Priv.-Doz. Dr. A. Naber Exercises to the lecture Nano-Optics, WS 2022/23

## Exercises (IV)

(Discussion is on Friday, 9.12.2022)

## Problem 1:

We discussed the solution of Surface-Plasmon-Polaritons (SPPs) in the case of a free electron gas as a simple model for a metal. Another model often used in (nano-) optics is an ideally conducting medium (ICM), i.e., a metal with vanishing electrical resistance and thus infinite conductivity,  $\sigma \to \infty$ . Find first a relation of the conductivity  $\sigma$  to the permittivity  $\epsilon$  at optical frequencies and then try to find a solution of SPPs at the air-ICM interface using the dispersion relation derived in the lecture.

Hint: Use Maxwell's equation  $\operatorname{curl} \vec{H} = \vec{j} + \dot{\vec{D}}$  and the harmonic Ansatz  $\vec{E} = \vec{E}_0 e^{i(\vec{k}\vec{r} - \omega t)}$  to identify  $\sigma/\epsilon_0\omega$  as the imaginary part of the complex permittivity  $\epsilon$  of the metal.

## Problem 2:

A plane electromagnetic wave of angular frequency  $\omega$  in vacuum is reflected back at normal incidence from the interface to a metal with given conductivity  $\sigma$ . Determine the reflection coefficient R and the penetration depth d of the wave into the metal. Assume that  $\sigma$  is a real quantity and that  $\sigma/\omega \gg \epsilon_0 \epsilon'$  in which  $\epsilon'$  is the real part of the permittivity  $\epsilon$ .