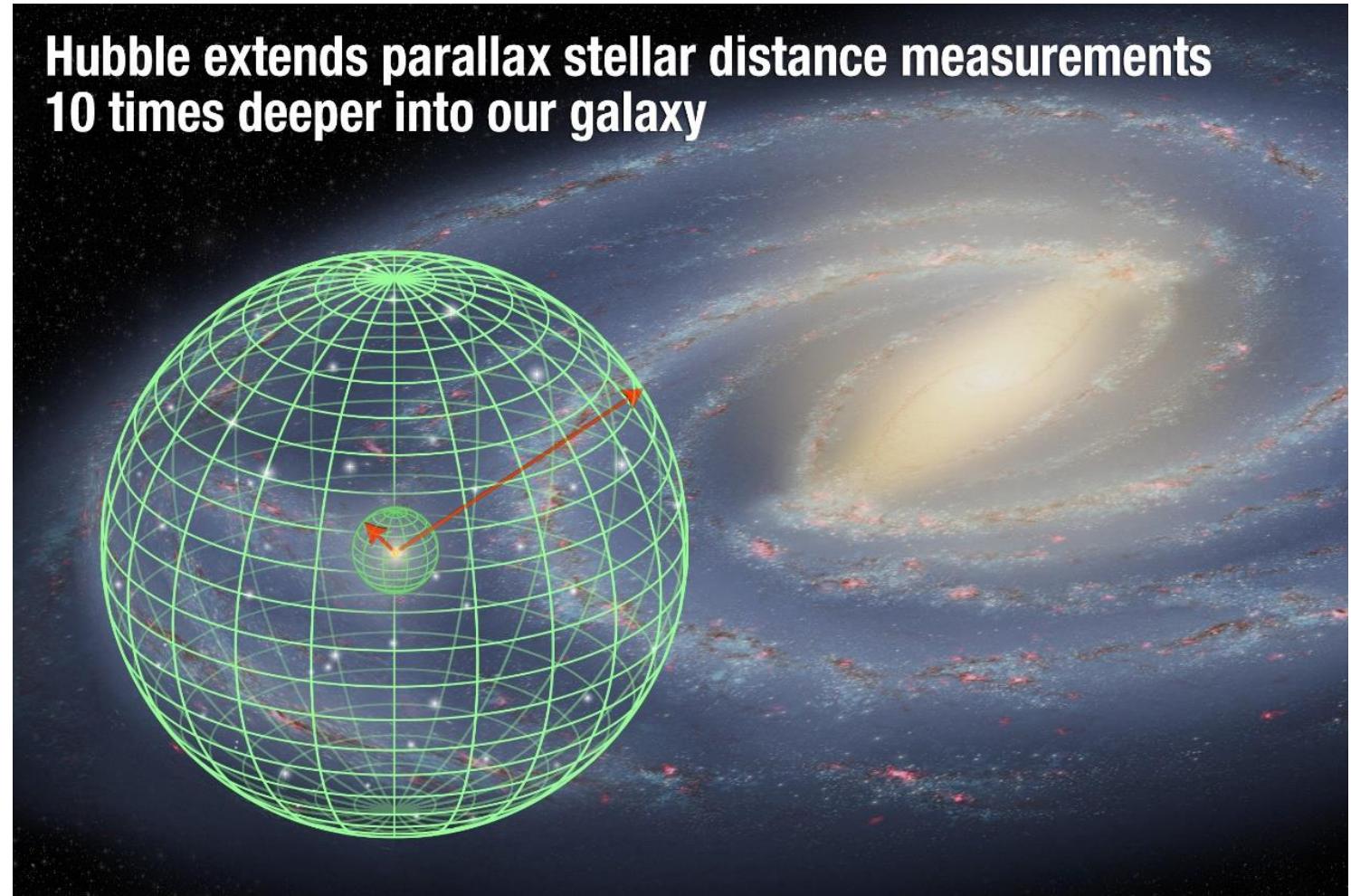
## Definition of „parallax“



**parallax:**

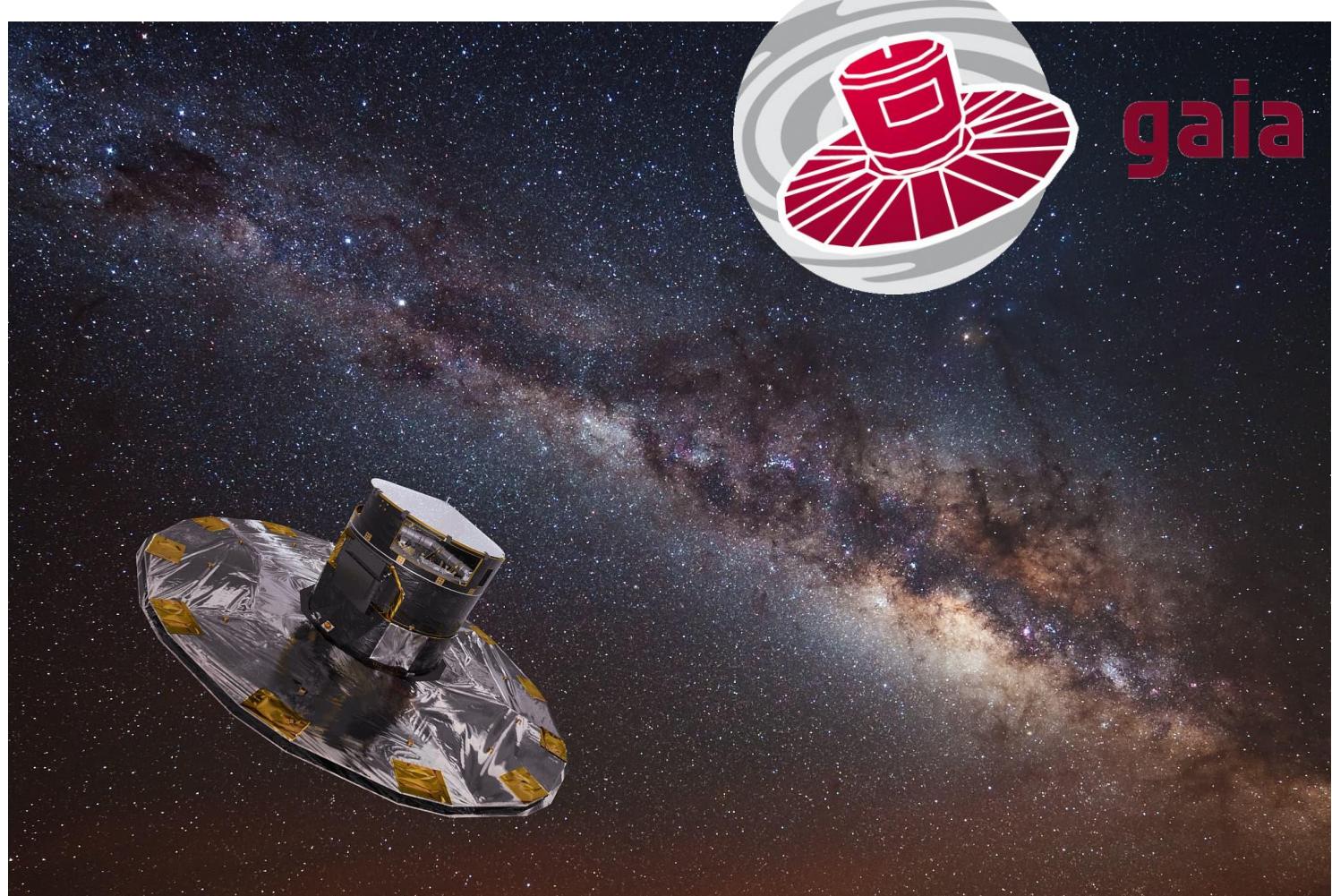
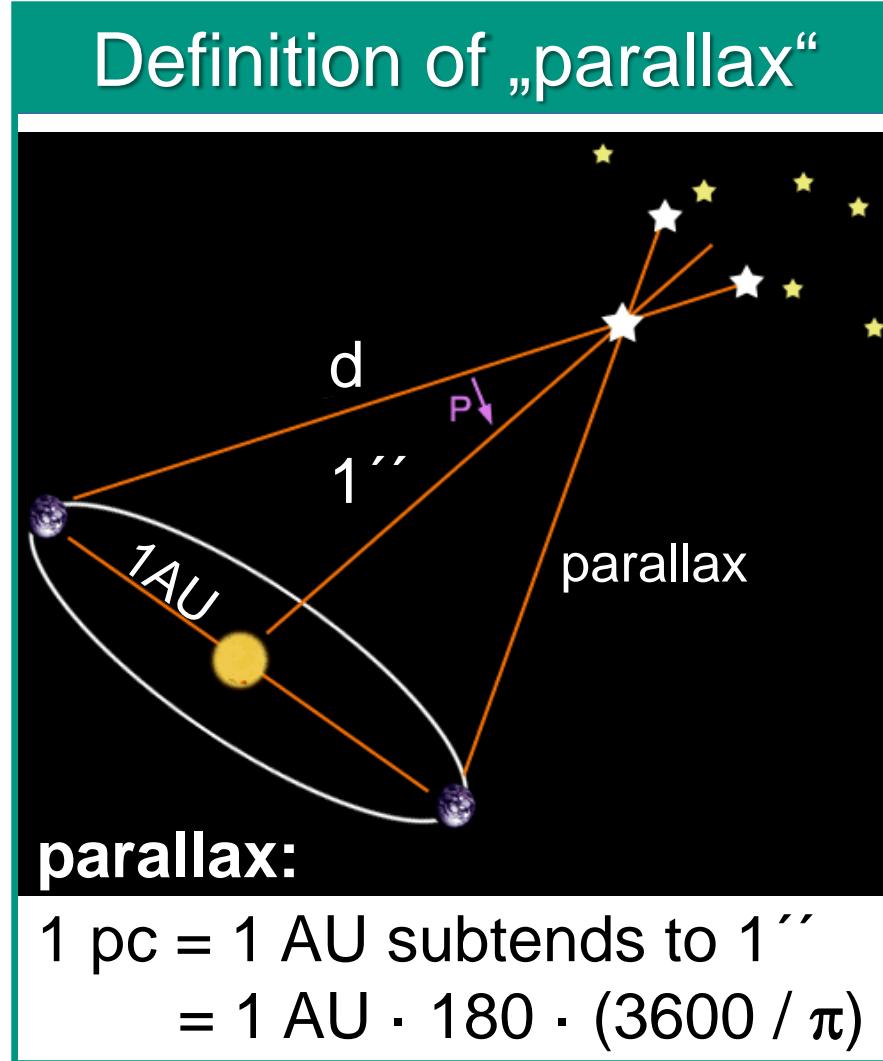
$$1 \text{ pc} = 1 \text{ AU subtends to } 1''$$
$$= 1 \text{ AU} \cdot 180 \cdot (3600 / \pi)$$

**Hubble extends parallax stellar distance measurements 10 times deeper into our galaxy**



2014 - range of parallax measurements now: 3-4 kpc

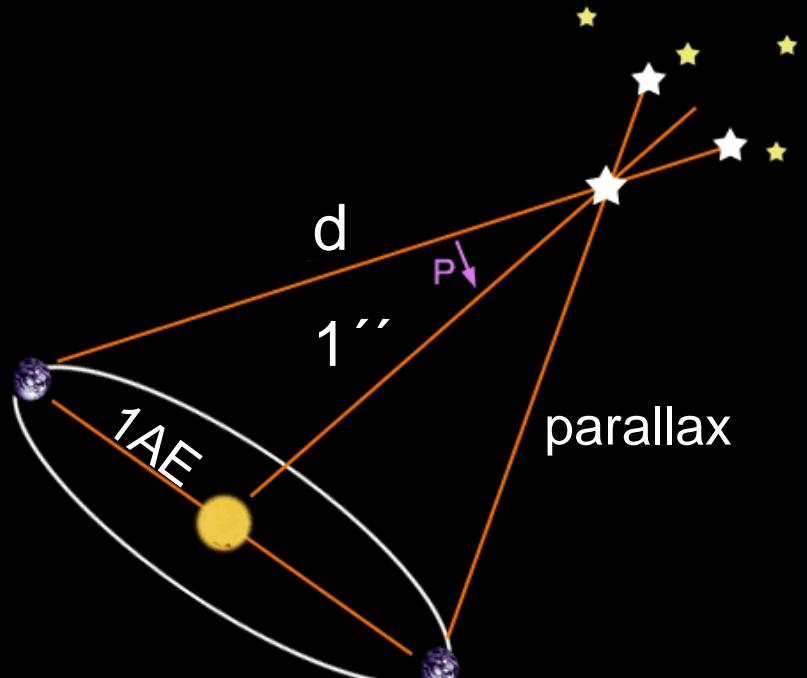
# Cosmology: typical time- and distance-scales



measurements of GAIA with  $\mu\text{as}$ -precision\*

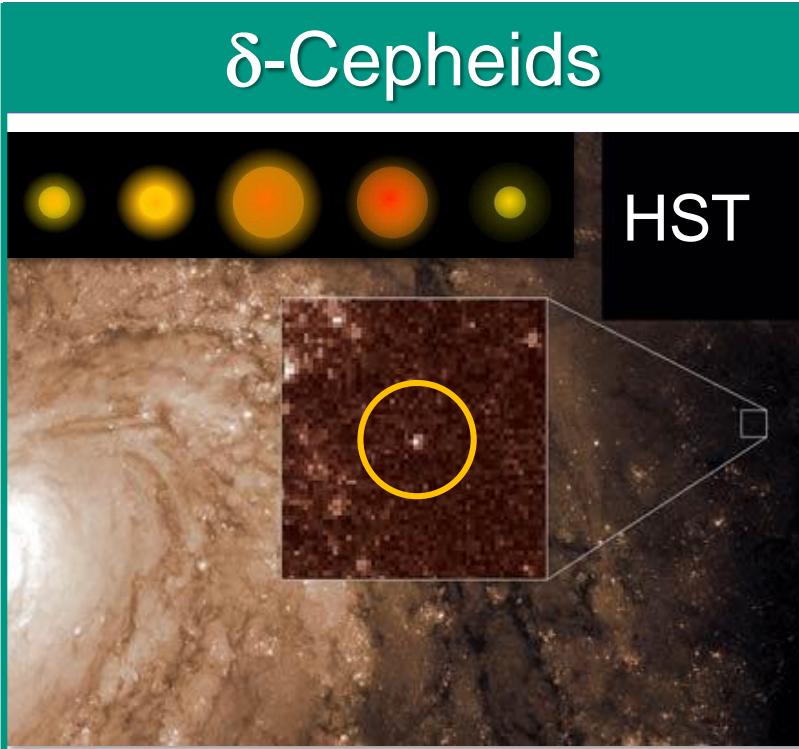
# Cosmology: typical time- and distance-scales

## parallax method



**Parallax method: reach to  
d = few kpc (Milky Way)**

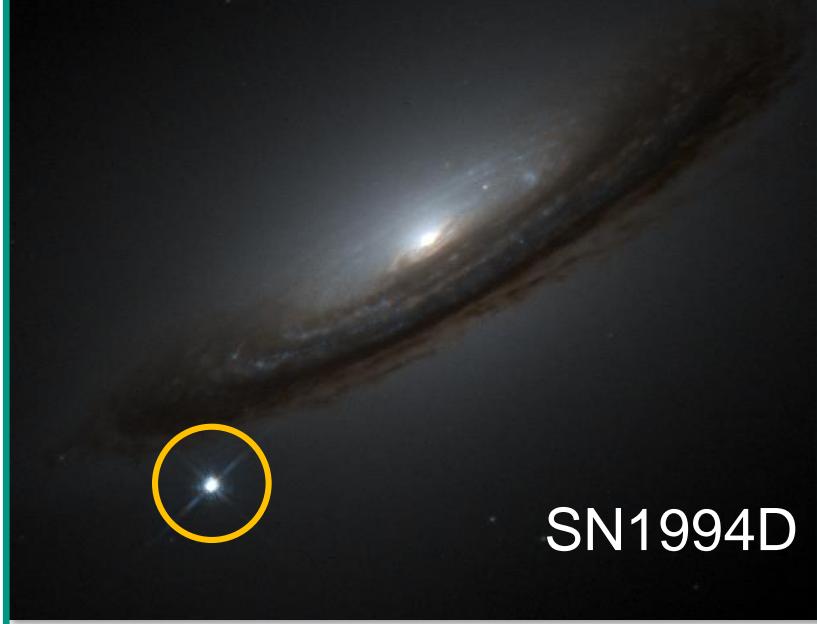
## $\delta$ -Cepheids



**$\delta$ -Cepheids:** absolute  
luminosity  $L_{abs} \sim 10^4 L_\odot$   
d = 1 kpc - 50 Mpc

luminosity of the sun:  $L_\odot$

## SN-Ia-brightness curve

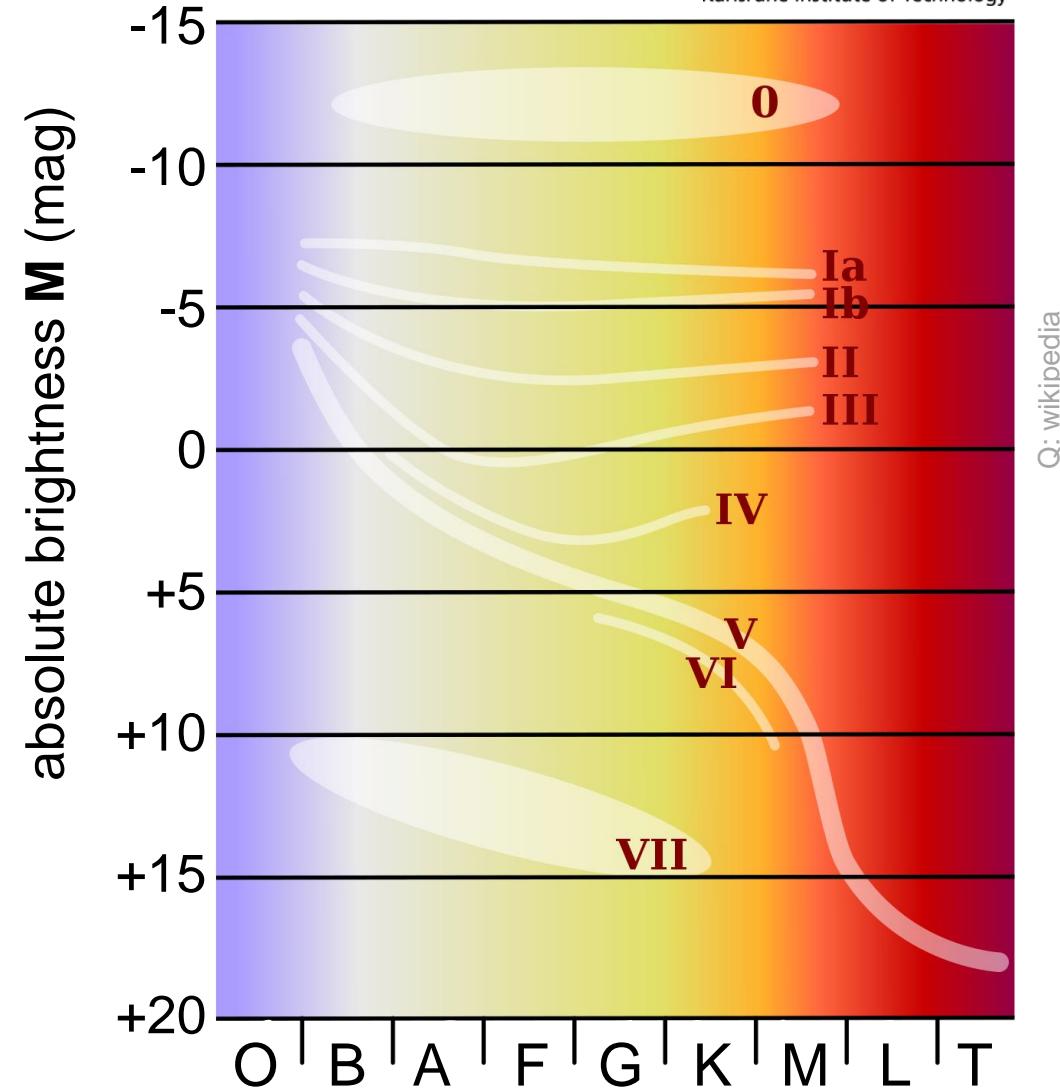
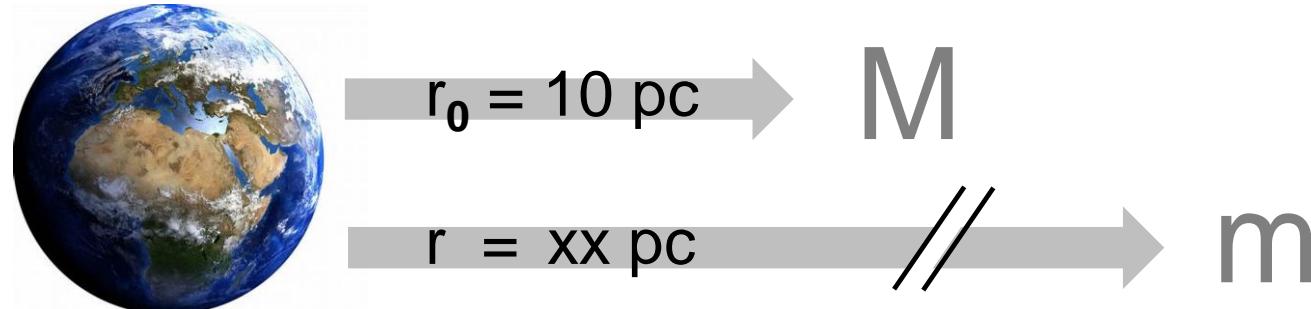


**Supernovae Type Ia:**  
luminosity  $L_{abs} \sim 10^9 L_\odot$   
d = 30 Mpc – 3 Gpc

# Brightness – definition in astronomy

## ■ absolute & relative brightness

- brightness of objects is measured in **magnitudes (mag)** = logarithmic scale
- absolute brightness **M**:  
defined at unit distance  $r_0 = 10 \text{ pc}$
- apparent brightness **m**:  
object as it appears here on Earth



Q: wikipedia

# Brightness – cosmological standard candles

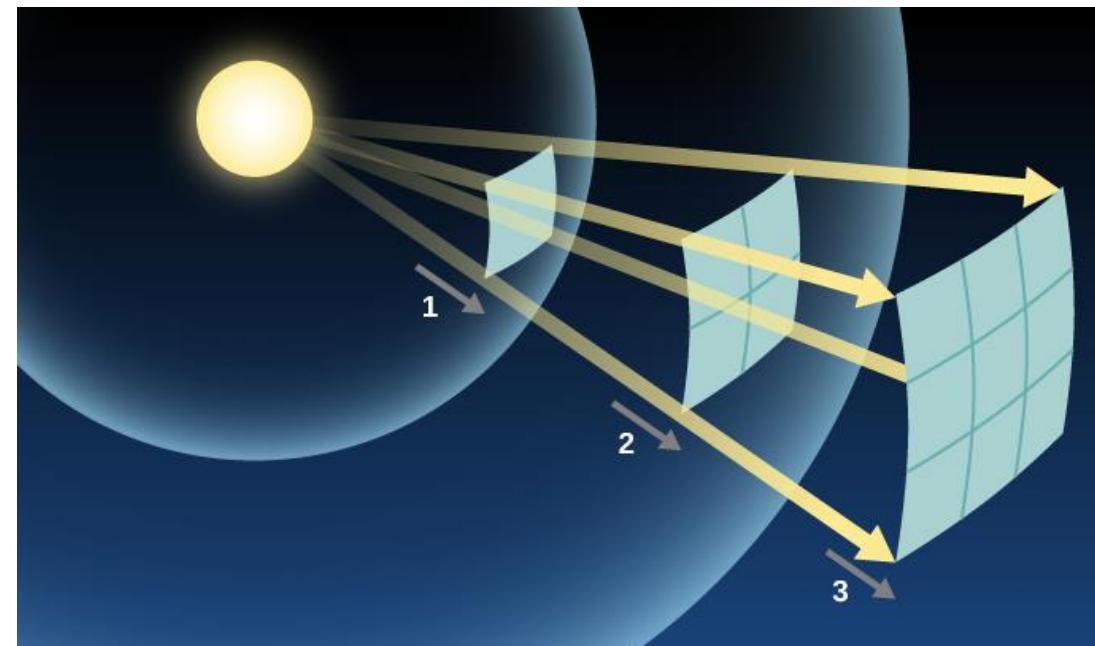
## ■ absolute & apparent brightness: magnitude

- reference:  $m \equiv 0$  is defined for the nearby star **Wega** ( $\alpha$  Lyrae)
- mag = logarithmic unit: difference of 5 mag  $\equiv$  factor 100 in brightness  
per magnitude: factor  $= \sqrt[5]{100} = 2.512$

## - Distance modulus $m - M$ :

$$m - M = 5 \cdot \log \left( \frac{r}{r_0} \right)$$

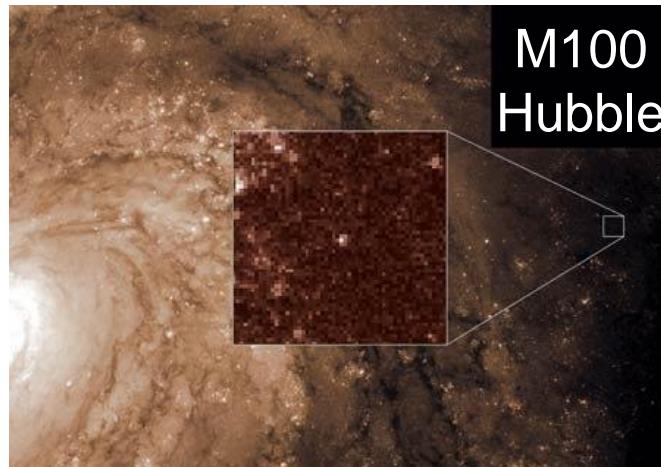
quadratic  
distance law



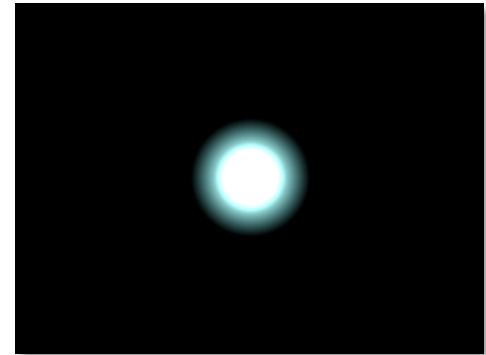
# Cepheids – cosmological standard candles

## ■ Cepheids:

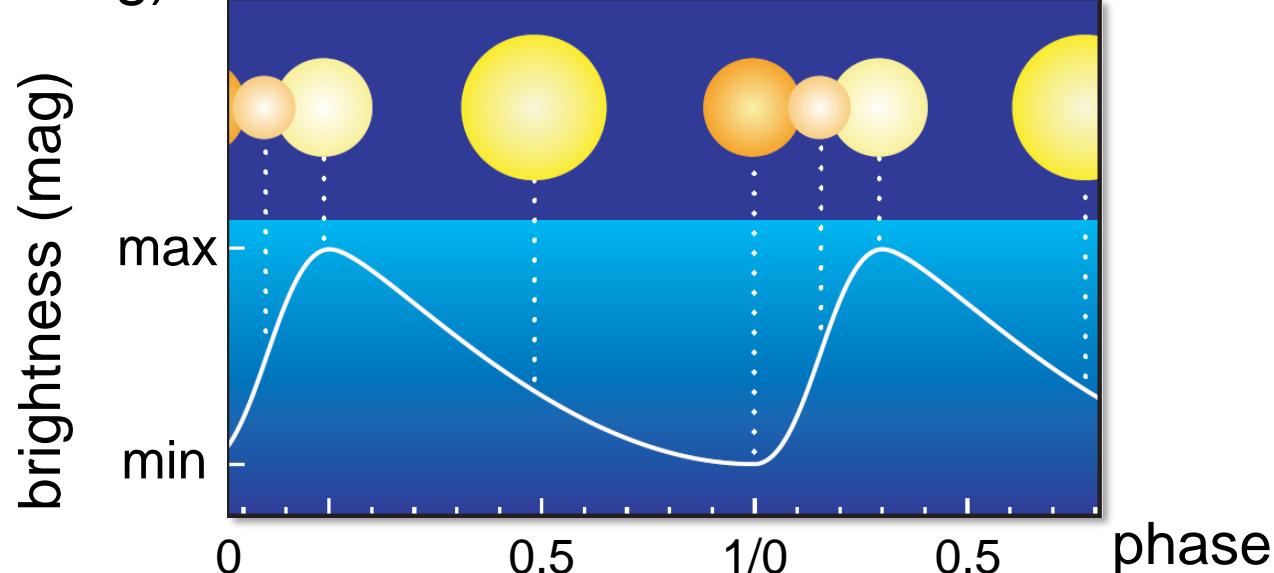
- giant stars with radial pulsations ('super-giants')
- allows to determine **absolute brightness from period  $T_0$**
- mass range:  $M = 5 - 15 M_\odot$  ( $\Rightarrow$  very rare stars)
- spectral class: F, G (white, yellow)
- brightness class: Ia, II ( $M_V = -2 \dots -7$  mag)
- period:  $T_0 < 100$  days



period of a  $\delta$ -Cepheid



Q: NASA



$M_V$  = visual brightness

# Cepheids – cosmological standard candles

## ■ „Kappa mechanism“ causes the radial pulsations of Cepheids

**changes in the opacity  $\kappa(p, T)$  of a specific stellar layer**

- important: hot stellar core causes an **He-ionisation layer** with  $He^{++}$  &  $He^+$  - ions

- **cycle of stellar pulsation:**

**increasing  $T$ :**

more  $He^{++}$  & free electrons

↳ larger opacity

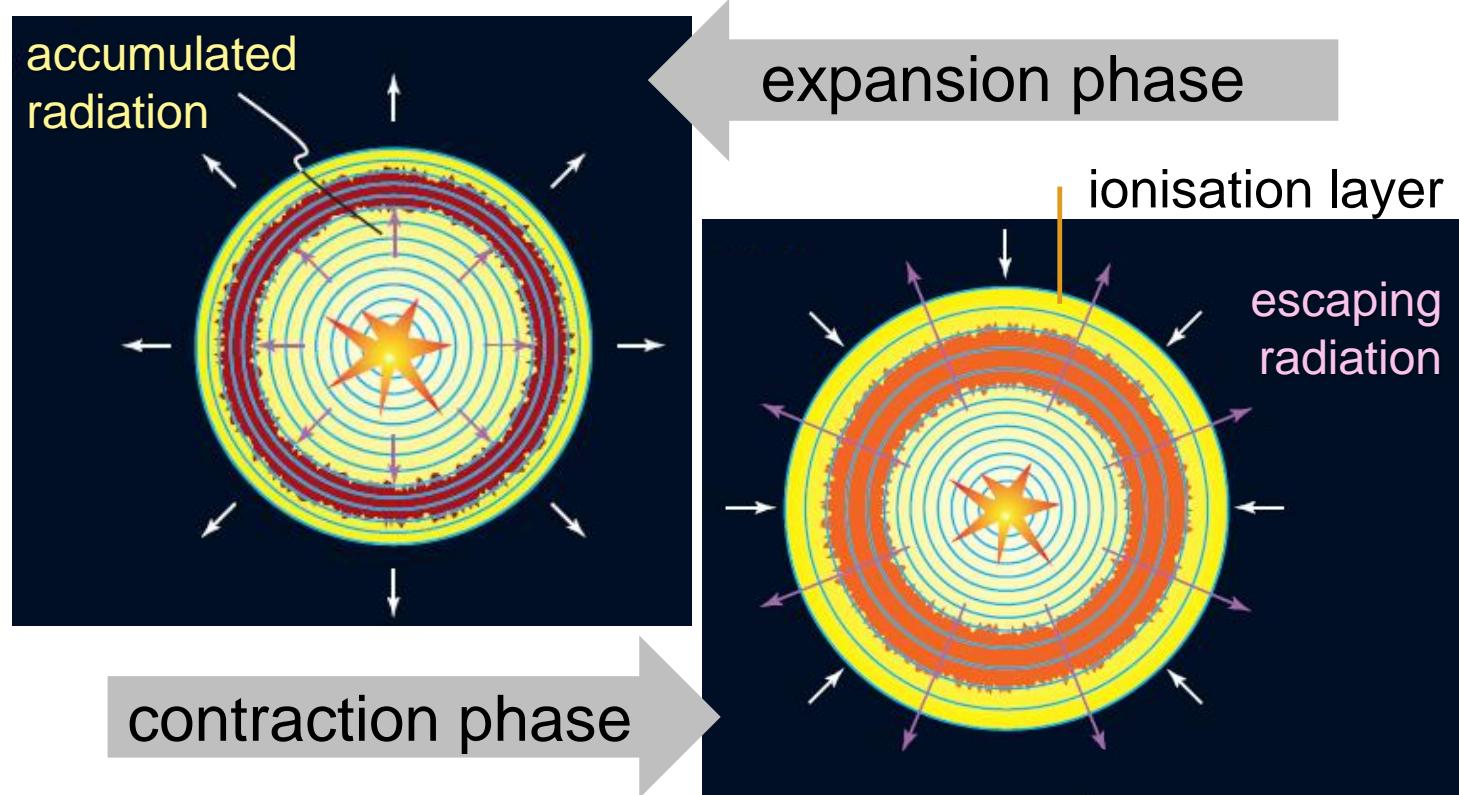
↳ increase of rad. pressure

↳ expansion of outer shell

**decreasing  $T$ :**

gravitational contraction

↳ recombination to  $He^+$



# Cepheids – cosmological standard candles

## ■ pulsation time scale of outer stellar shell

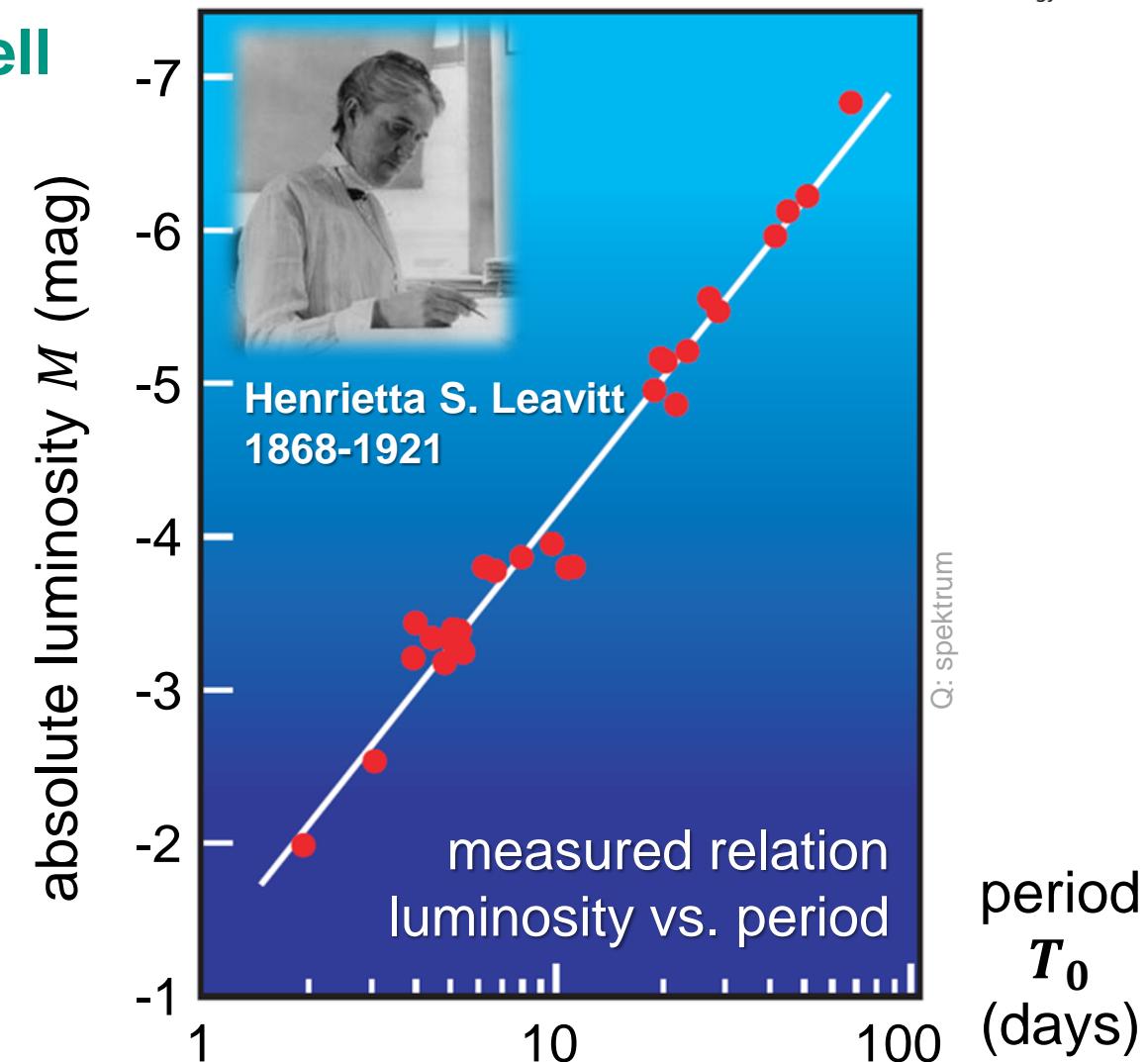
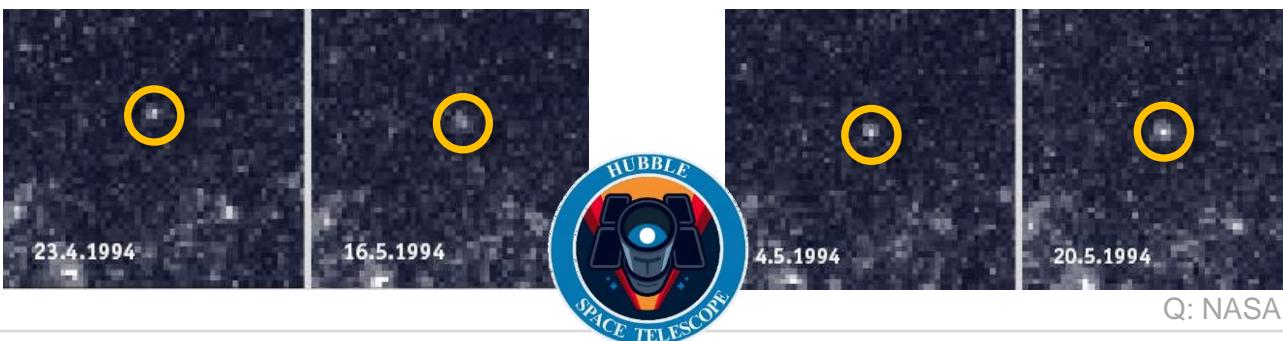
- very massive, very bright cepheids are pulsating more slowly, **period  $T_0 \sim L^{3/4}$**

## pulsation period - luminosity relation

$$M = -2.81 \cdot \log(T_0) - (1.43 \pm 0.1)$$

**$T_0$** : pulsation period (days)

**$M$** : absolute brightness (mag)



# Supernovae – cosmological standard candles

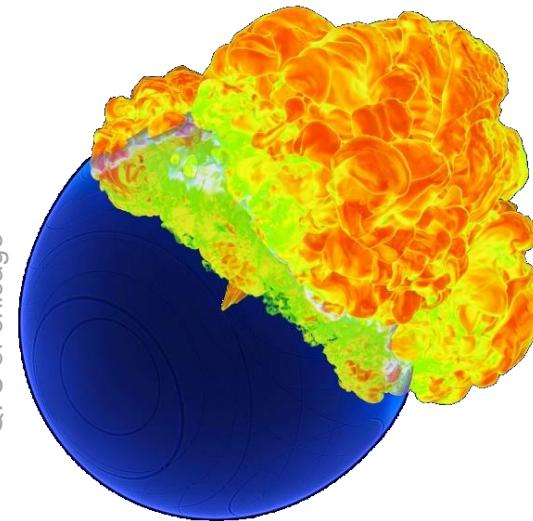
## ■ SN Ia: thermonuclear detonation\*

- a white dwarf reaches a mass of  $M \geq 1.4 M_{\odot}$



merger scenario

Q: U of chicago



or

accretion scenario

