

Introduction to Cosmology

Winter term 23/24

Lecture 1

Oct. 24, 2023



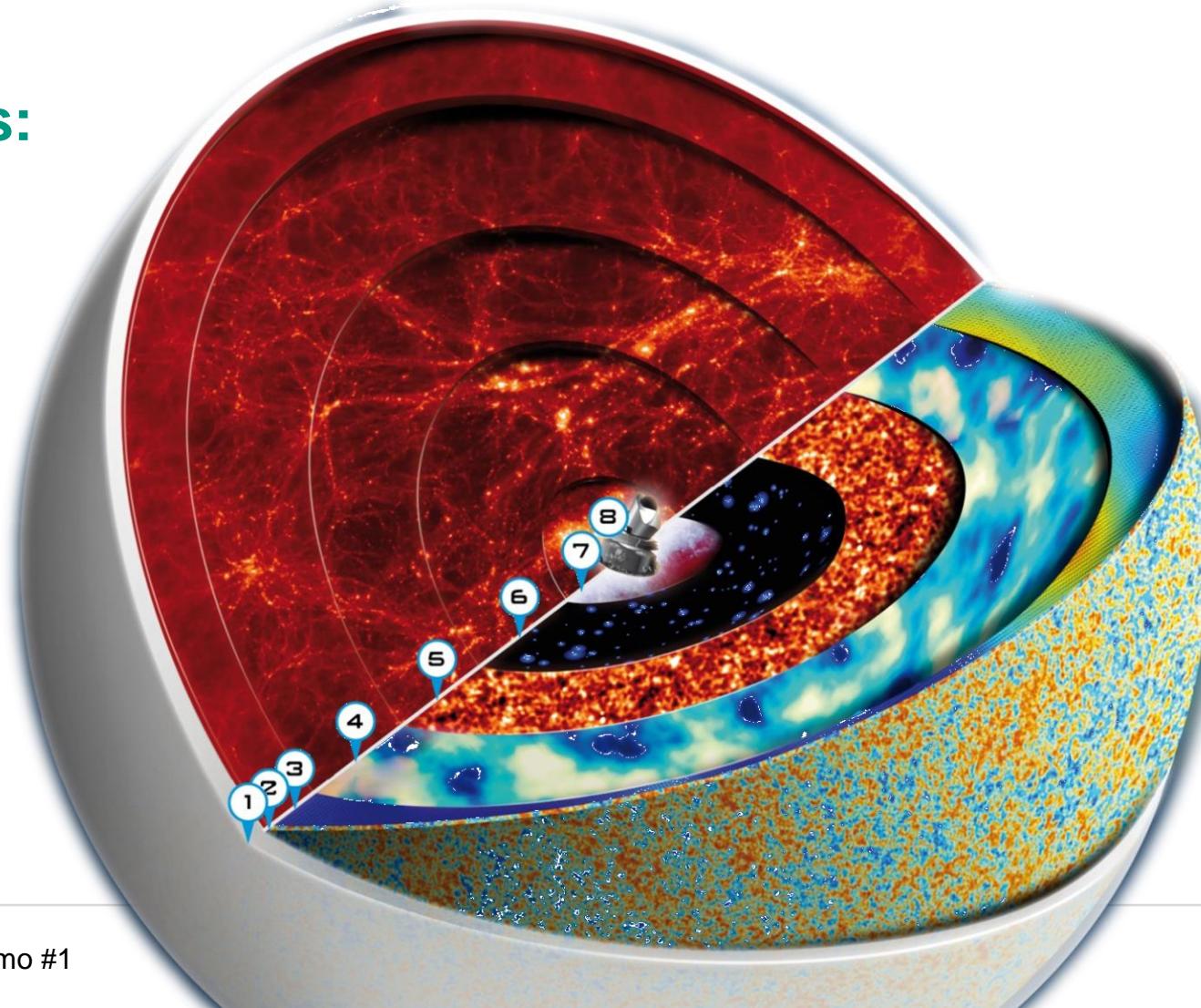
Evolution & Structure of the
Universe from the Big Bang
up to now

Cosmology – Definition

■ Evolution & Structure of the Universe from the Big Bang to now

important stopovers:

- 1 – Big Bang
- 2 – *CMB (3K)*
- 3 – reionisation
- 4 – dark ages
- 5 – first stars
- 6 – first galaxies
- 7 – Milky Way
- 8 – today



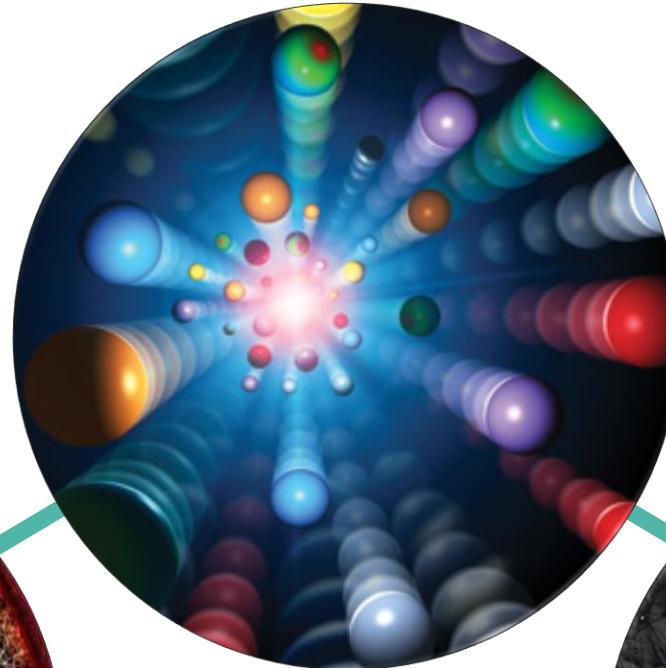
Cosmology – range of subjects

■ subjects of cosmology

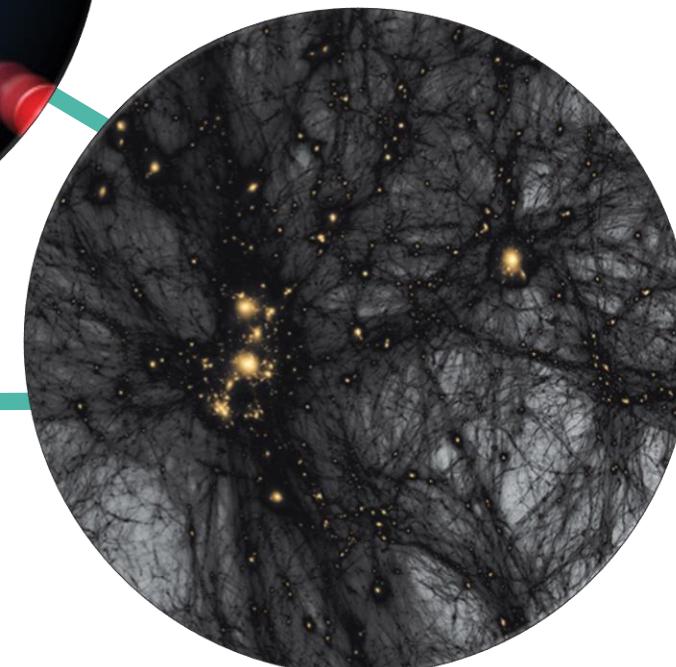
processes in



the Early Universe



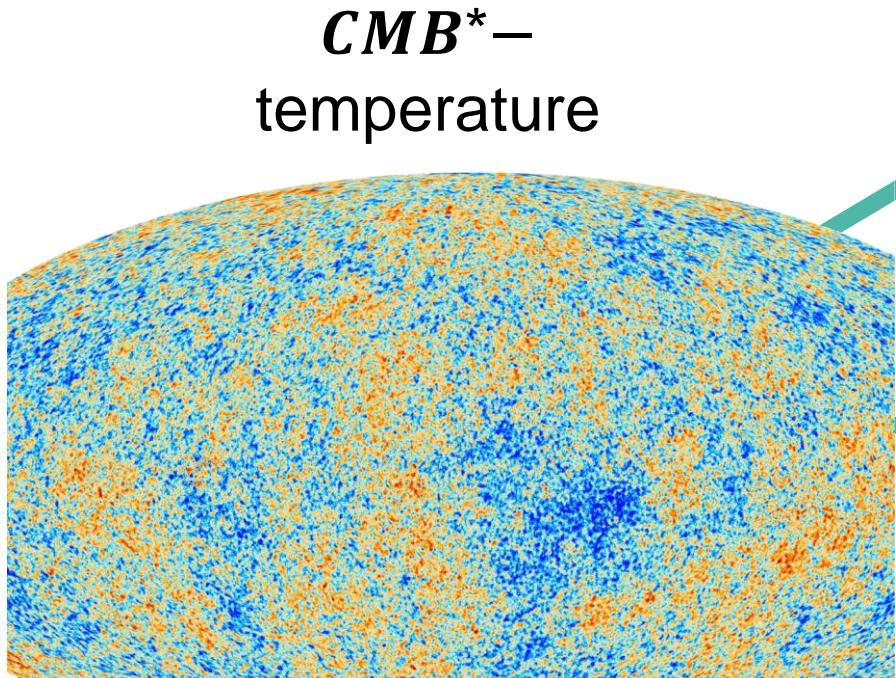
Dark
Universe



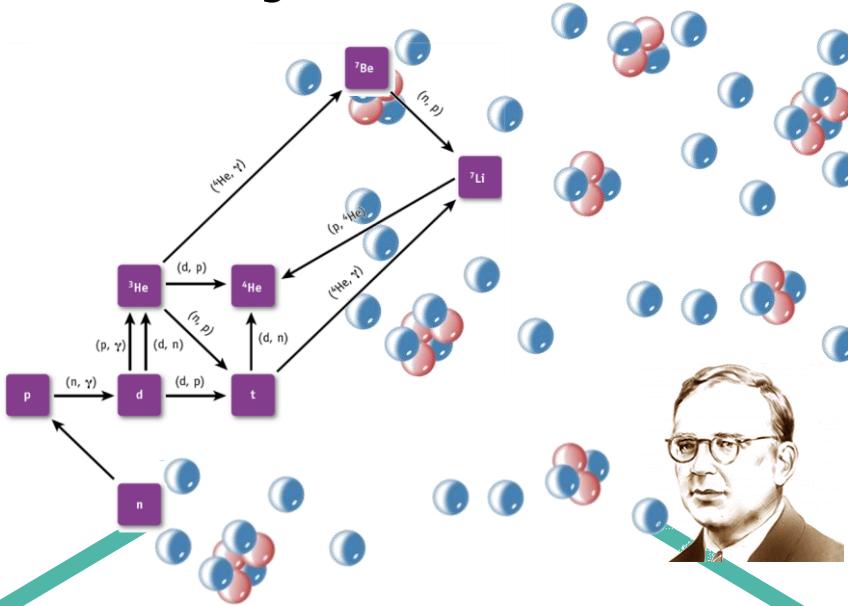
three pillars
of these lectures

Cosmology – range of subjects

■ example: thermal processes



*CMB**–
temperature



formation of
elements
during Big Bang

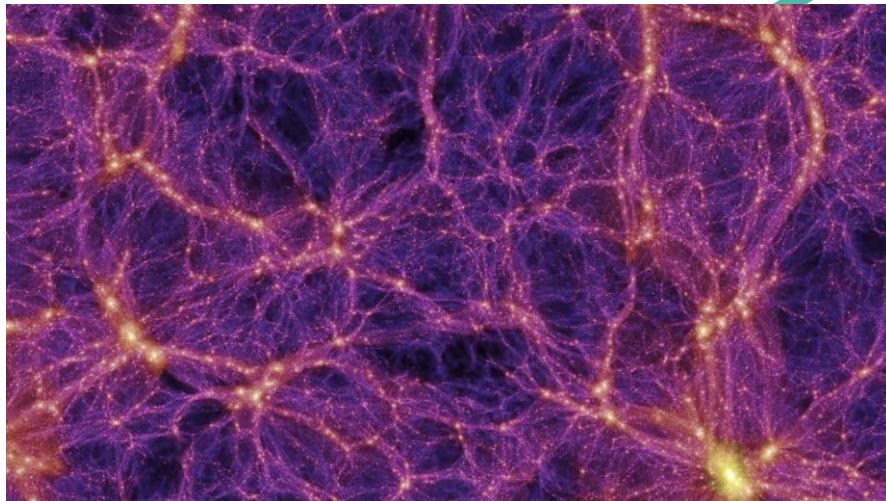


neutrino
properties

Cosmology – range of subjects

- example:
Dark Matter (DM)

DM in
structure formation



DM – particle candidates:
HDM*, **WDM****, **CDM*****

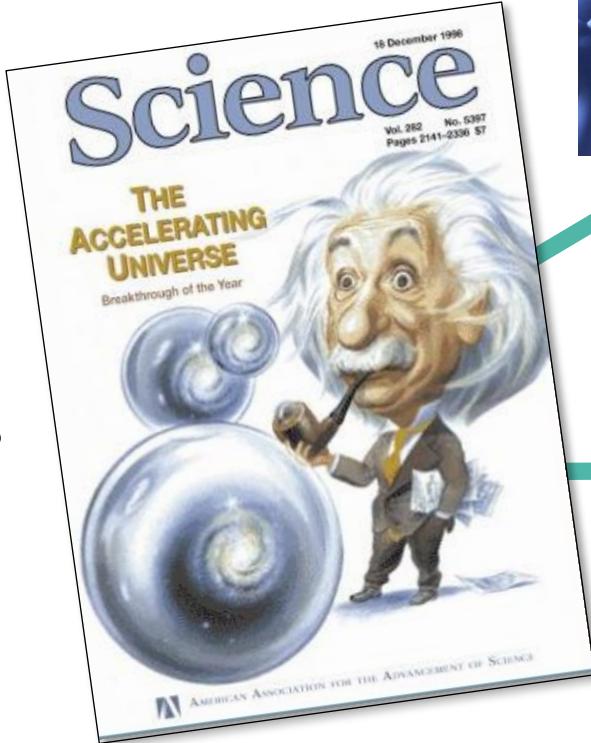


galactic
DM –
halos

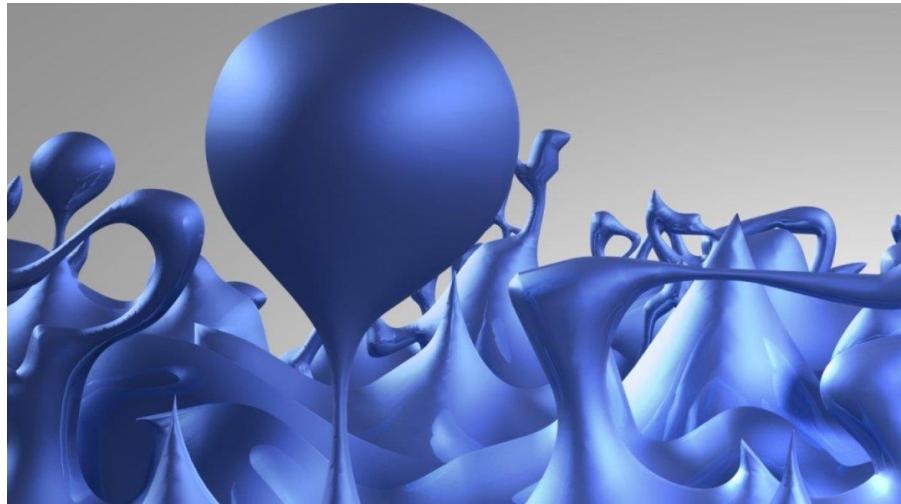
Cosmology – range of subjects

■ example:

Dark Energy (DE)



evidences
for **DE**



nature of **DE**:
**cosmological
constant ?**

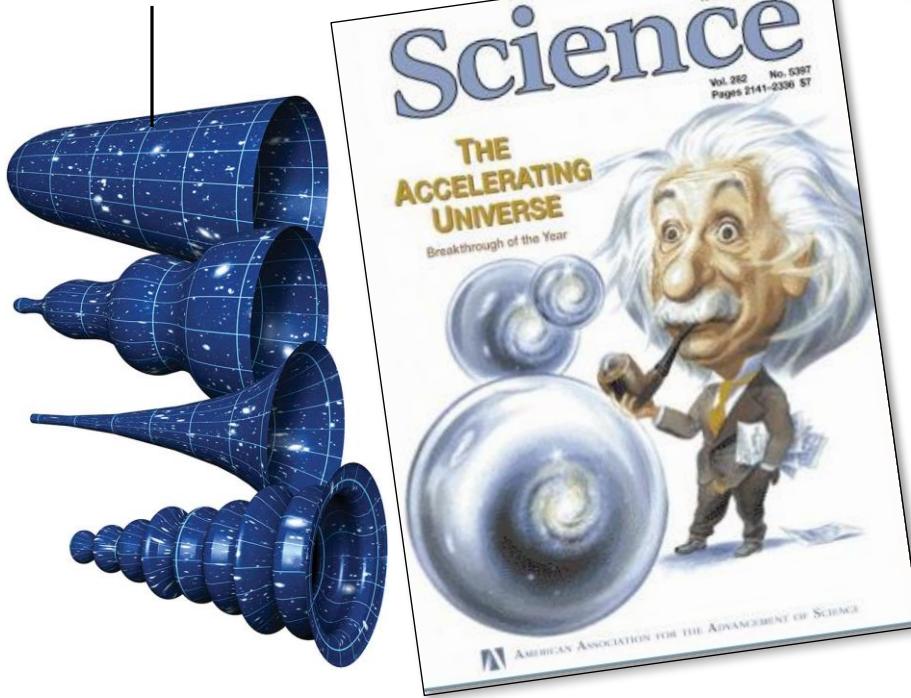


DE &
expansion
rate of the
universe

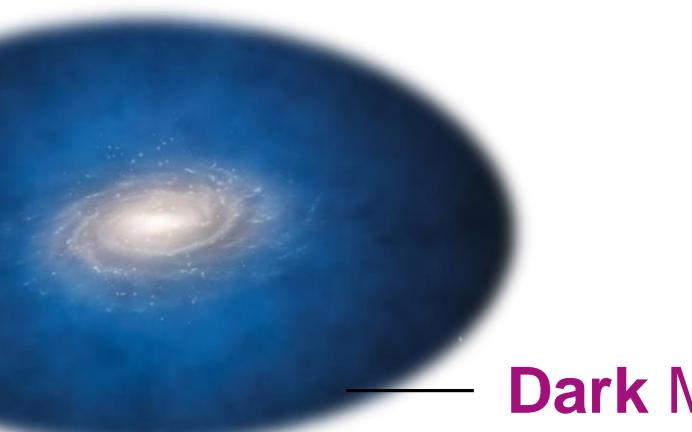
Cosmology – new concepts

■ classification

Anti–gravity



Dark Matter



Bachelor
Studies



gravity



nuclear physics
thermodynamics
optics

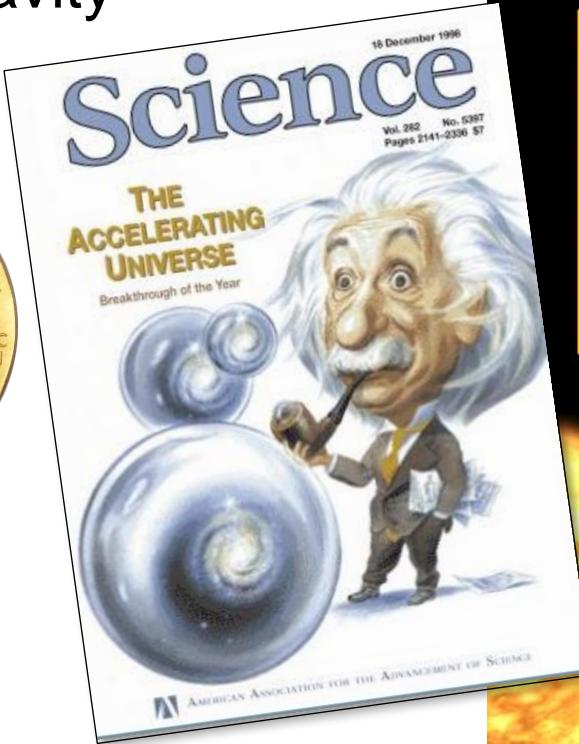
condensed
matter, atoms,
molecules

Cosmology – modern observations

■ Nobel Prize 2011

*„for the discovery of the **accelerating expansion of the Universe** through observations of distant supernovae“*

Anti–gravity



Saul Perlmutter



Adam G. Riess



Brian P. Schmidt

Cosmology – modern theories

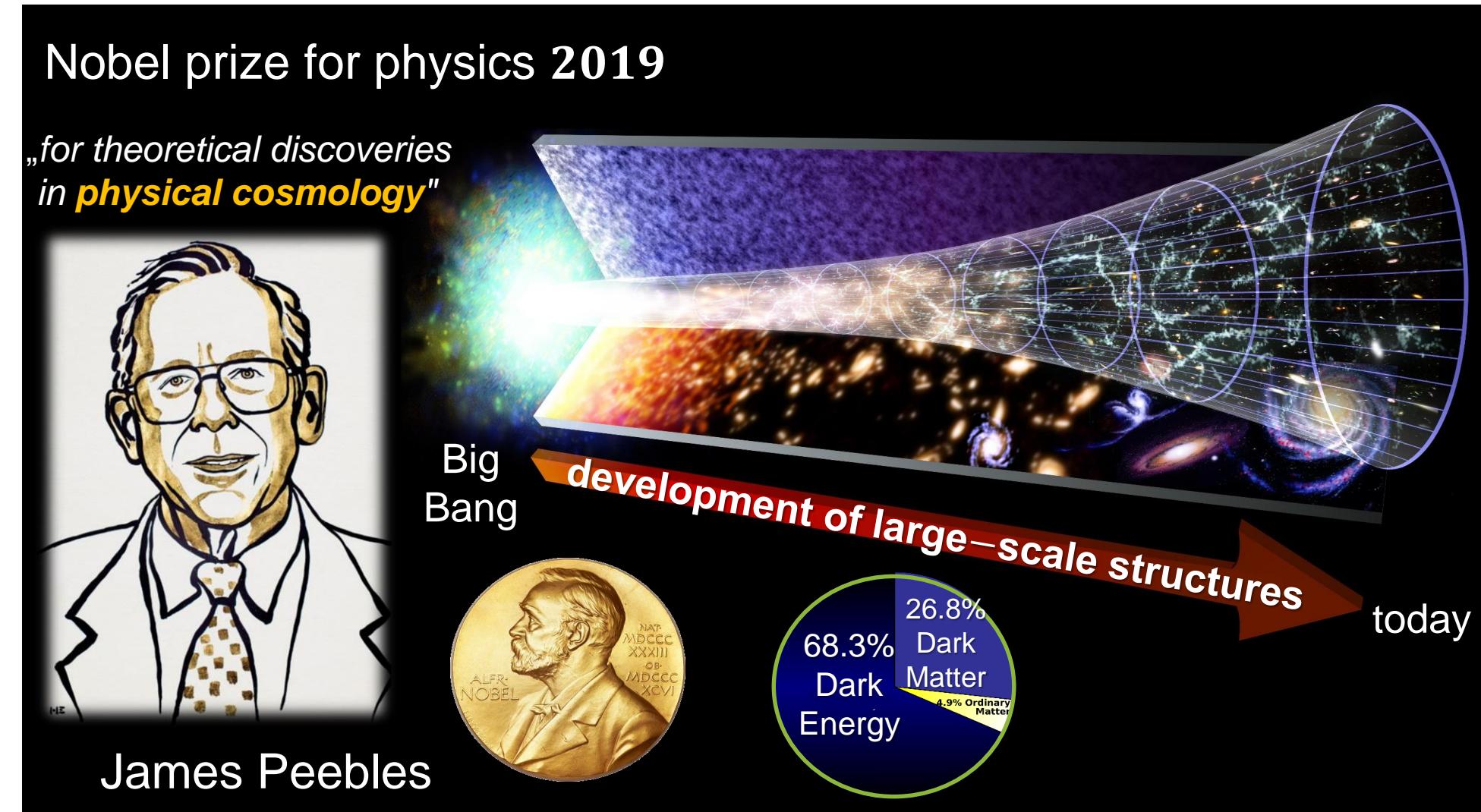
■ Nobel Prize 2019

structure formation



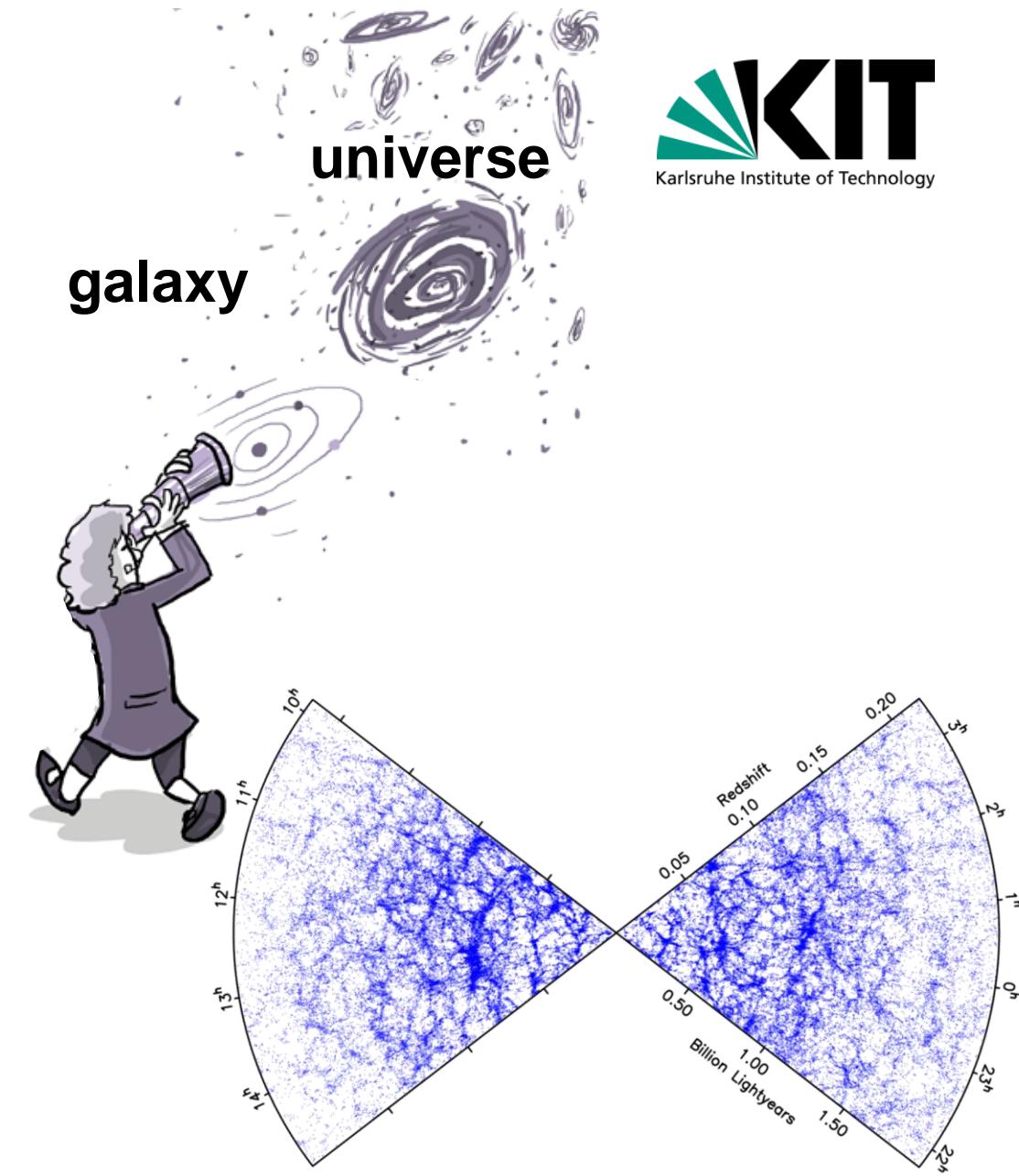
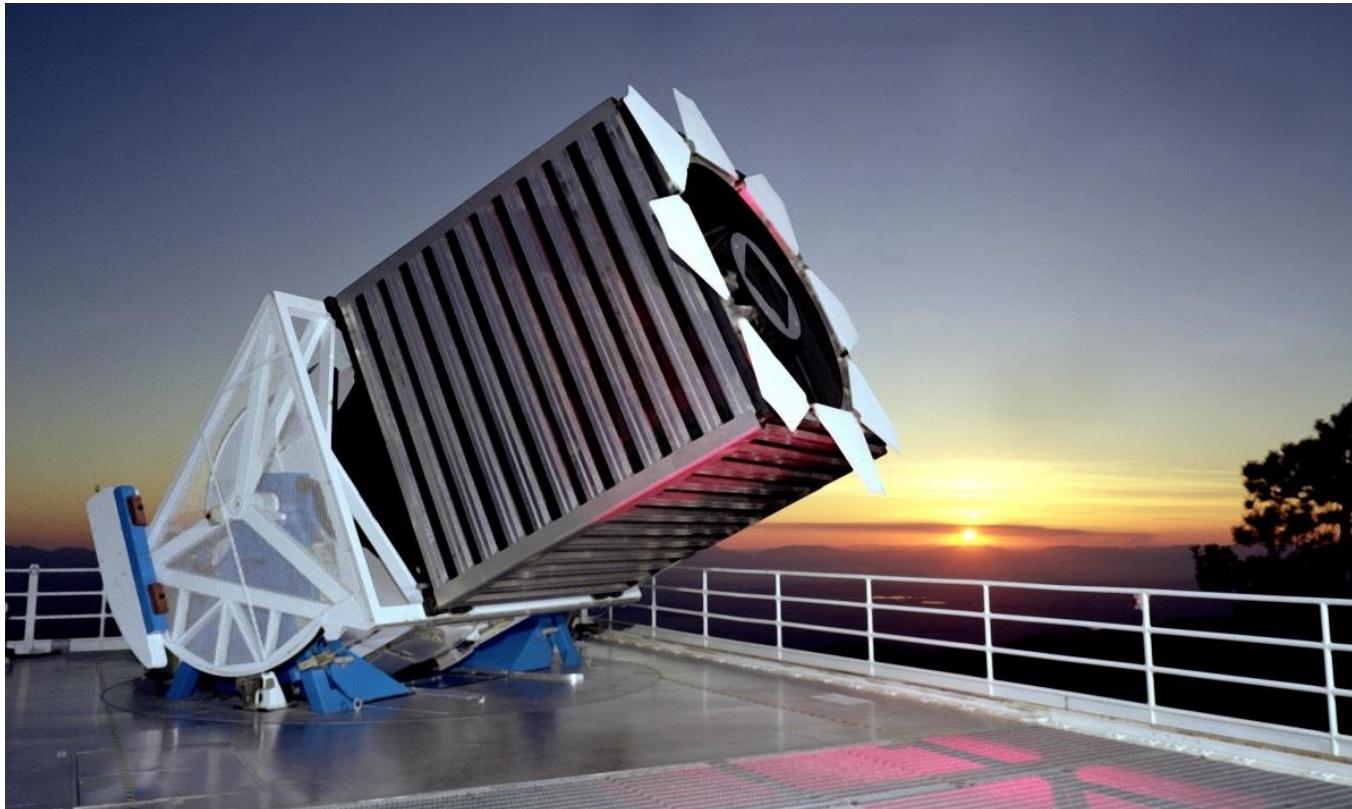
50 %

$$\delta(\vec{r}) = \frac{\rho(\vec{r}) - \langle \rho \rangle}{\langle \rho \rangle}$$



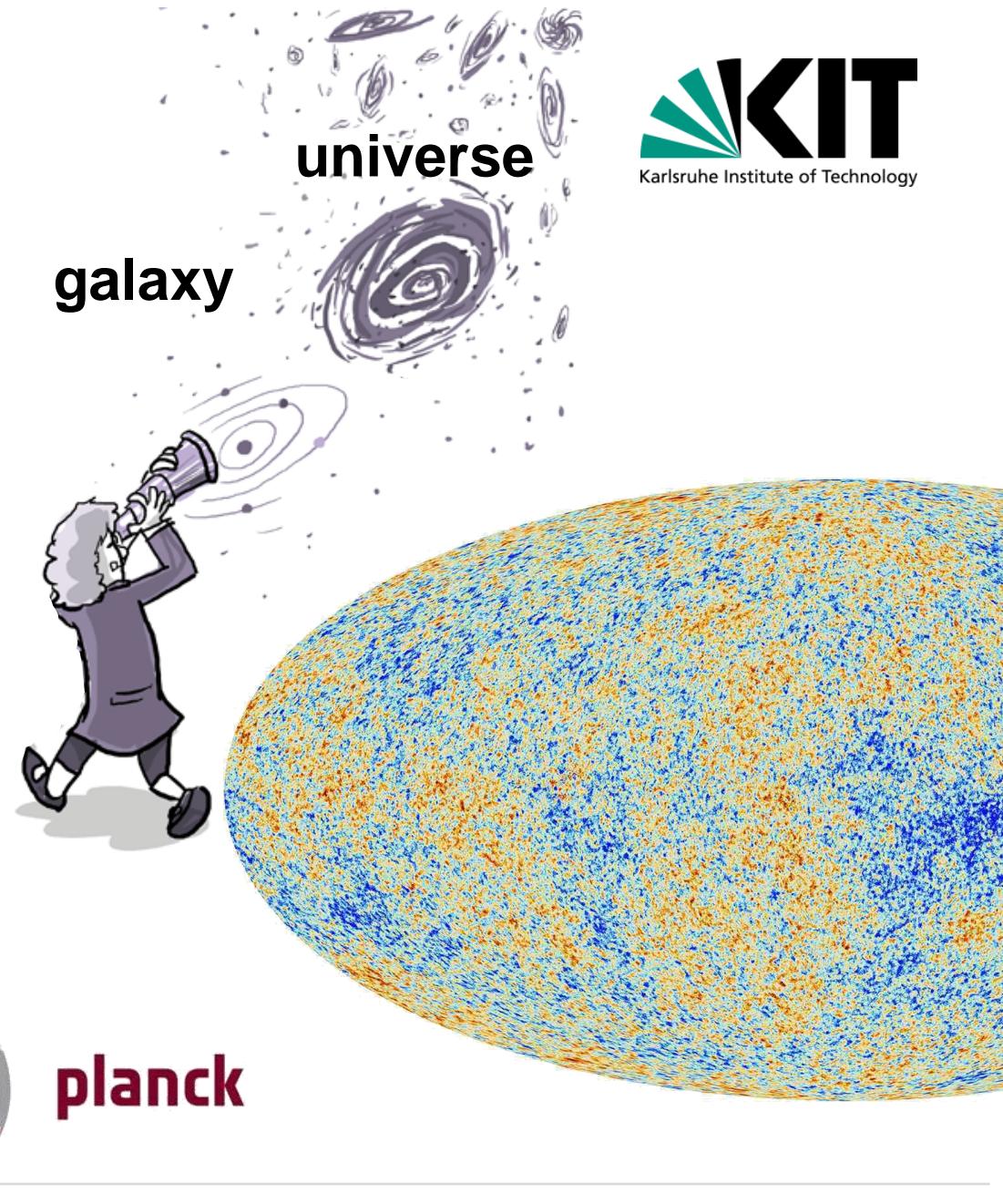
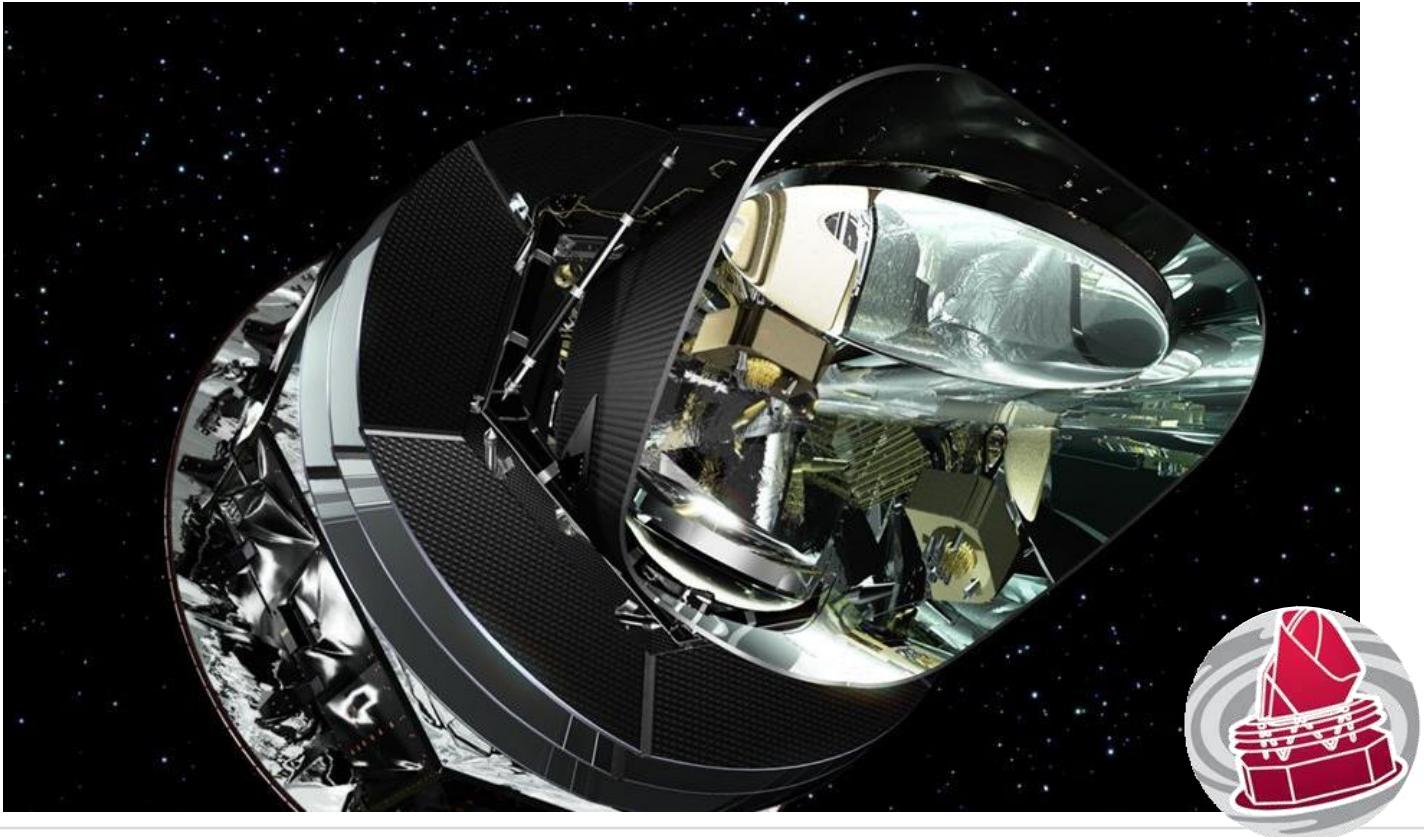
Cosmology – observations

- example: **galaxy redshift surveys**



Cosmology – observations

- example: temperature fluctuations of the *CMB* (Cosmic *Microwave Background* radiation)



Cosmology – open questions

- what is the intrinsic nature of Dark Matter & Dark Energy ?



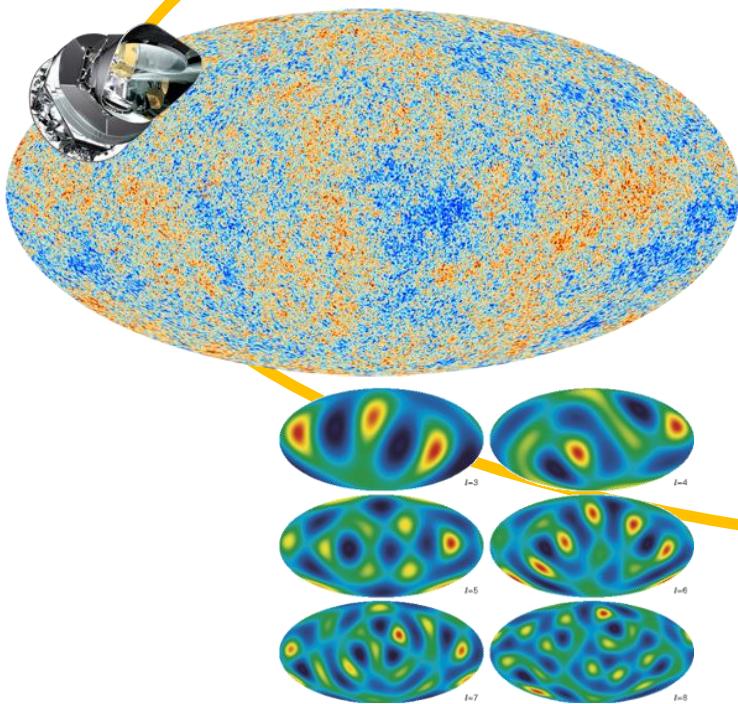
I can learn the following in this lecture series:

BREAKING
NEWS



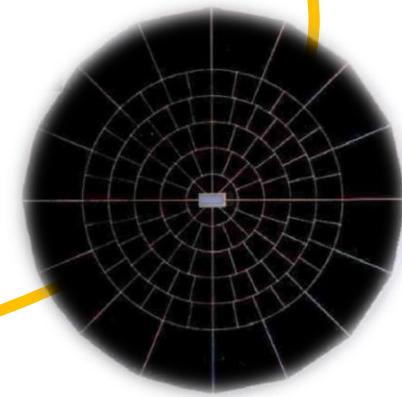
$$\left(\frac{\dot{H}(t)}{H(t)}\right)^2 \sim 1 + \frac{7\Delta N_\nu}{43}$$

...new tools for discoveries...



hands-on
TRAINING

...modern analysis methods...



...advanced experimental methods...



OUTLINE

1. Introduction

1.1 fundamental principles

1.2 distance ladders for the Universe

2. Expanding Universe

2.1 Hubble Expansion

2.2 Friedmann–Lemaître equations

3. Thermal Universe

- 3.1 **primordial nucleosynthesis (*BBN*)**
 the first three minutes
- 3.2 **cosmic microwave background radiation – essentials:**
 formation, black body radiation, fluctuations
- 3.3 **cosmic microwave background radiation – experiments:**
 COBE, WMAP & Planck
- 3.4 **cosmological Λ CDM concordance model**

4. Structure Formation in the Universe

4.1 **Inflation & Early Universe**

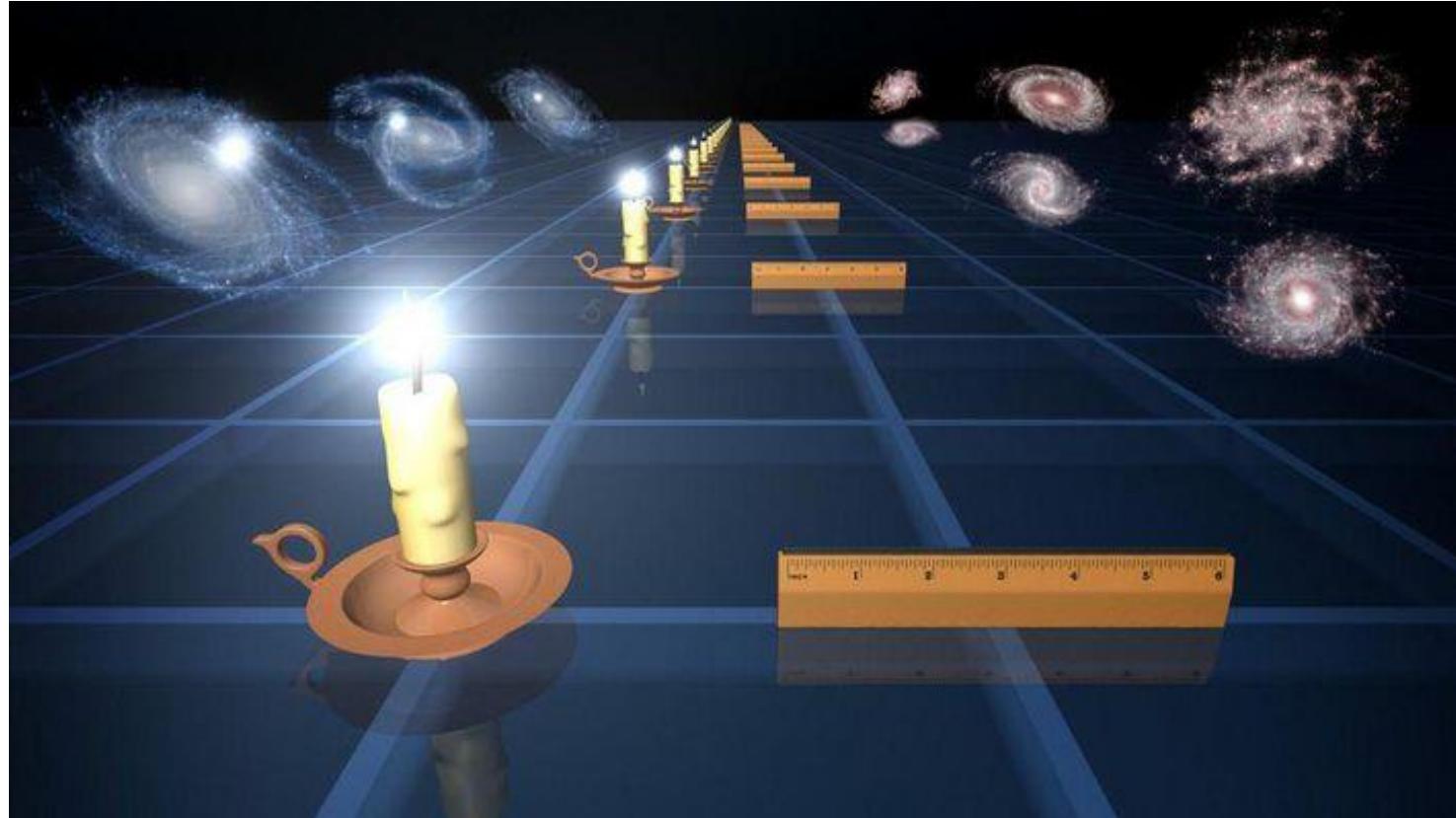
4.2 ***BAO – Baryon Acoustic Oscillations :***
formation & relevance in the present universe

4.3 **Large-Scale Galaxy Surveys:**
the matter power spectrum

4.4 **Evolution of Large-Scale Structures:**
Hot, Warm & Cold Dark Matter

5. Dark Universe

- 5.1 **Evidences for Dark Matter:**
from *Vera Rubin & Fritz Zwicky* to the Bullet–Cluster
- 5.2 **Gravitational Lenses for the Dark Universe:**
strong & weak lensing
- 5.3 **Dark Matter Halos: the *NFW* – Profile**
- 5.4 **Dark Energy:**
the future evolution of the Universe



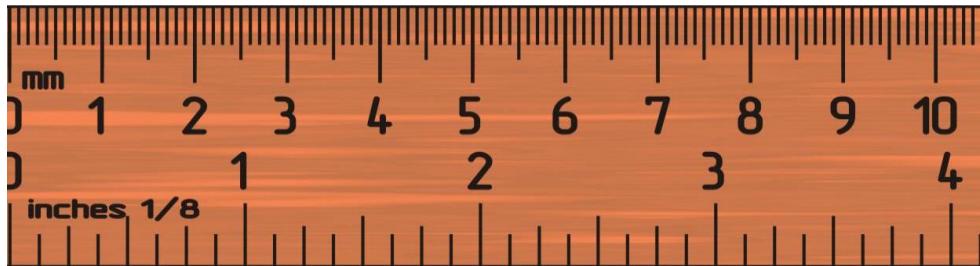
Q: NASA,S. Harris

CHAPTER 1 – INTRODUCTION

cosmological distances and time scales

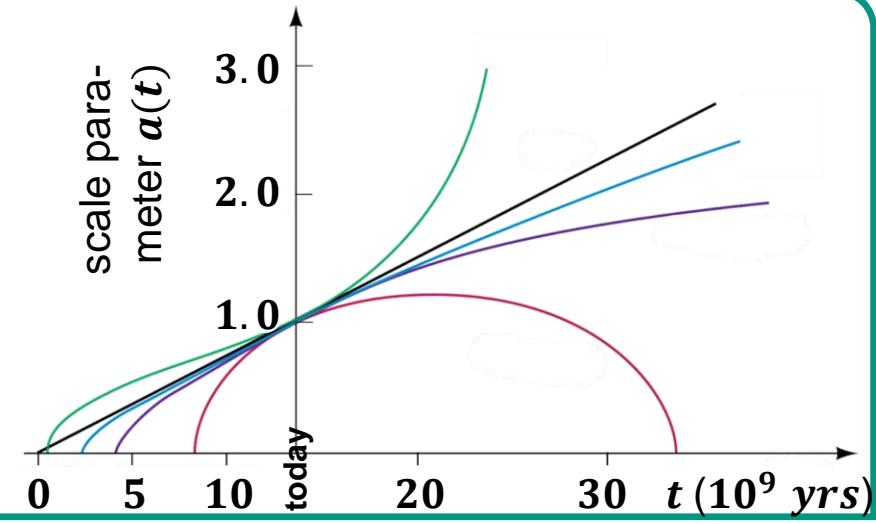
■ Measurement of distances

- cosmological standard candles up to $D = ?$

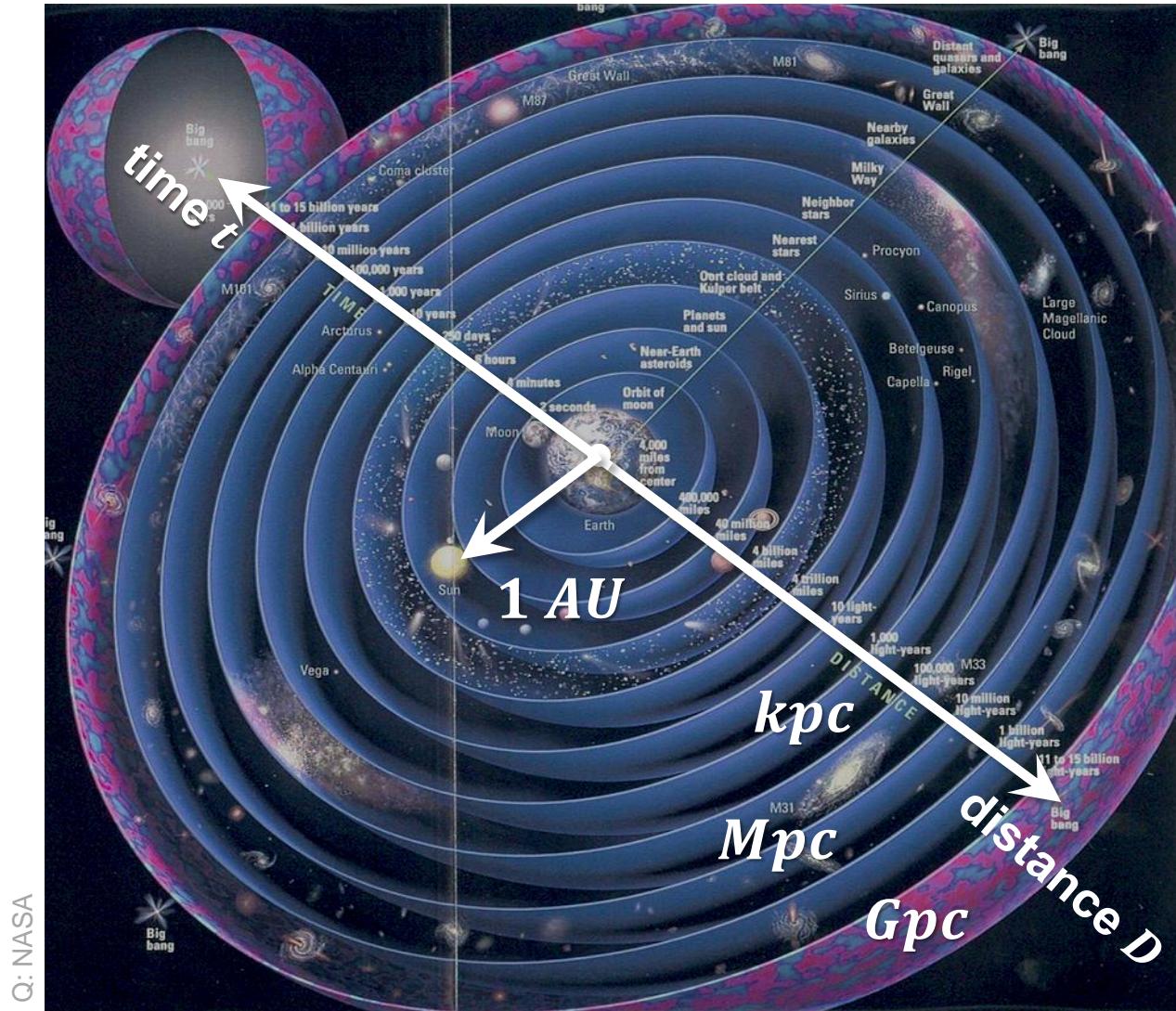


■ Measurement of cosmological time scales

- cosmological standard time scale up to $t = ?$



Cosmology: typical time – and distance – scales



astronomical scales	
1 AU	$1.496 \times 10^{11} \text{ m}$
1 ly	$9.461 \times 10^{15} \text{ m}$ $= 63\,240 \text{ AU}$
	$= 0.3066 \text{ pc}$
1 pc	$3.086 \times 10^{16} \text{ m}$ $= 2.06 \times 10^5 \text{ AU}$ $= 3.262 \text{ ly}$

AU: Astronomical Unit

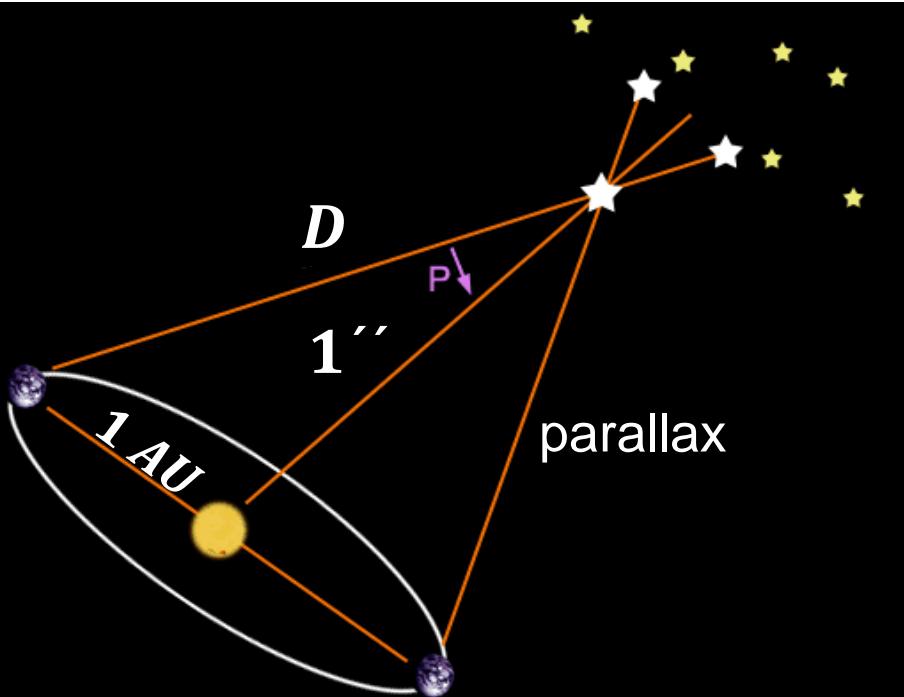
major semi-axis of Earth around Sun

ly: light-year light trajectory in $t = 1 \text{ yr}$

pc: parsec parallax of 1 arc - sec

Cosmology: distance – scale pc

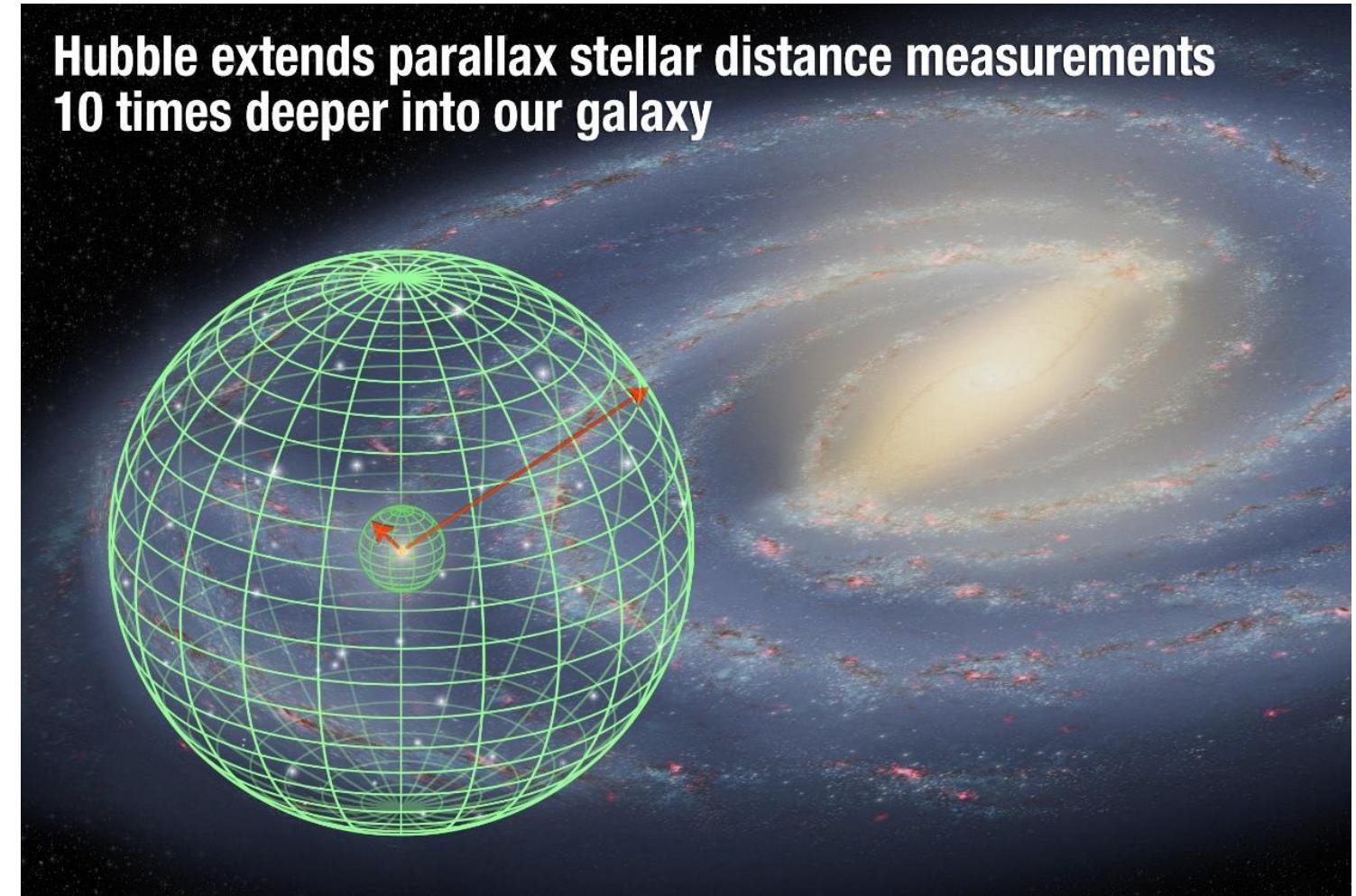
definition of 'parallax'



parallax:

$$\begin{aligned}1 \text{ pc} &= 1 \text{ AU} \text{ subtends to } 1'' \\&= 1 \text{ AU} \cdot 180 \cdot (3600 / \pi)\end{aligned}$$

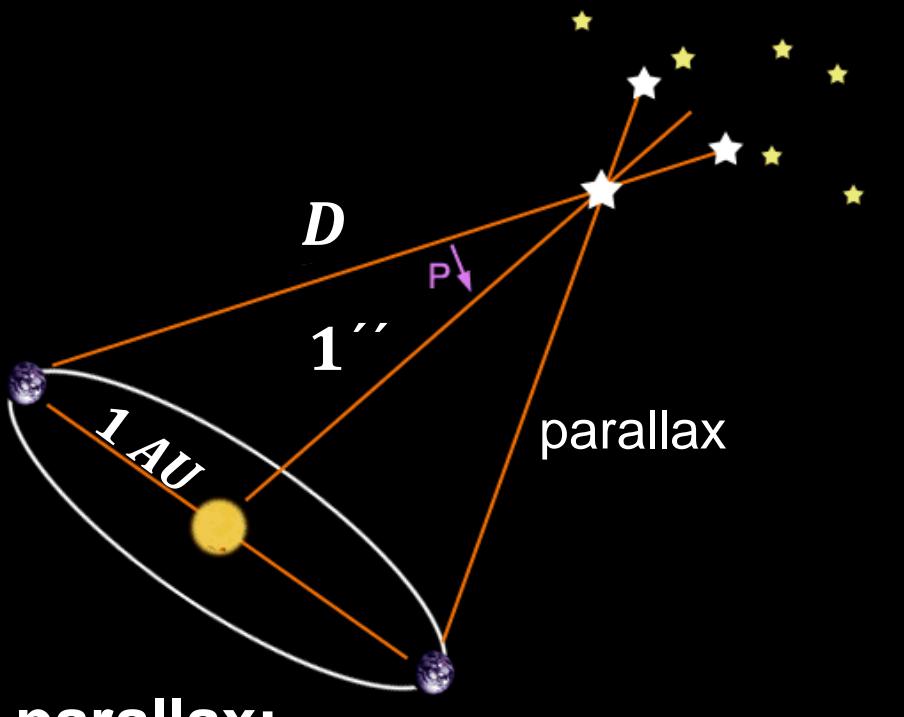
Hubble extends parallax stellar distance measurements
10 times deeper into our galaxy



2014 – parallax measurements now up to 3 – 4 kpc

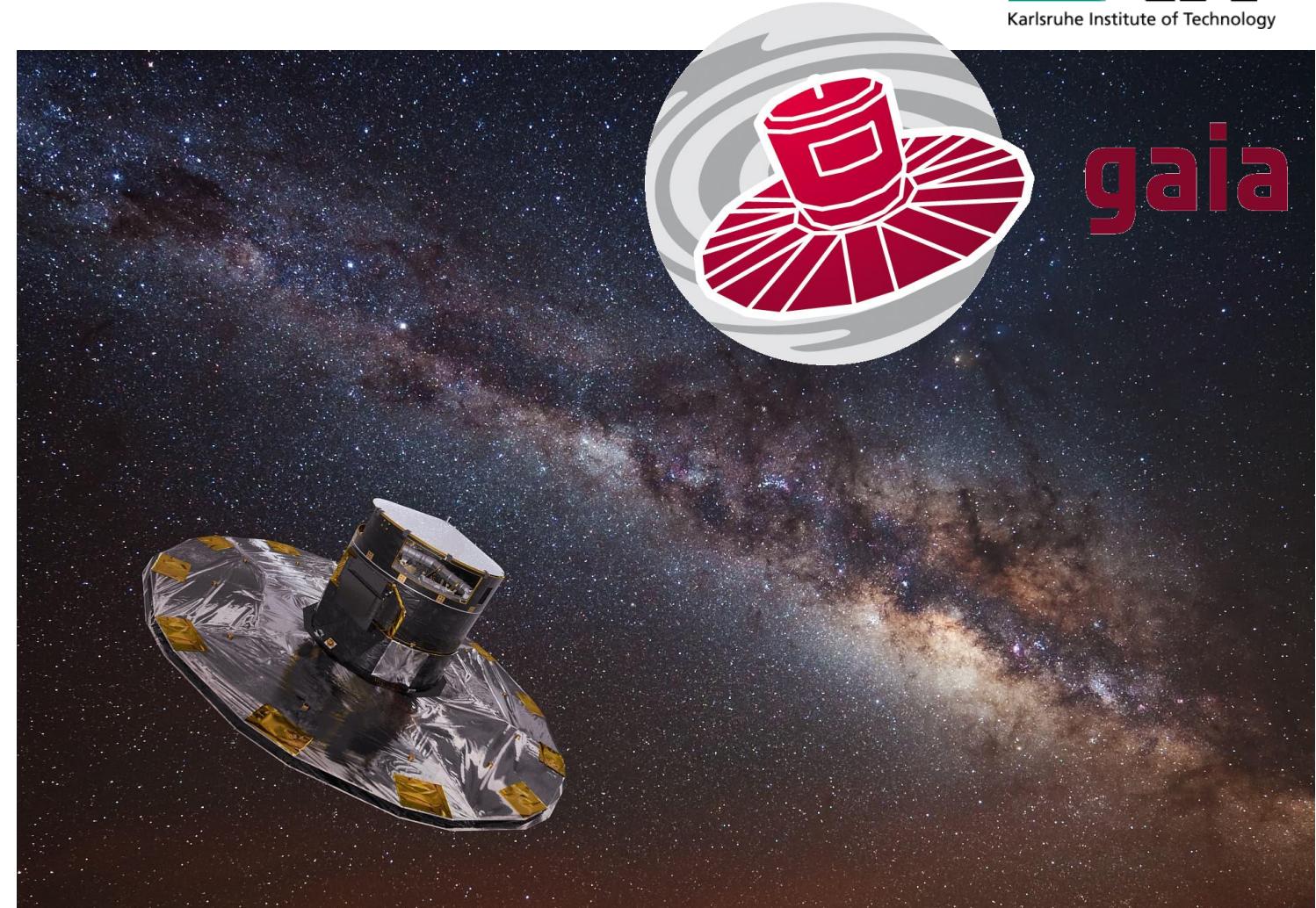
Cosmology: distances & *GAIA* observatory (ESA)

definition of 'parallax'



parallax:

$$\begin{aligned}1 \text{ pc} &= 1 \text{ AU} \text{ subtends to } 1'' \\&= 1 \text{ AU} \cdot 180 \cdot (3600 / \pi)\end{aligned}$$



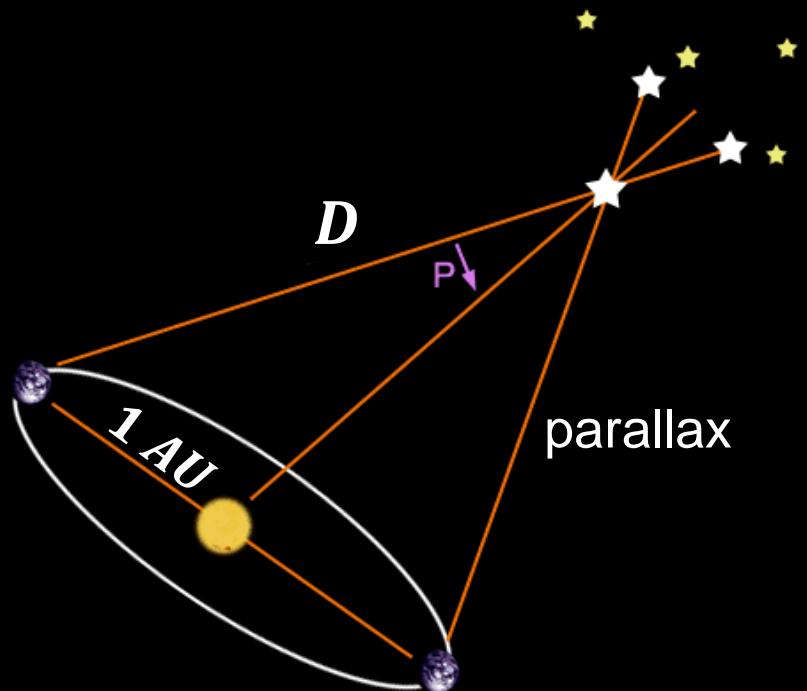
Q: ESA

measurements of *GAIA* with μas – precision*

**GAIA DR 3* = 3. Data Release (*June 2022*)

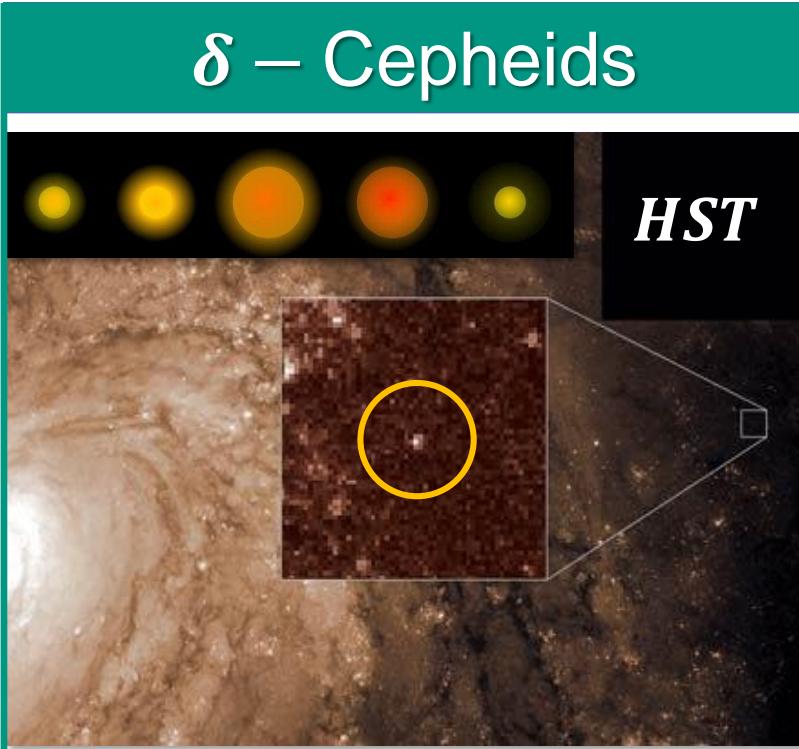
Cosmology: the 'classical' distance ladder

parallax method



Parallax method: reach to
 $D = \text{few kpc}$ (Milky Way)

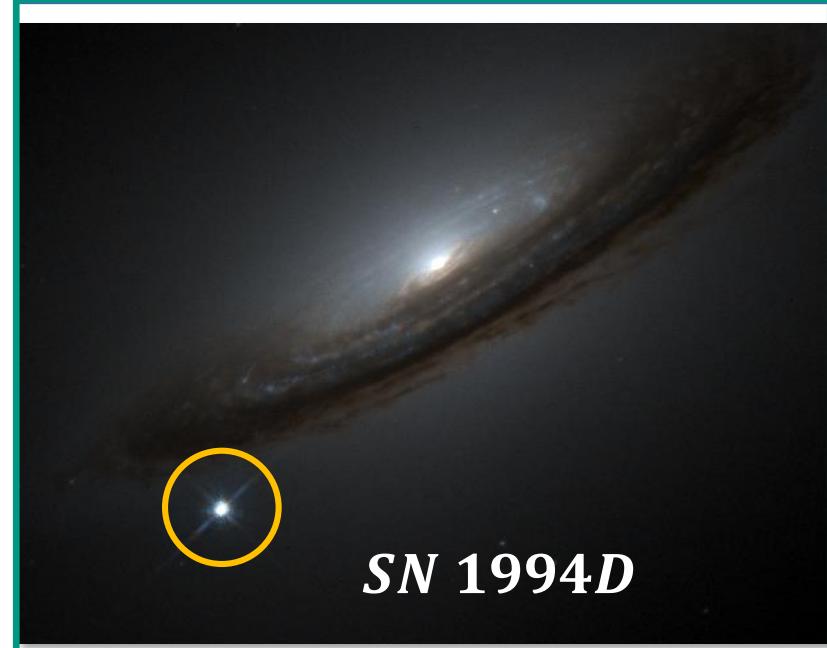
δ – Cepheids



δ – Cepheids: absolute
luminosity $L_{abs} \sim 10^4 L_\odot$
 $D = 1 \text{ kpc} \dots 50 \text{ Mpc}$

luminosity of the sun: L_\odot

$SN - Ia -$ brightness



Supernovae Type Ia:
luminosity $L_{abs} \sim 10^9 L_\odot$
 $D = 30 \text{ Mpc} \dots 3 \text{ Gpc}$

Brightness – definition in astronomy

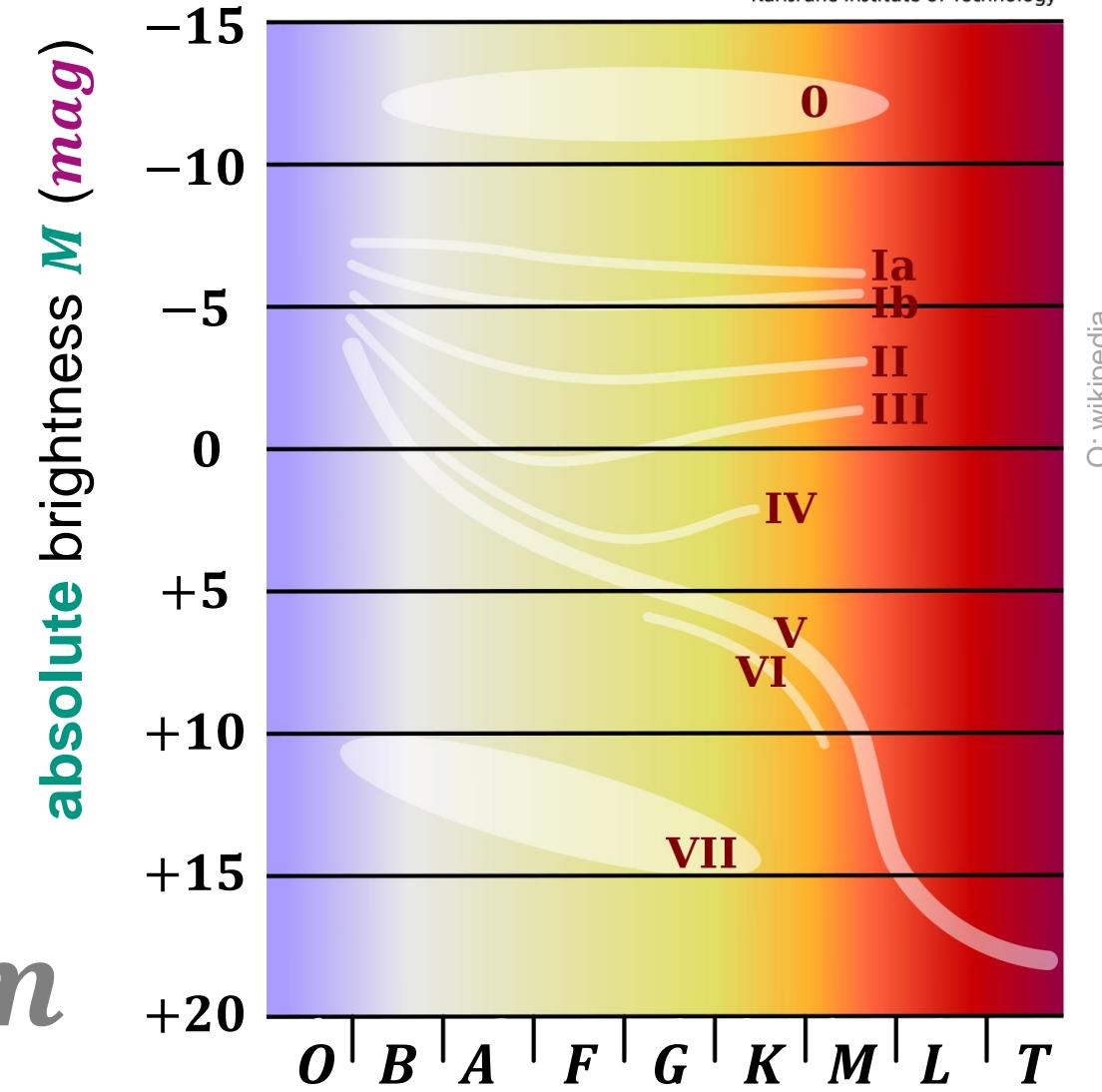
■ absolute & relative brightness

- brightness of objects is measured in **magnitudes (*mag*)** = logarithmic scale
- **absolute** brightness ***M***:
defined at unit distance $r_0 = 10 \text{ pc}$
- **apparent** brightness ***m***:
object as it appears **here on Earth**



$$r_0 = 10 \text{ pc} \rightarrow M$$

$$r = xx \text{ pc} \quad // \quad m$$



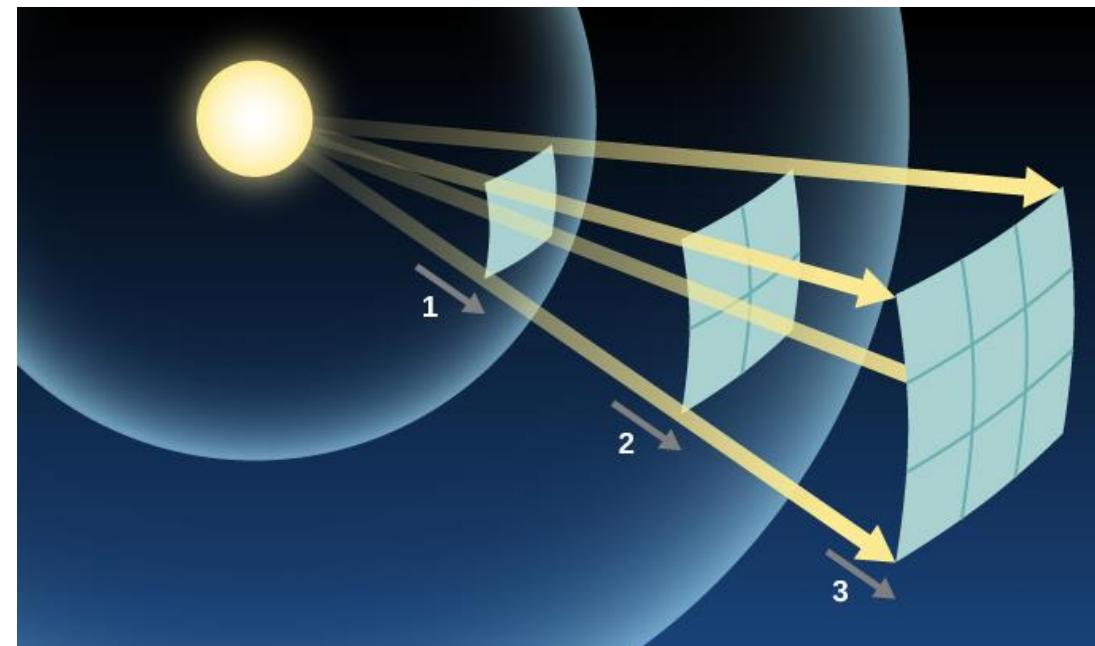
Brightness – definition in astronomy

■ absolute & apparent brightness: magnitude

- reference: $m \equiv 0$ is defined for the nearby star **Wega** (α Lyrae)
- **mag** = logarithmic unit \Leftrightarrow difference of **5 mag** \equiv **factor 100** in brightness
per magnitude: **factor** $= \sqrt[5]{100} = 2.512$
- **Distance modulus $m - M$:**

$$m - M = 5 \cdot \log \left(\frac{r}{r_0} \right)$$

quadratic
distance law

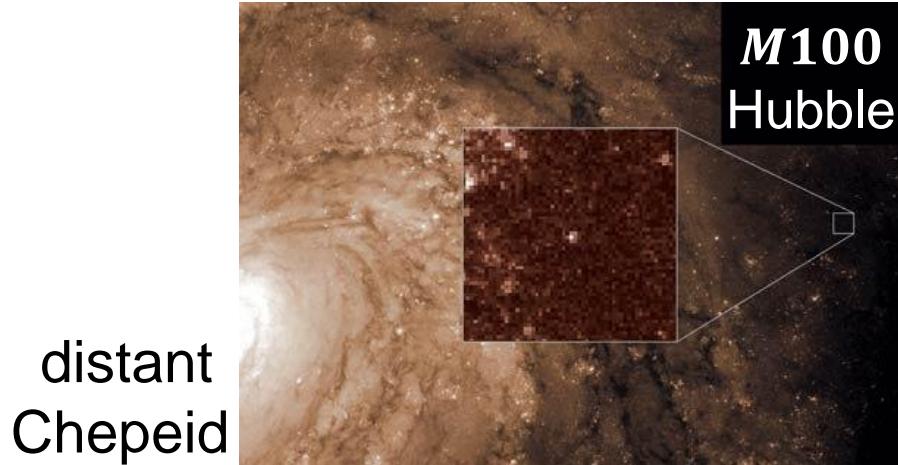


Q: BCcampus

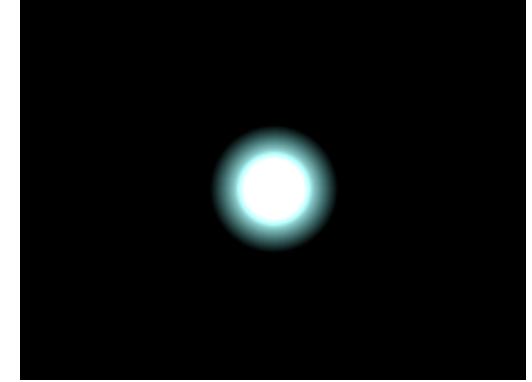
Cepheids – cosmological standard candles #1

■ Cepheids:

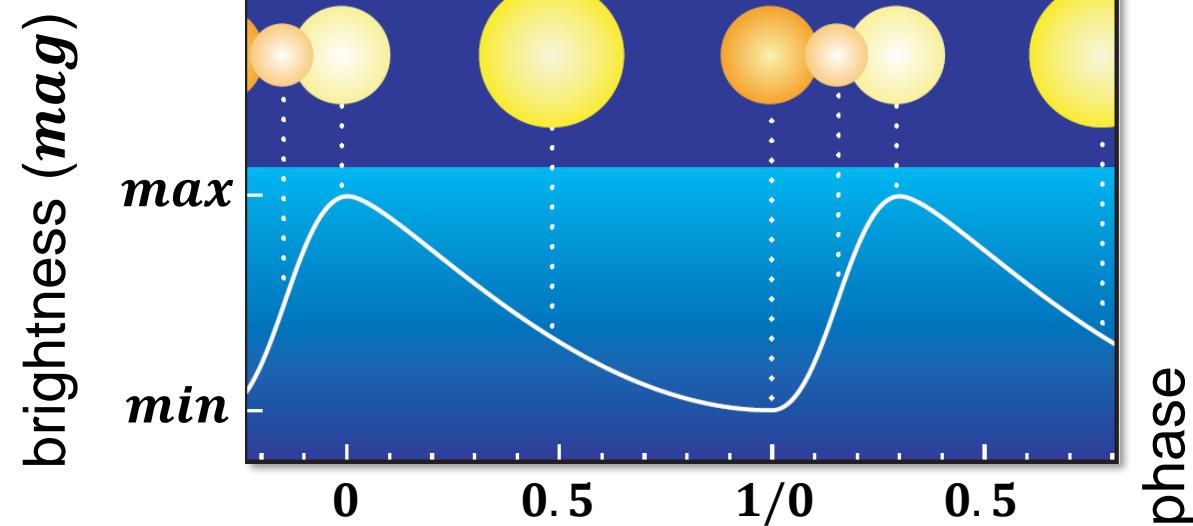
- giant stars with radial pulsations ('super-giants')
- allows to determine **absolute brightness from period T_0**
- mass range: $M = 5 \dots 15 M_\odot$ (\Rightarrow very rare stars)
- spectral class: F, G (white, yellow)
- brightness class*: Ia, II ($M_V = -2 \dots -7 \text{ mag}$)
- period: $T_0 < 100 \text{ days}$



period of a δ – Cepheid



Q: NASA



M_V = visual brightness

Cepheids – cosmological standard candles #1

■ ‘Kappa mechanism’: the underlying cause of radial pulsation

changes in the opacity $\kappa(p, T)$ of a specific stellar layer

- key: hot stellar core with an **He – ionisation layer** of He^{++} & He^+ – ions

- cycle of stellar pulsation:

increasing T :

more He^{++} & free electrons

↳ larger opacity

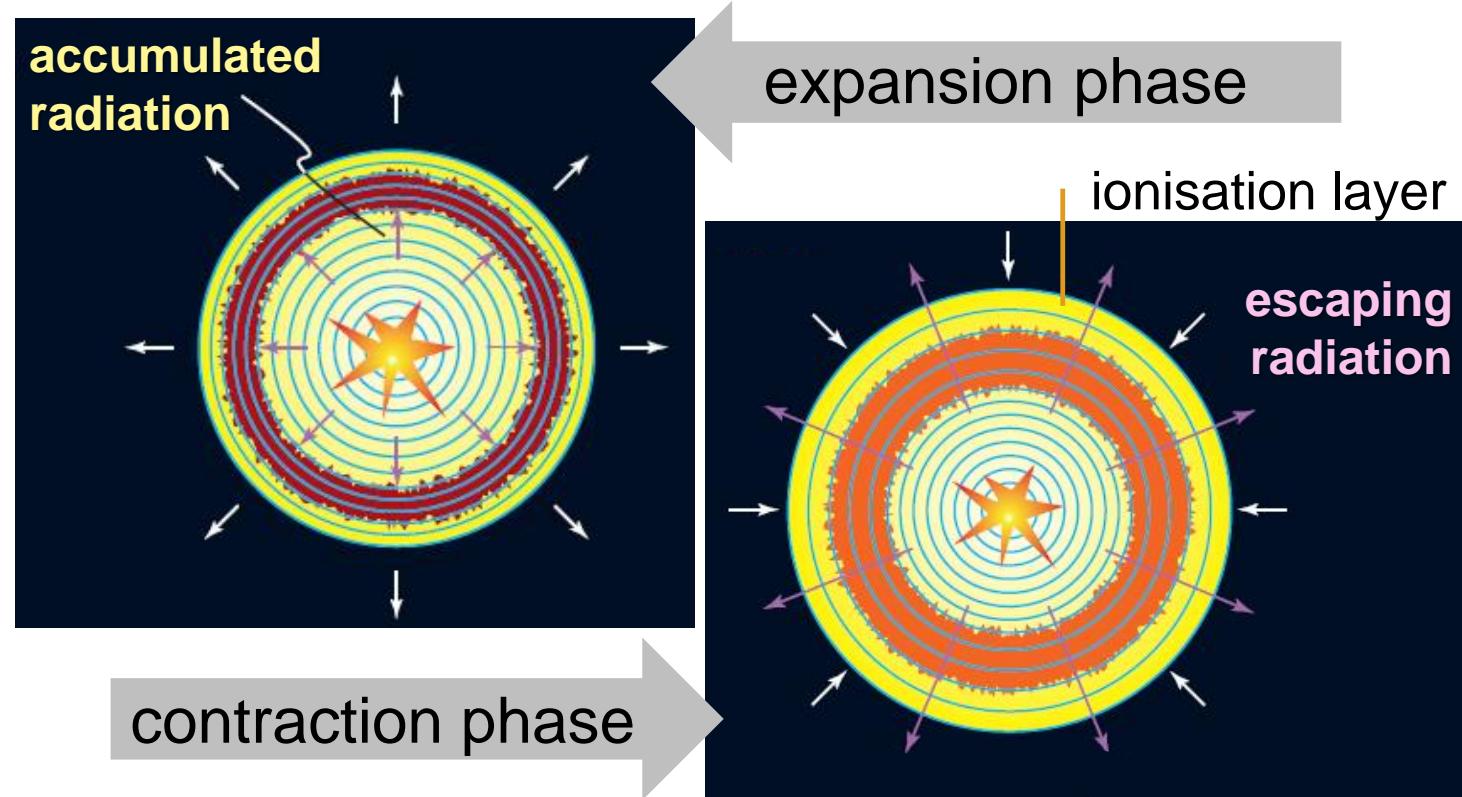
↳ increase of rad. pressure

↳ expansion of outer shell

decreasing T :

gravitational contraction

↳ recombination to He^+



Cepheids – cosmological standard candles #1

■ pulsation time scale of outer stellar shell

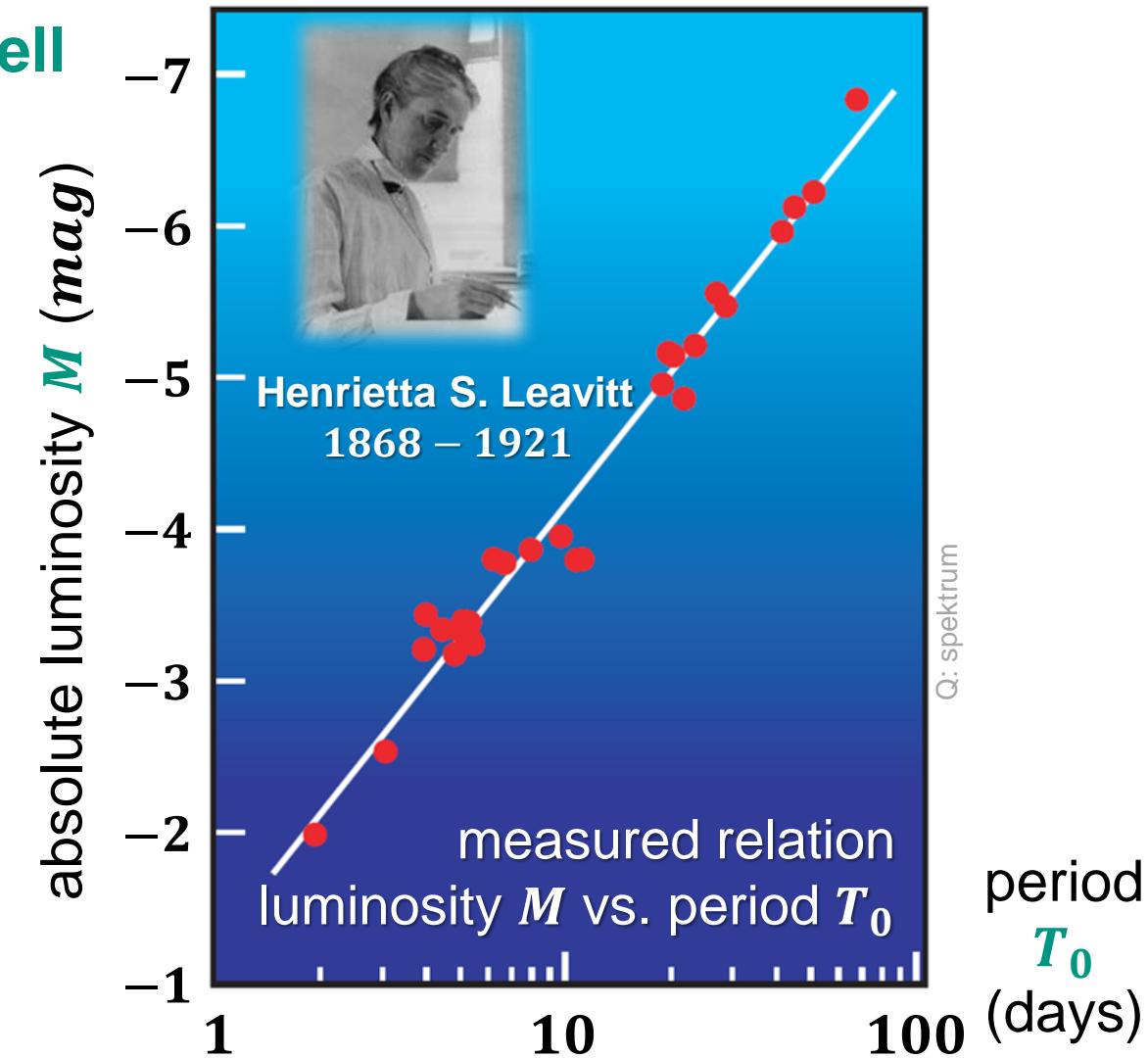
- very massive, very bright cepheids are pulsating more slowly, **period $T_0 \sim L^{3/4}$**

pulsation period – luminosity relation

$$M = -2.81 \cdot \log(T_0) - (1.43 \pm 0.1)$$

T_0 : pulsation period (*days*)

M : absolute brightness (*mag*)



Supernovae – cosmological standard candles #2

■ *SN Ia: thermonuclear detonation**

- a White Dwarf reaches a mass of $M \geq 1.4 M_{\odot}$



merger scenario

Q: U of chicago

