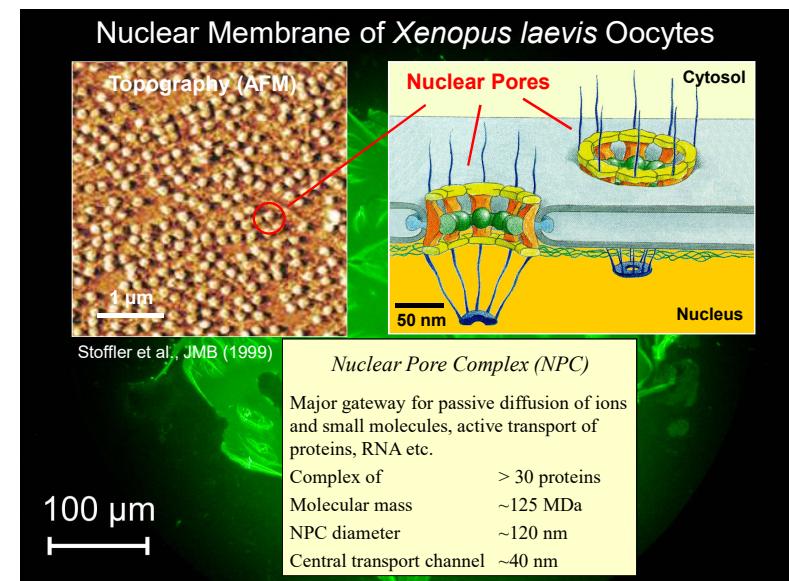
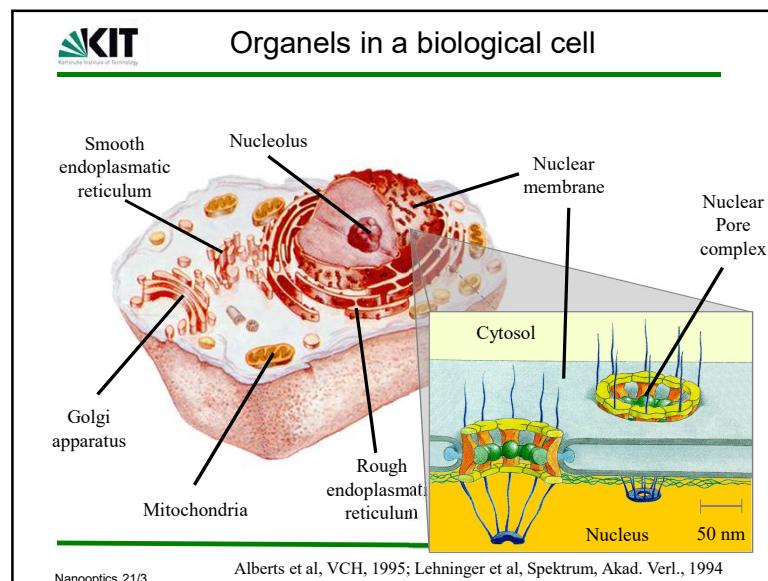
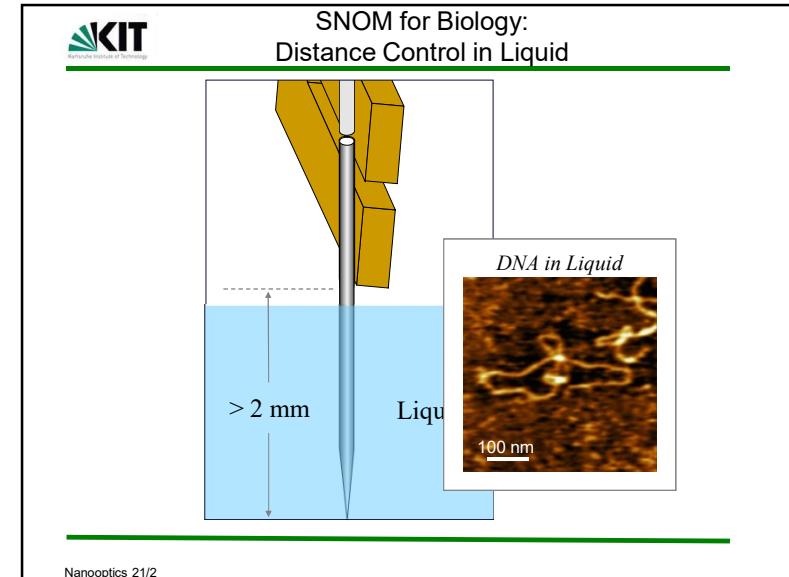


Near-field optics

3. Near-field optics

- 3.5 Scanning near-field optical microscopy : Applications
 - 3.5.1 Single molecule imaging
 - 3.5.2 Imaging of single proteins in biological membranes
 - 3.5.3 Autocorrelation measurements
 - 3.5.4 Fluorescence Correlation Spectroscopy
 - 3.5.5 Observation of single protein transport through a biological membrane

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Nuclei of *Xenopus Laevis*

KIT
Karlsruhe Institute of Technology

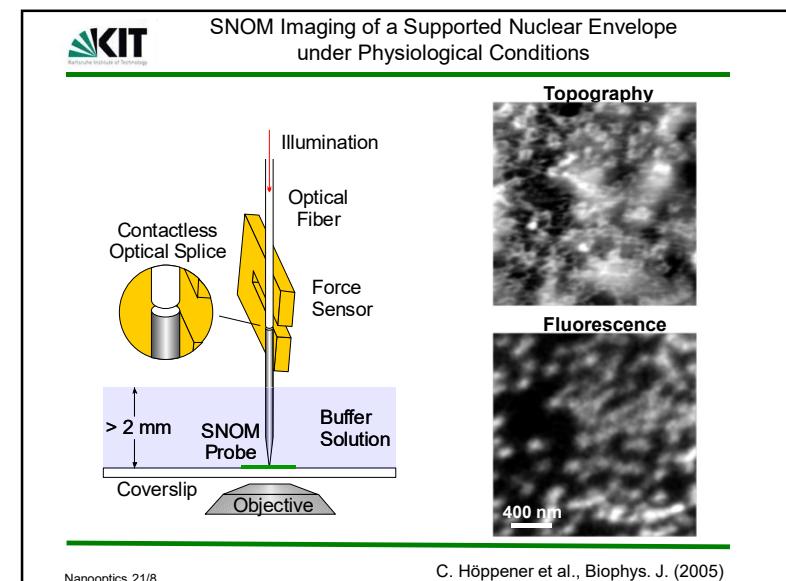
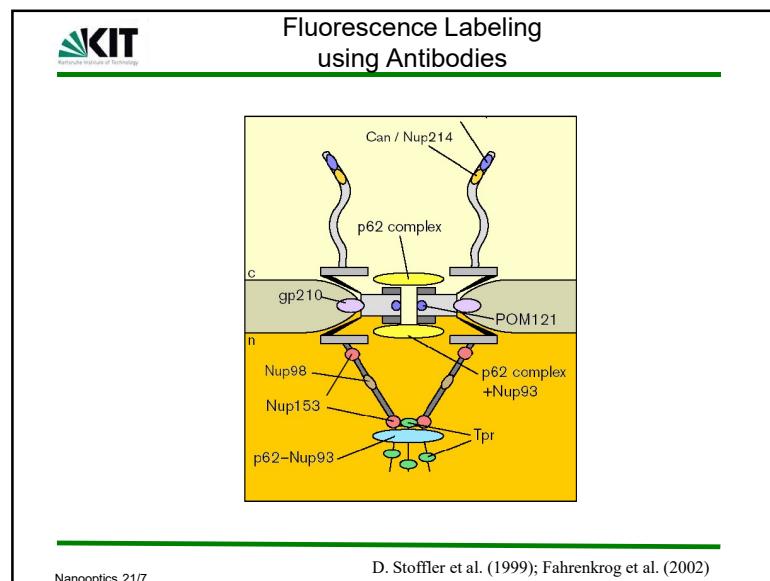
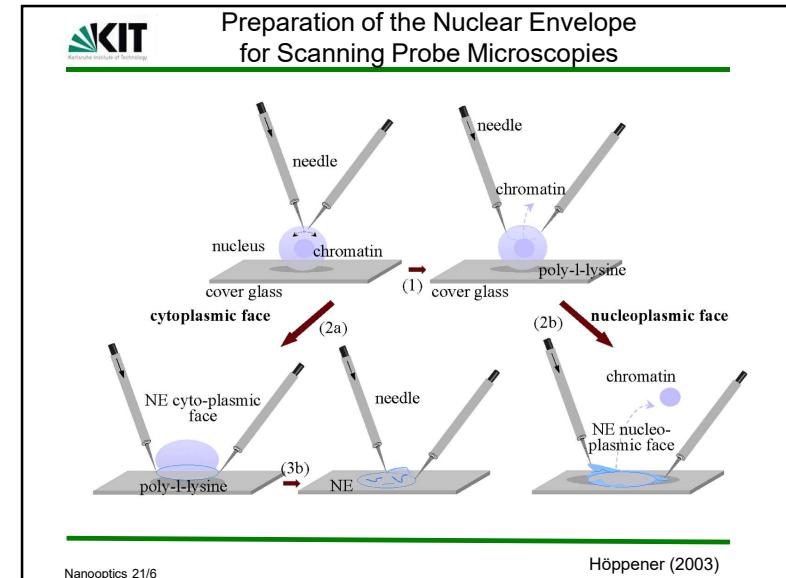
African Clawed Frog (*Xenopus Laevis*)
Oocytes – immature egg cells
extraction of the nucleus
isolated nuclei

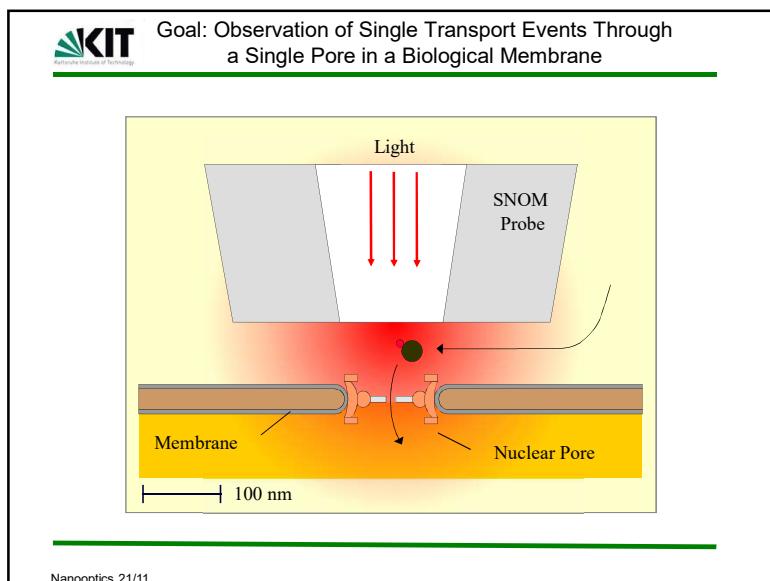
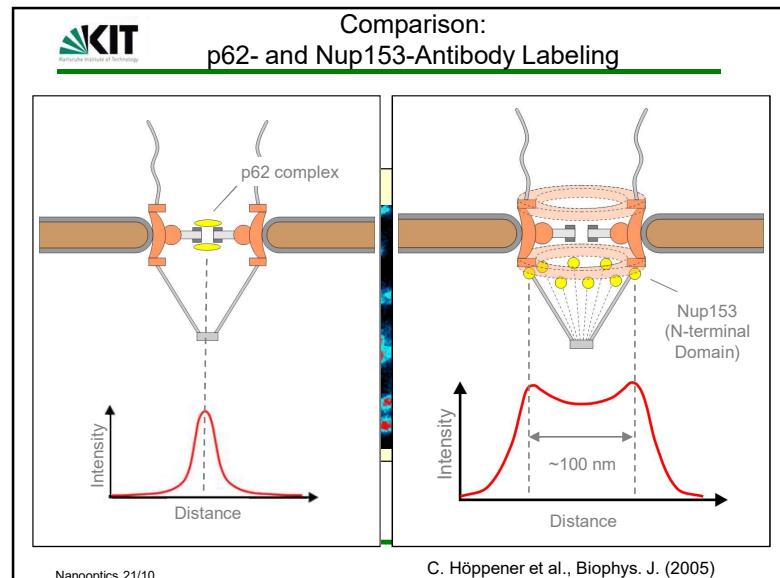
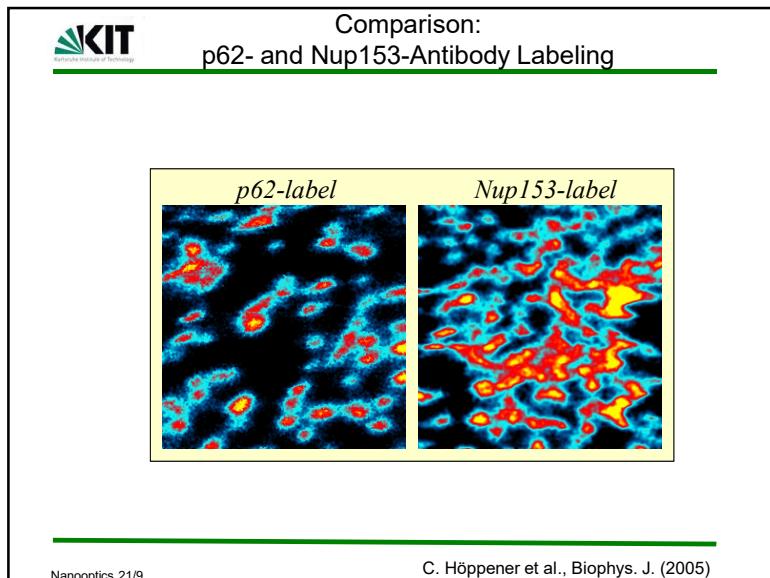
Cytoplasmic face
Nuclear face

500 µm
100 nm
100 nm

Fahrenkrog & Aebi (2003)

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- Near-field optics**
3. Near-field optics
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Autocorrelation and Crosscorrelation

Definitions:

The autocorrelation function of a time-dependent function $f(t)$ is given by

$$ACF(\tau) = \int_{-\infty}^{+\infty} f(t) \cdot f(t + \tau) dt$$

with lag time τ .

The crosscorrelation function of two different functions $f(t)$ and $g(t)$ is

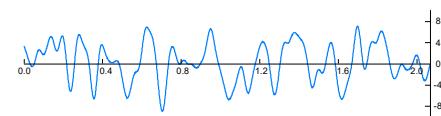
$$CCF(\tau) = \int_{-\infty}^{+\infty} f(t) \cdot g(t + \tau) dt$$

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Example

$E_1(t)$



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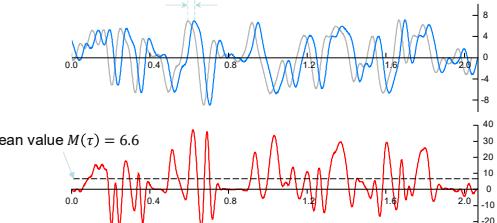


Example

$E_1(t)$
 $E_1(t + \tau)$

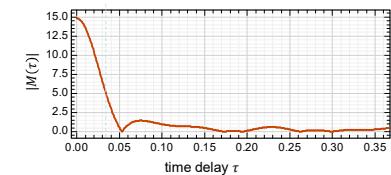
$\tau = 0.03$

$E_1(t) \cdot E_1(t + \tau)$



$$M(\tau) = \frac{1}{T} \int_0^T E_1(t) E_1(t + \tau) dt$$

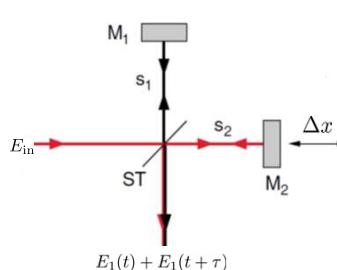
(„autocorrelation function“)



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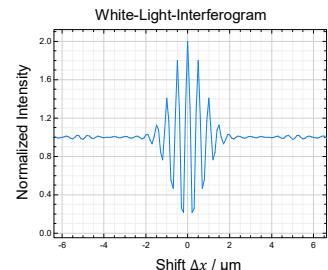
Example: Michelson-Interferometer



M_1, M_2 Mirror
ST Beamsplitter
 s_1, s_2 Beampath

$$s_2 = s_1 + \Delta x$$

$$\tau = \frac{2\Delta x}{c_0}$$



Detector measures

$$I(t) \propto 2 \langle E_1^2(t) \rangle_T + \langle E_1(t) \cdot E_1(t + \tau) \rangle_T$$

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Autocorrelation of the light-electric field

First-order electric field correlation function:

$$\langle E^*(t) E(t + \tau) \rangle = \frac{1}{T} \int_T E^*(t) E(t + \tau) dt \quad \text{with measurement time } T$$

Normalized first-order electric field correlation function:

$$g^{(1)}(\tau) = \frac{\langle E^*(t) E(t + \tau) \rangle}{\langle E^*(t) E(t) \rangle} \quad \text{with} \quad \langle E^*(t) E(t) \rangle = |E(t)|^2 \sim \bar{I}$$

(average intensity)

➤ depends on phase (interference, e.g. Michelson interferometer)

Normalized second-order electric field correlation function:

$$g^{(2)}(\tau) = \frac{\langle I(t) I(t + \tau) \rangle}{\bar{I}^2}$$

➤ depends on photon statistics (quantum optics)

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Near-field optics

3. Near-field optics

3.5 Scanning near-field optical microscopy : Applications

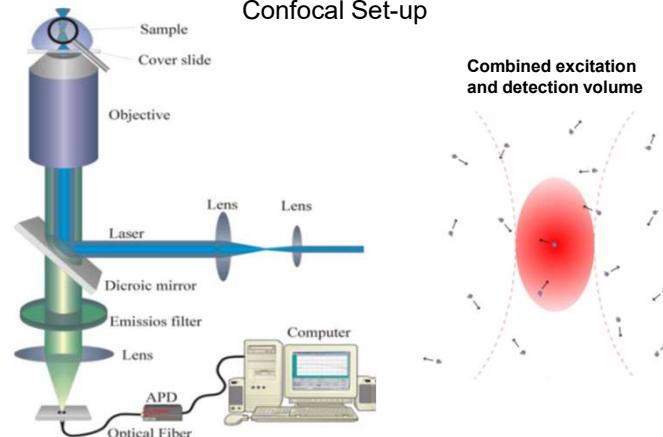
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Fluorescence Correlation Spectroscopy

Confocal Set-up

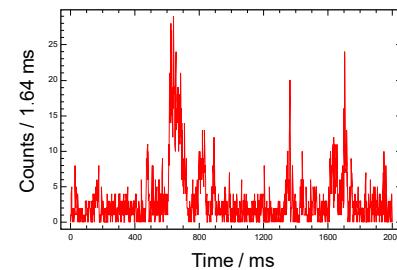


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Haustein & Schwille (2004)



FCS



- How long, in average, does a molecule stay in the excitation-detection volume?
→ residence time τ
- How fast, in average, does a molecule move through the excitation-detection volume?
→ diffusion coefficient D

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