

## Exercises (VI)

(Discussion is on Friday, 26.1.2024)

### Problem 1:

Using an optical microscope (lens  $L$ , focal distance  $f$ ), a point-like light source  $P$  in object plane  $O$  is imaged to a point  $P'$  in image plane  $I$ . Simultaneously a similar light source  $Q$  with distance  $s$  to  $P$  is imaged to  $Q'$  with distance  $s'$  to  $P'$  (see drawing). The vacuum emission wavelength of  $P$  and  $Q$  is  $\lambda$ , object plane  $O$  and lens  $L$  are embedded in a material with index of refraction  $n$ , and focal plane  $F$  and image plane  $I$  are embedded in a material with index of refraction  $n'$ . Show that in the case of diffraction limited resolution (Rayleigh criterion) for incoherent light emission of  $P$  and  $Q$  their distance  $s_{\min}$  is given by

$$s_{\min} = 0.61 \frac{\lambda_0}{n \sin \varphi} ,$$

with the maximum angle  $\varphi$  at which light from an object can pass the aperture of radius  $a'$ . In deriving this relation you can assume that  $f \ll d'$ ,  $s' \ll d'$ , and that the lens fulfills Abbe's sine condition for a best possible imaging process.

*Note:* The first minimum in the Airy diffraction pattern of the aperture with radius  $a'$  is given by the angle  $\vartheta = 0.61 \lambda_0 / n' a'$ .

