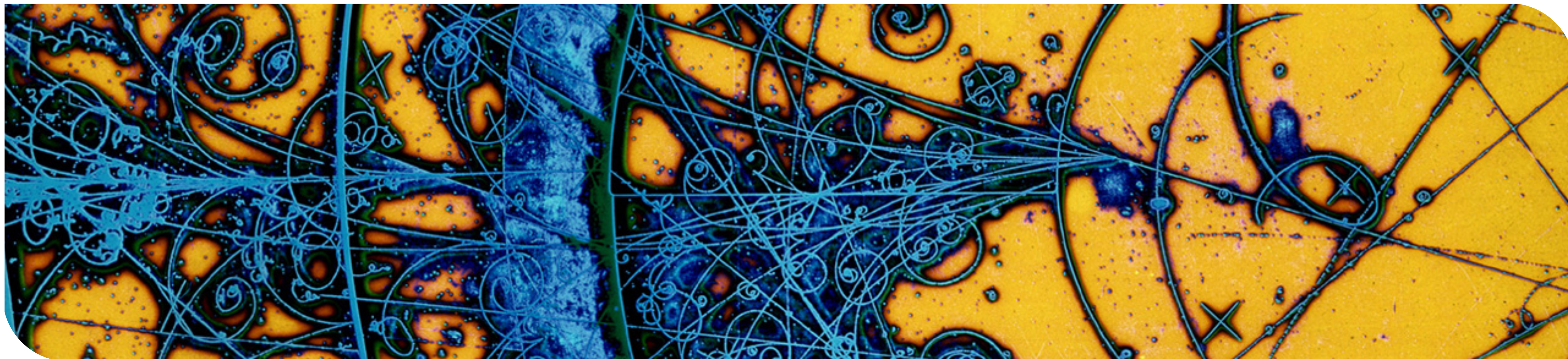


Particle Physics 1

Lecture 17: Jets and high p_T physics

Prof. Dr. Torben FERBER (torben.ferber@kit.edu, he/him), Institut für Experimentelle Teilchenphysik (ETP)
Wintersemester 2023/2024



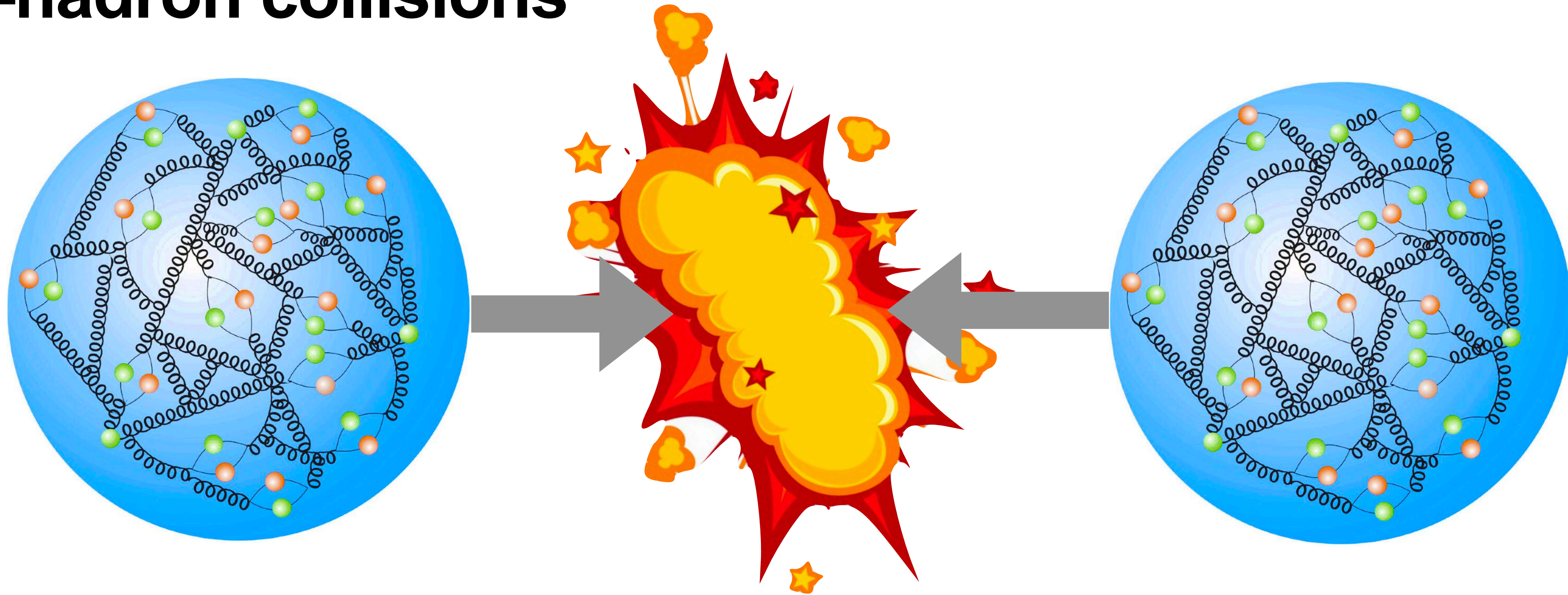
Credit: CERN

Learning goals

- What are jets?
- W production and properties
- Top production and properties

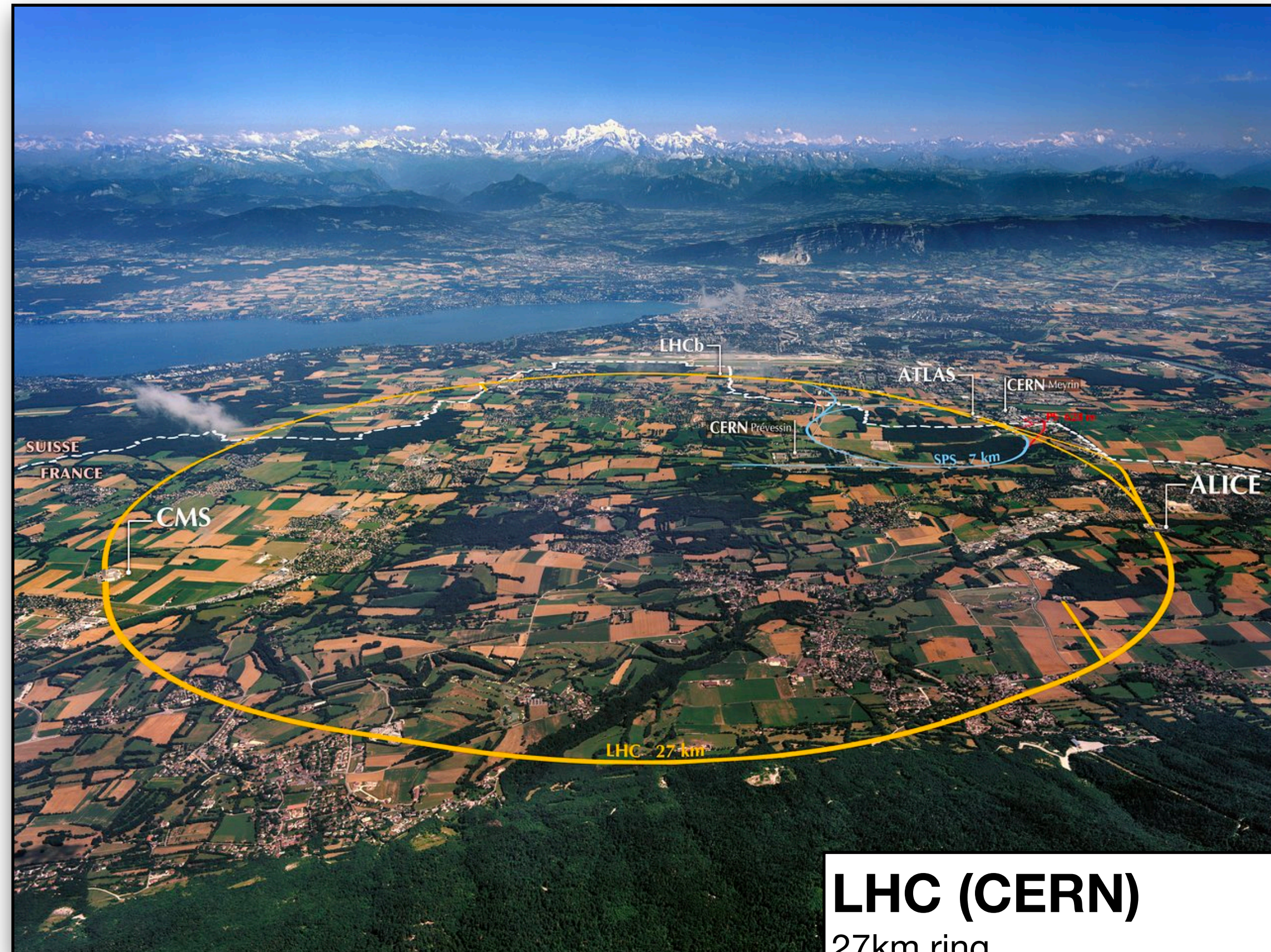
- What is high- p_T physics?
 - Particle physics at very large momentum (transfer), often at hadron colliders
 - Most important analysis objects: jets originating from fragmentation and hadronization of quarks and gluons
 - Study of most massive particles of the standard model: W and Z bosons, top quarks, Higgs boson (later)

Hadron-hadron collisions



- No collision of point-like particles at fixed energy, but “broad-band” beam of various partons (quarks, gluons) with different color and energy
- Challenge: Reliable calculation of observables

Hadron-hadron collisions



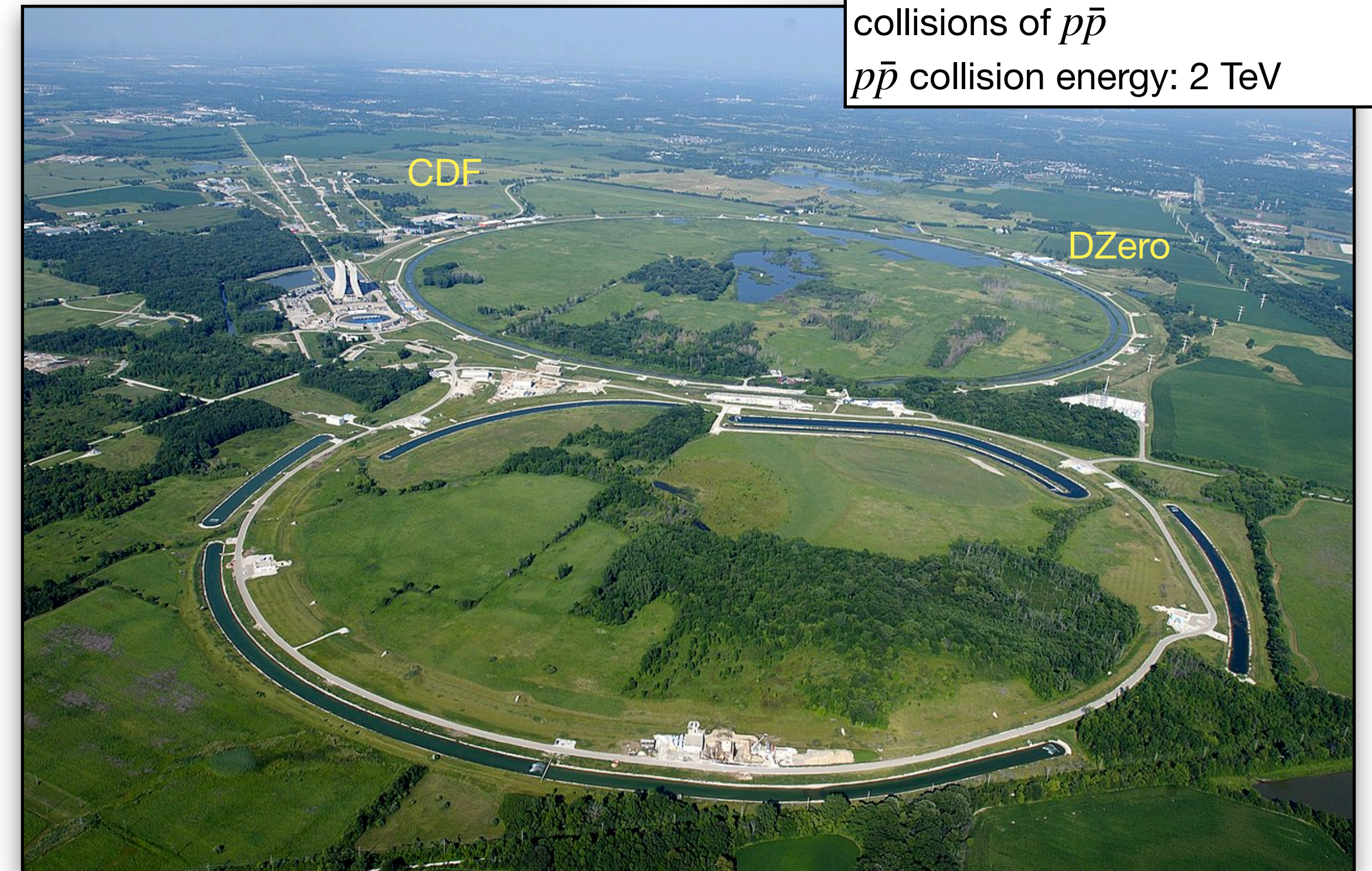
Credit: Maximilien Brice (CERN)

LHC (CERN)

27km ring
collisions of pp and heavy ions
 pp collision energy: 13.6 TeV

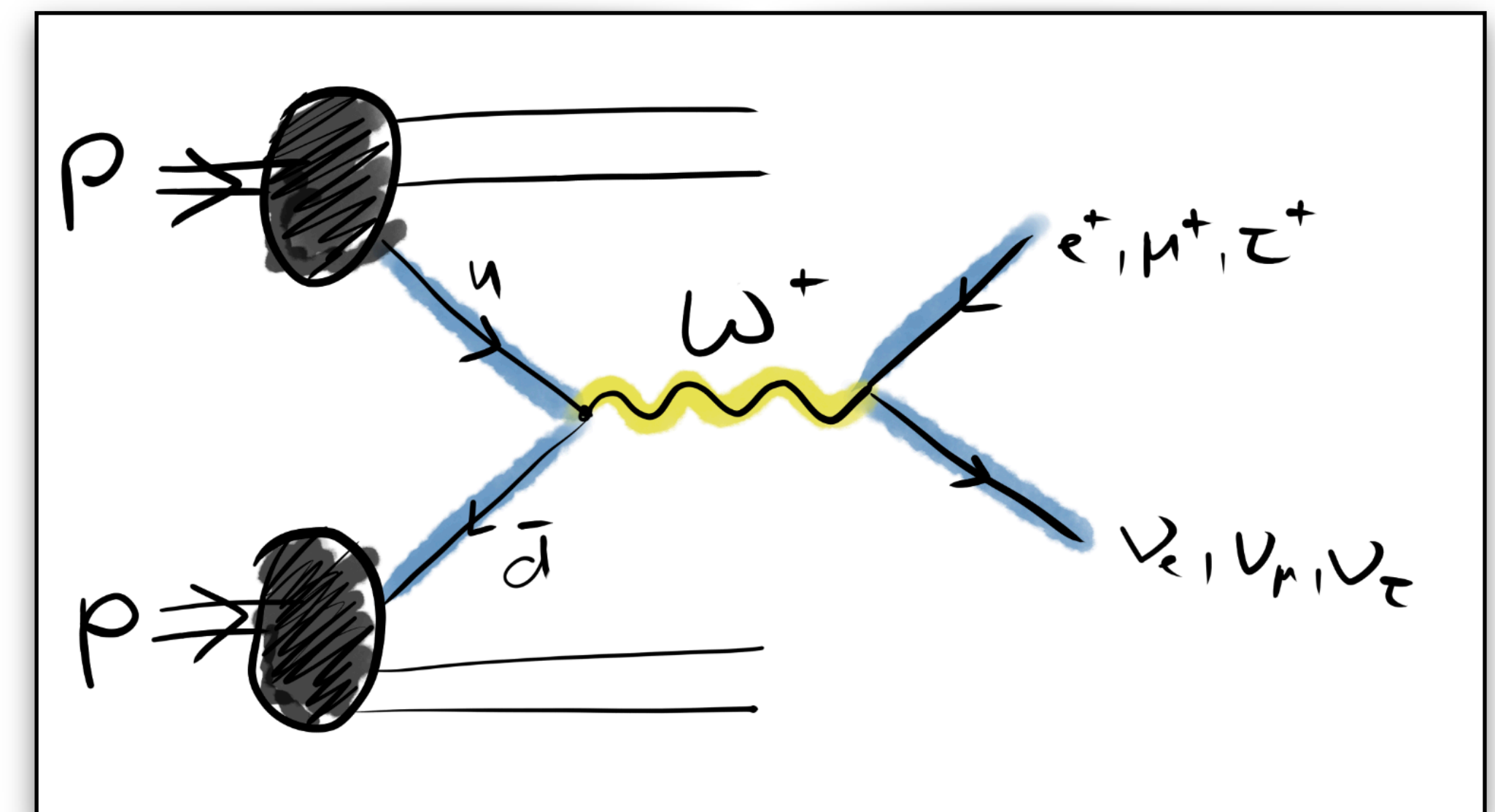
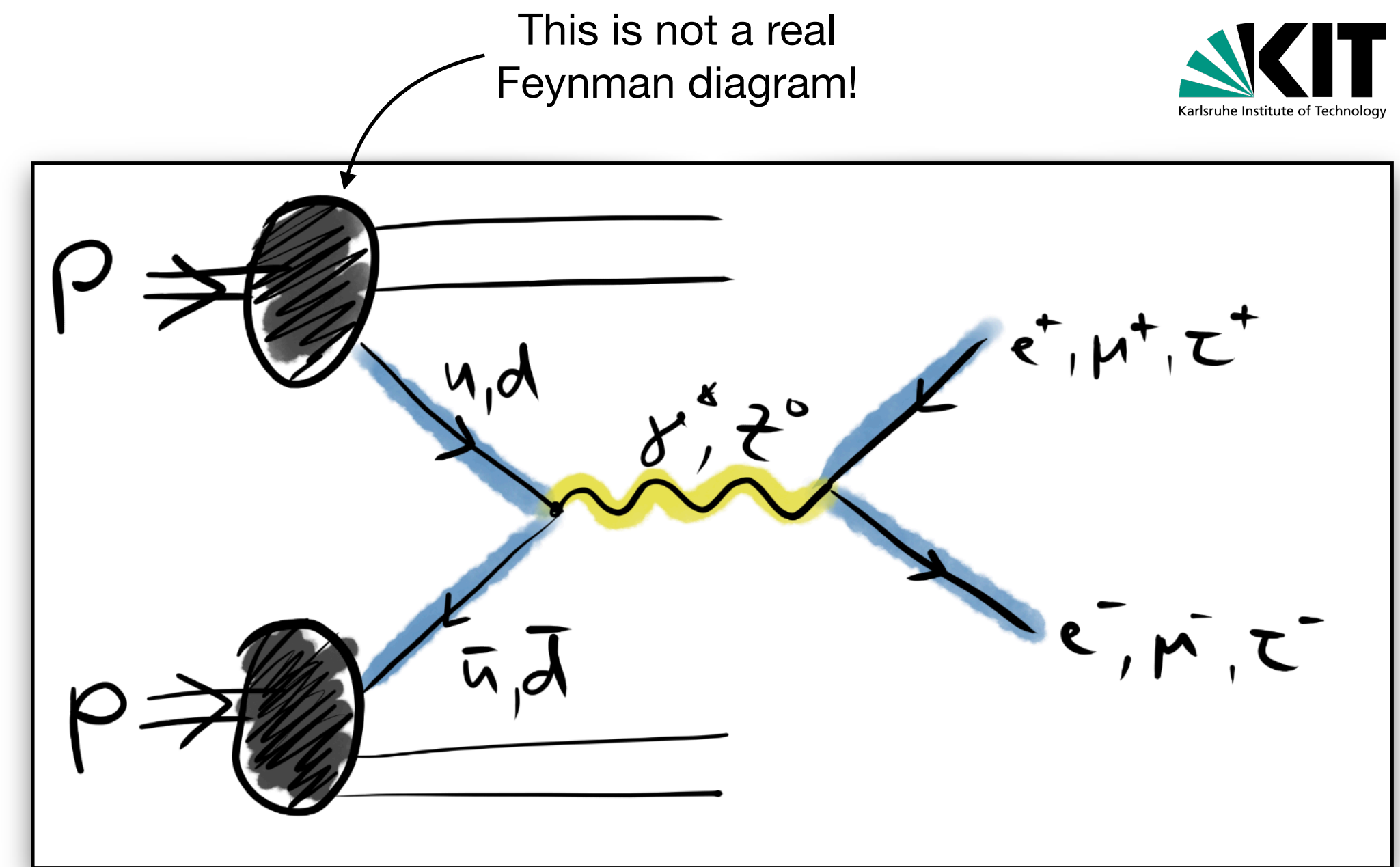
Tevatron (Fermilab)

6km ring
collisions of $p\bar{p}$
 $p\bar{p}$ collision energy: 2 TeV

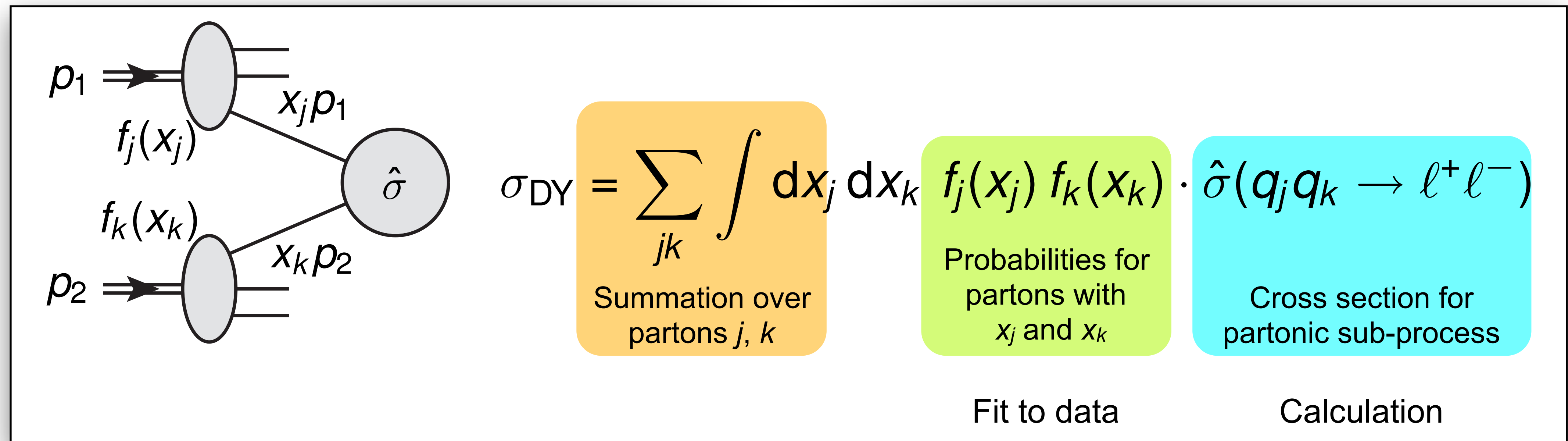


Example: Drell-Yan

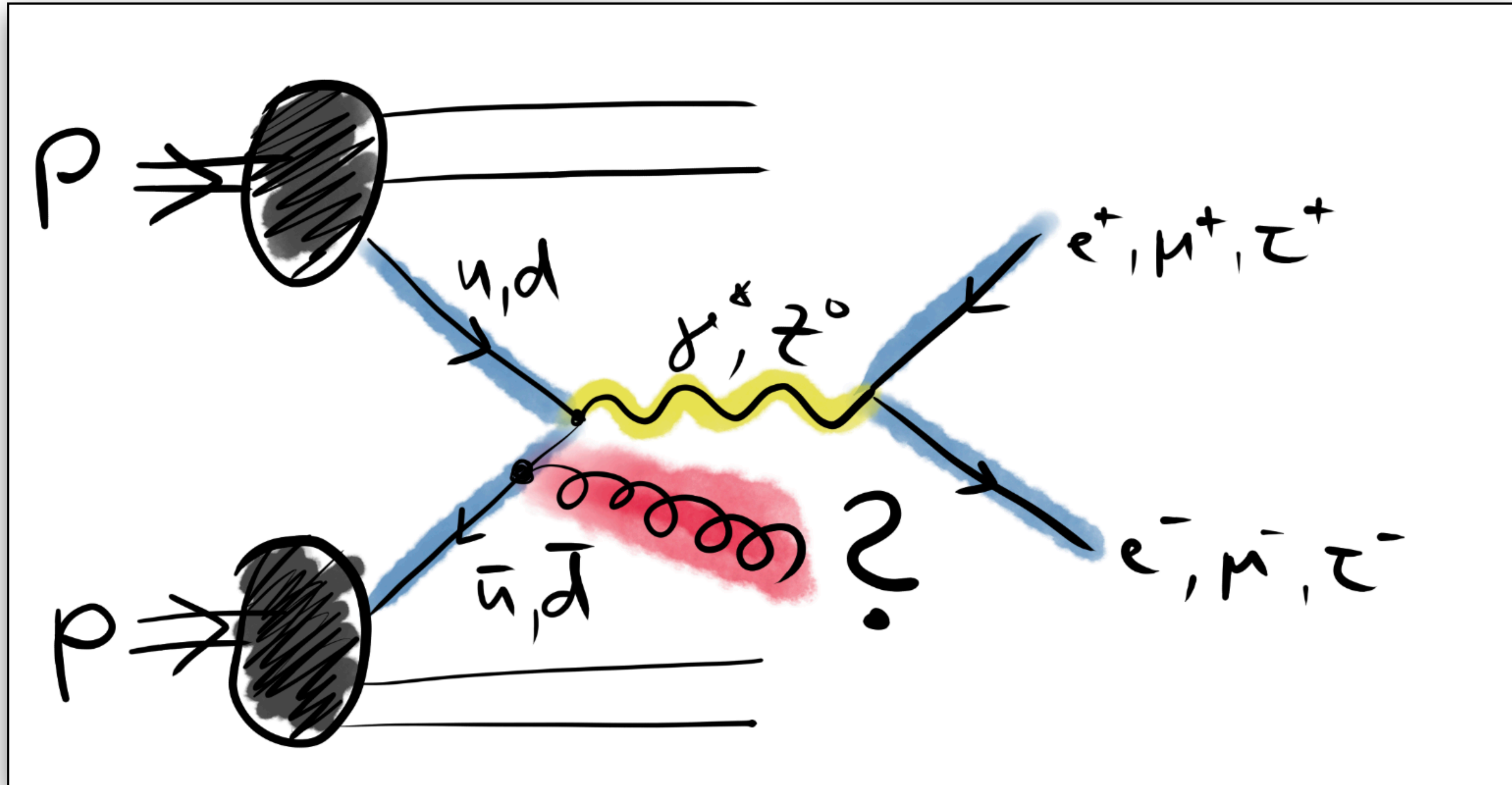
- Drell-Yan: quark-antiquark annihilation into (virtual) photon, Z, or W into lepton pairs
- $pp \rightarrow \gamma^*/Z \rightarrow \ell^+ \ell^-$ or $pp \rightarrow W^\pm \rightarrow \ell^\pm \bar{\nu}$
- large center of mass energies with large momentum transfers
- no hadronisation (apart from proton remnants)



- Factorization theorem (can be proven): cross section of Drell-Yan process can be calculated by factorizing hard/soft components:
 - Compute “hard” partonic sub-process in perturbative QCD, e.g. $q\bar{q} \rightarrow \mu^+\mu^-$
 - Weight cross section with probability to find these partons in hadrons ($\rightarrow$ PDFs $f_i(x)$) and integrate over all partons and parton momenta
 - PDFs universal $\rightarrow$ measured independently, e.g. in DIS



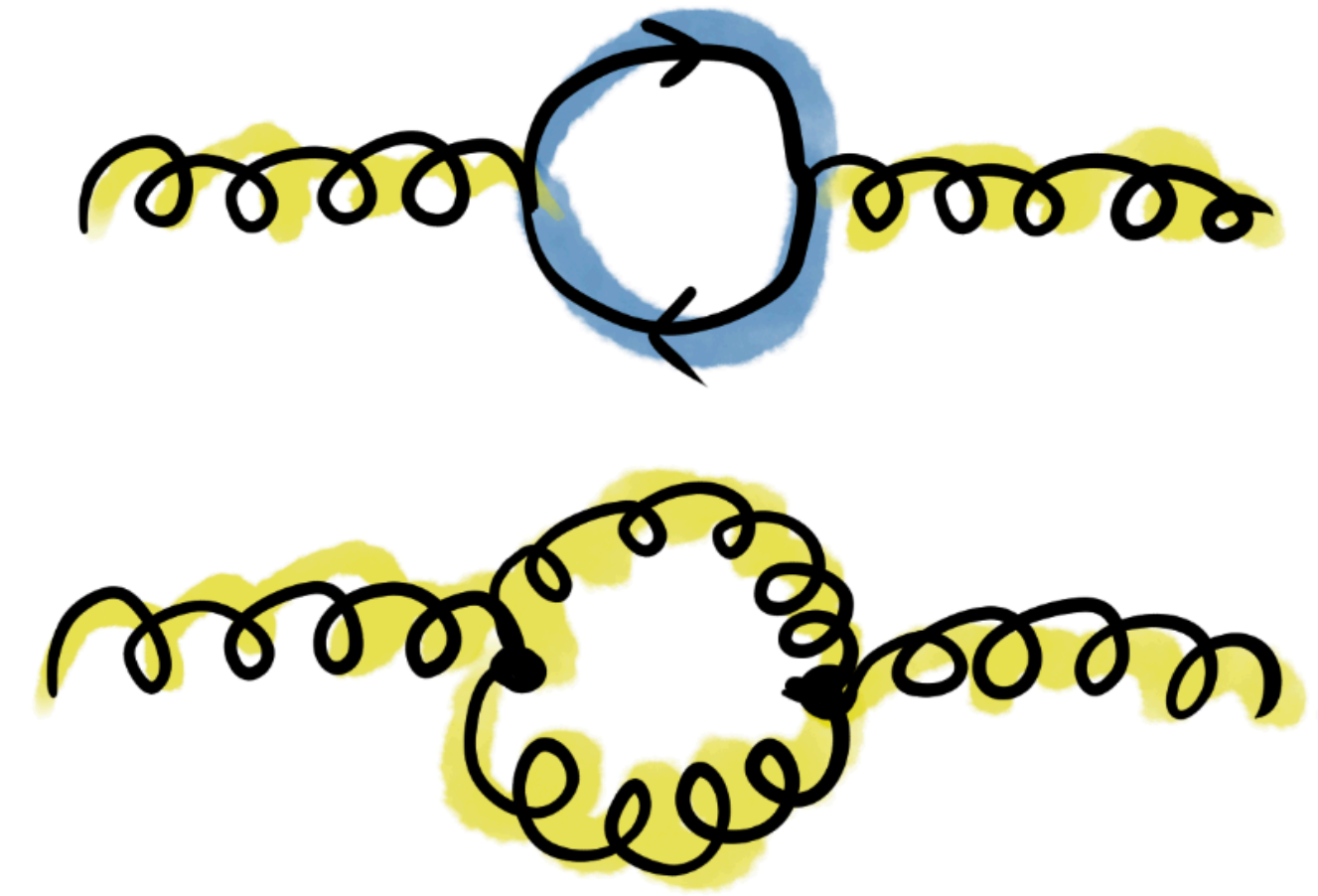
Divergencies



Divergencies

■ Ultraviolet divergencies:

- Source: unbound momenta of particles in loops
- Solution: **Renormalization** (with scale μ_R); **UV divergencies absorbed in running coupling α_s**



■ Infrared divergencies:

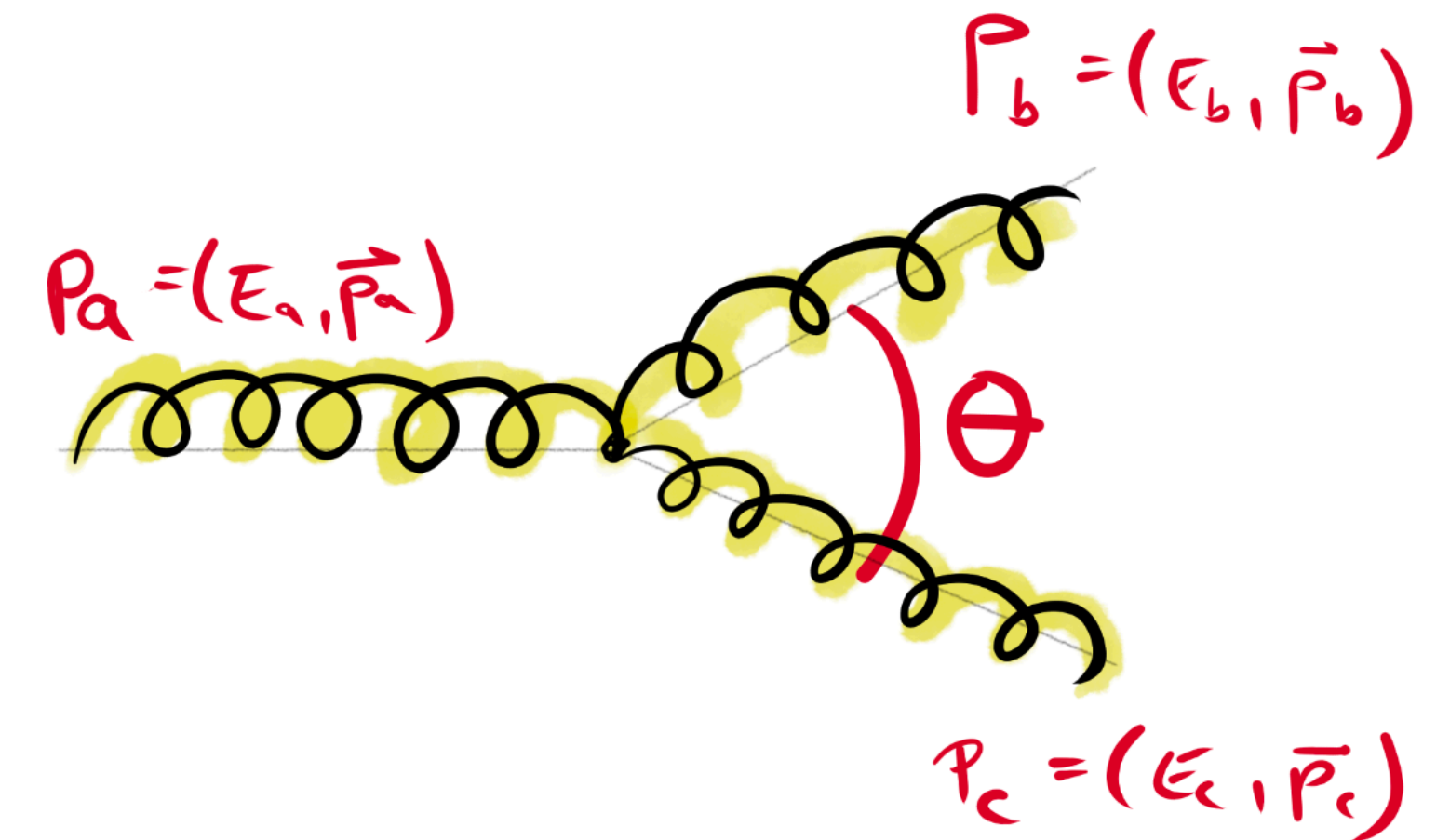
- Consider propagator of the incoming gluons $\sim 1/p_a^2$:

$$p_a^2 = (p_b + p_c)^2 = m_b^2 + m_c^2 + 2(E_b E_c - \mathbf{p}_b \cdot \mathbf{p}_c)$$

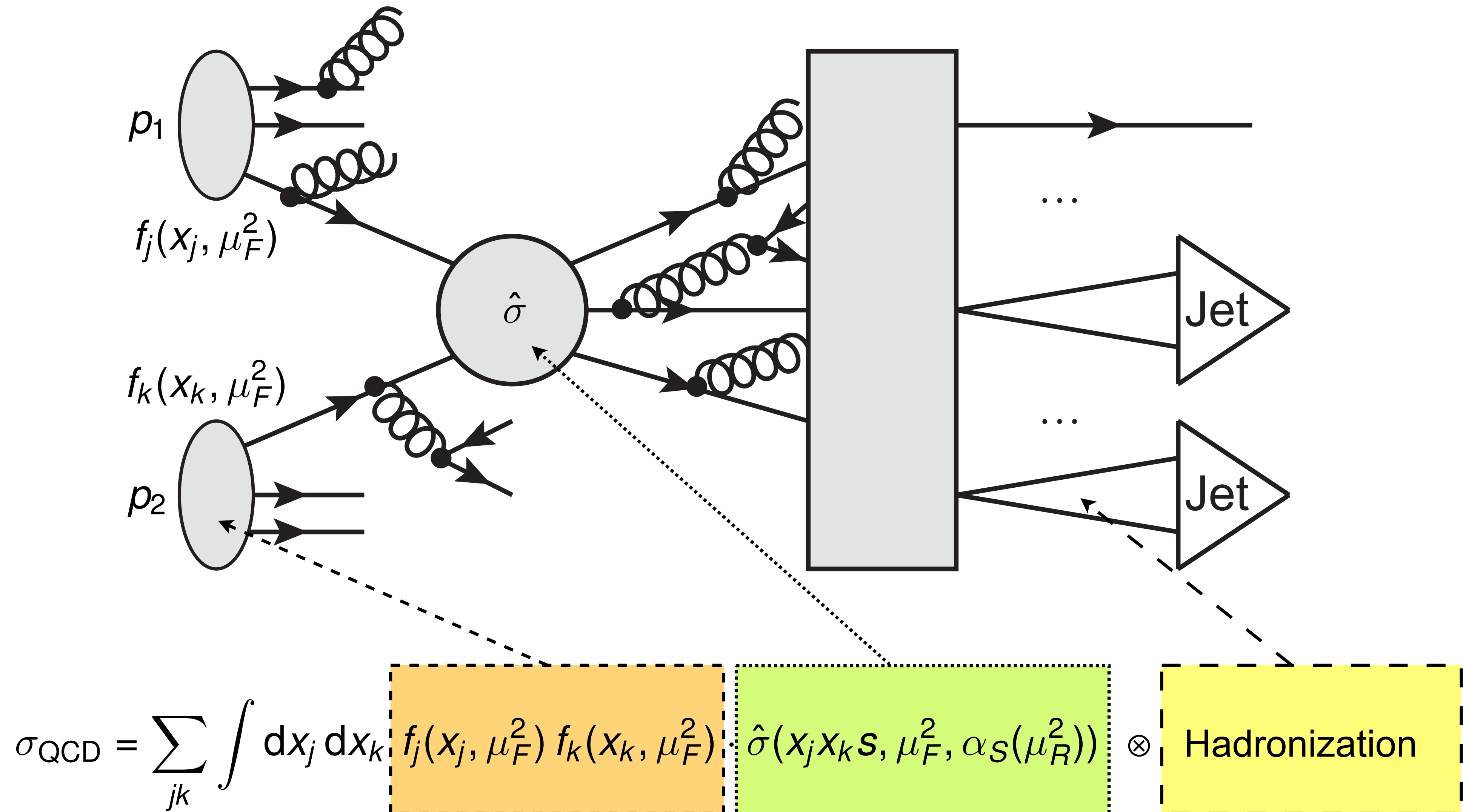
$$\underset{m_i=0}{=} 2E_b E_c (1 - \cos \theta) = 2E_a^2 z(1 - z)(1 - \cos \theta)$$

Source: soft ($z \rightarrow 0$ or 1) or collinear ($\theta \rightarrow 0$) gluons ($\rightarrow$ large range, pQCD not valid)

- Solution: **IR divergencies absorbed in PDFs** (the PDFs become scale dependent with **factorization scale μ_F**)



Cross section = PDFs $\otimes$ hard process $\otimes$ hadronization

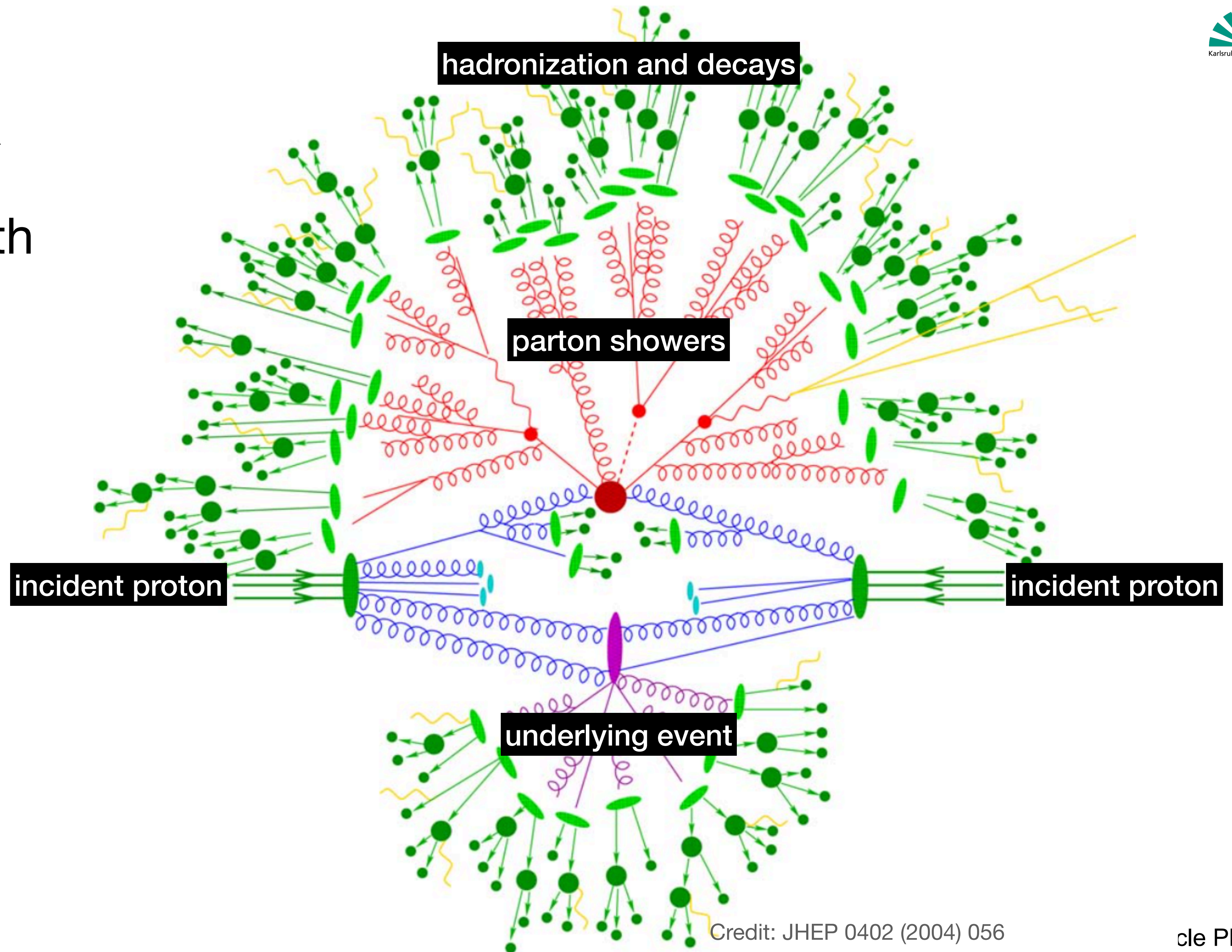


What is a jet?

- Relation between **properties of partons** (quarks and gluons) and objects measured in collider detector (jets)?
 - Unknown momentum fractions of interacting partons → **unknown Lorentz boost** of partonic center-of-mass frame relative to laboratory frame
 - Quarks and gluons carry color charge, jets are color neutral
→ **no unambiguous jet-parton assignment** possible
 - Working hypothesis (“local parton-hadron duality”): parton properties can be **inferred directly** from measurements of hadrons

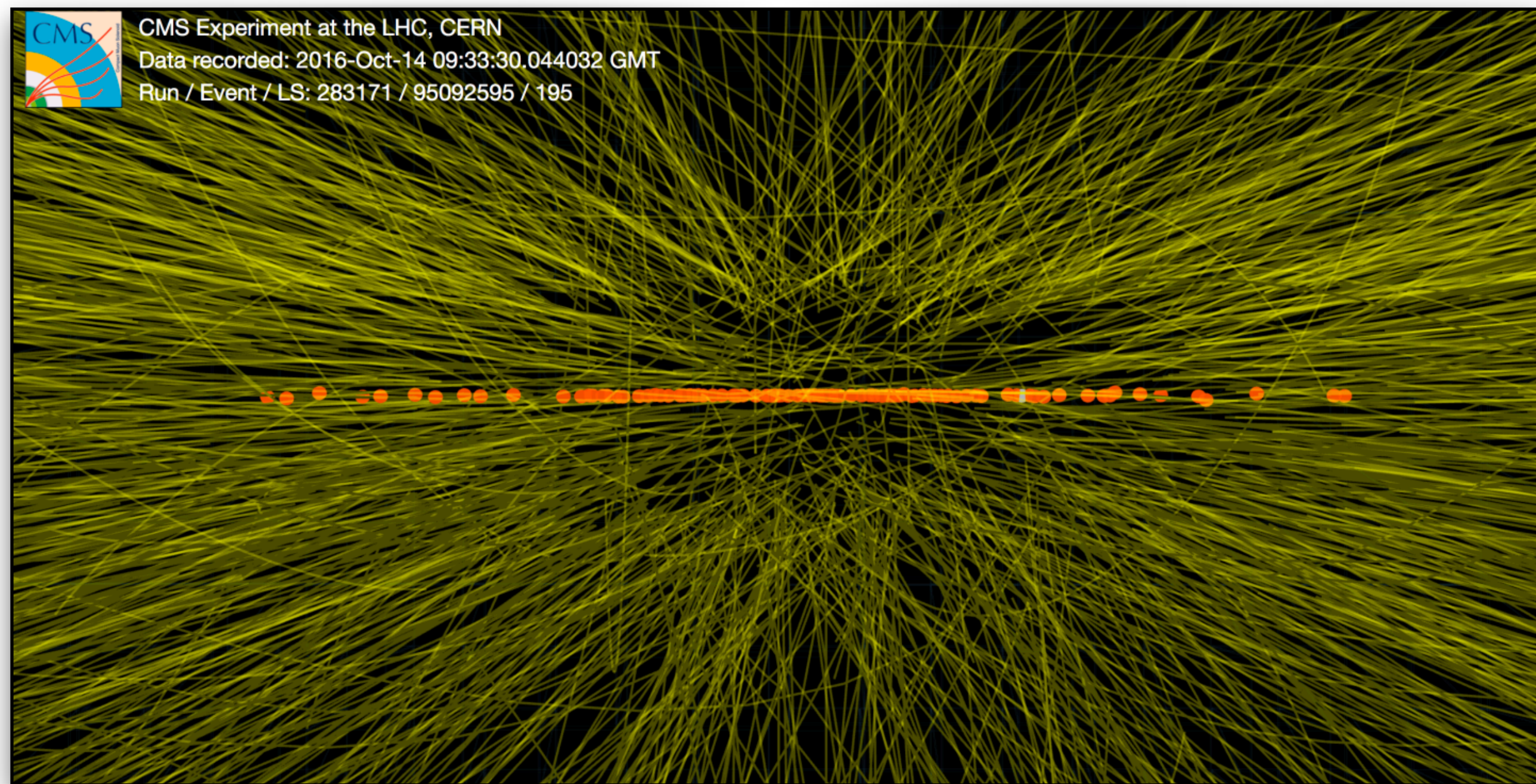
Jets

- Very complex process:
Described with
Monte Carlo

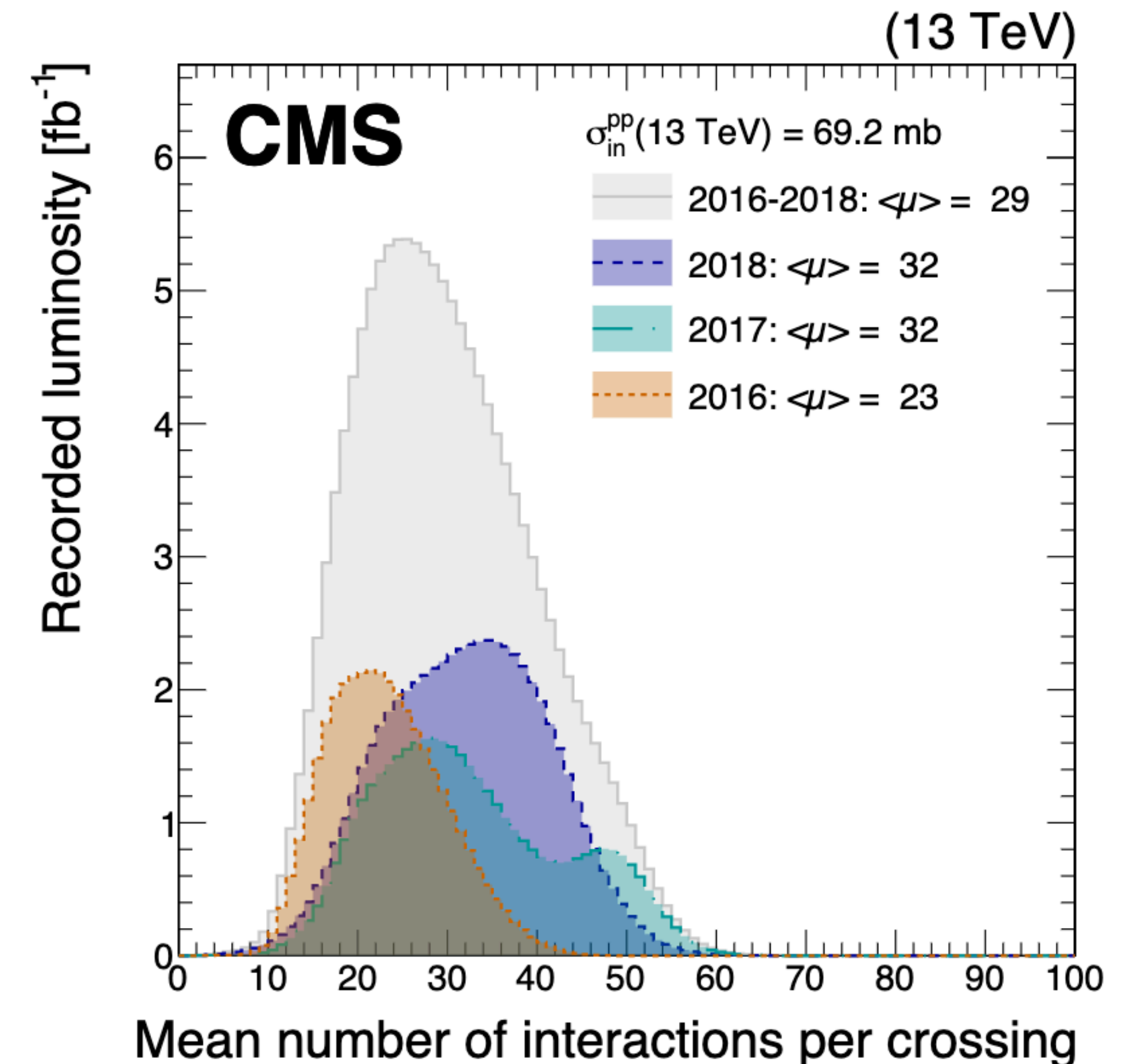


Additional challenge: Pile up

- In addition to unwanted particles from the underlying event, in LHC pp collisions, more than one interaction occurs per bunch crossing



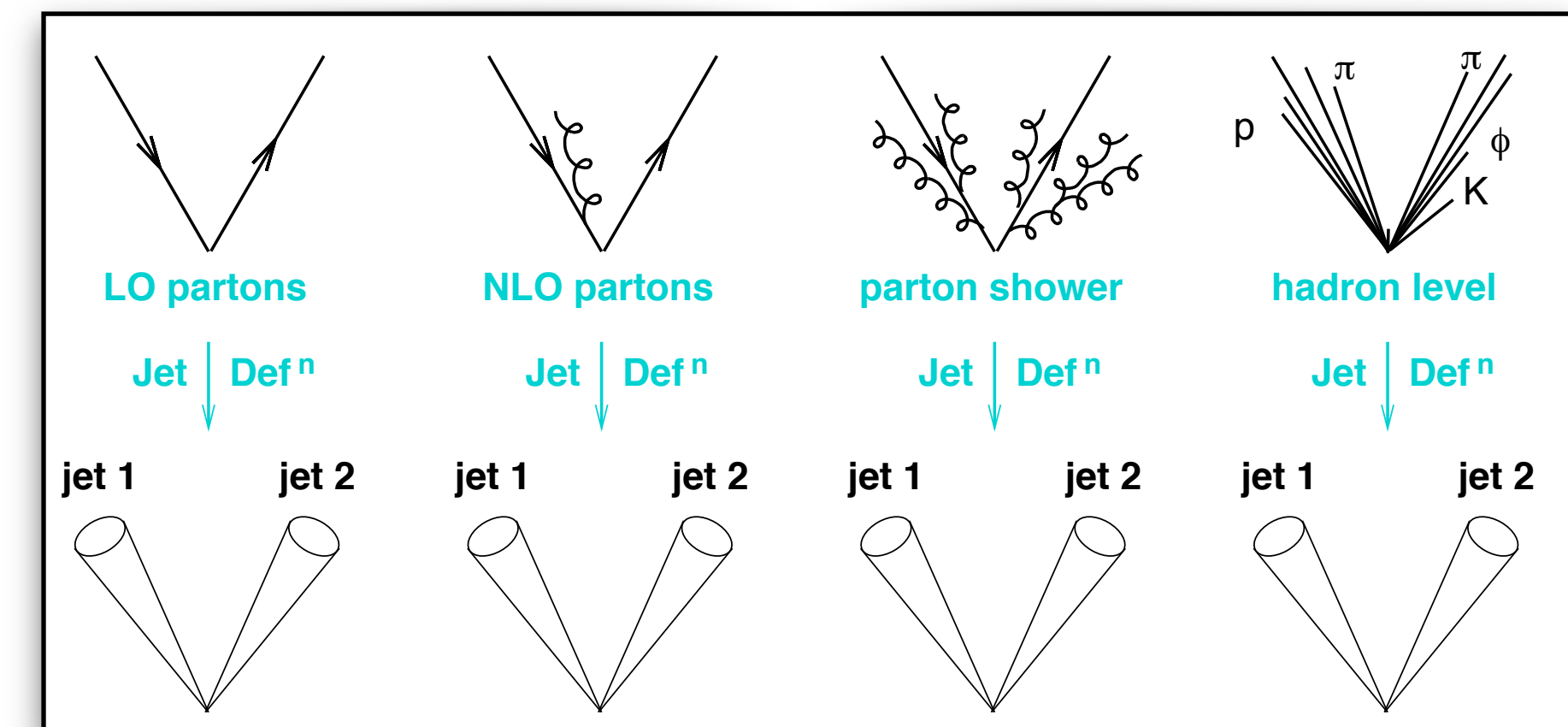
Credit: <https://cds.cern.ch/record/2231915>



Credit: <https://arxiv.org/pdf/2003.00503.pdf>

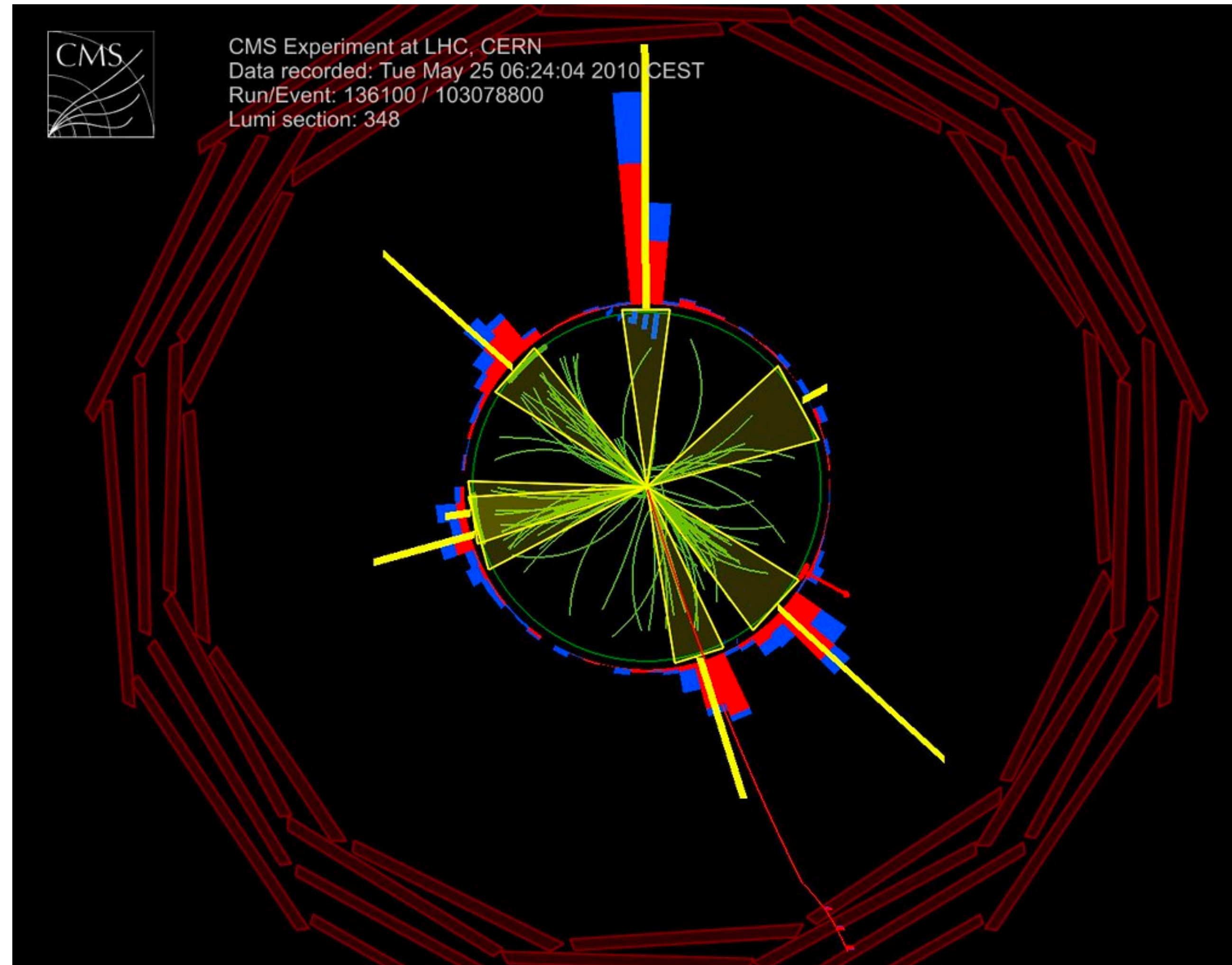
Jet reconstruction

- Jets can be defined on different technical levels:
 - Parton level: for calculations in perturbative QCD (“theory jets”)
 - Particle level: jets reconstructed from stable hadrons
 - Detector level: jets reconstructed from energy deposits in calorimeter and/or tracks in tracking detectors
- Design of successful jet algorithms:
 - Independent of technical level
 - Invariant under Lorentz boosts
 - Comparison with theory: infrared and collinear safe → find same jet even after emitting soft/collinear radiation



Credit: G. Salam

Jet example

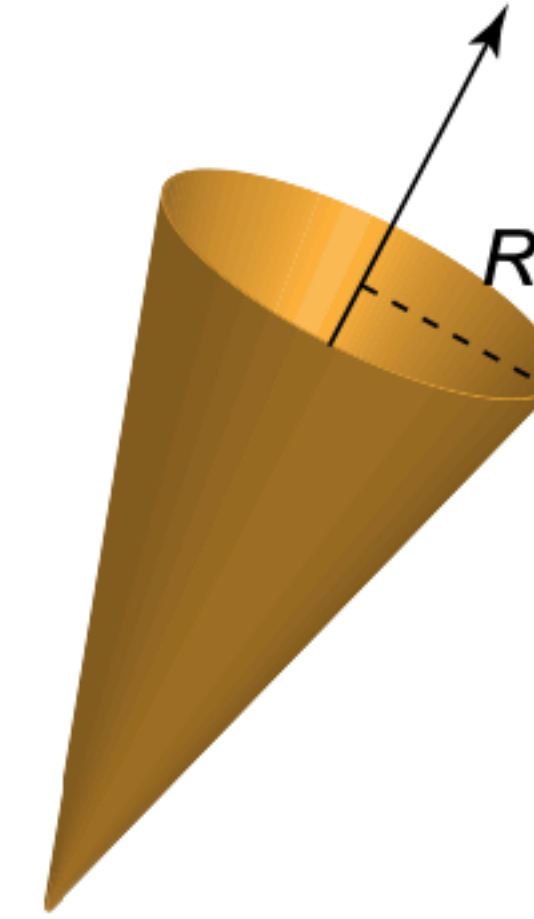


Jet reconstruction

■ Fixed cone algorithms:

- Start with high energy seed
- collect all energy within a cone with radius

$$R = \sqrt{(\eta - \eta_0)^2 + (\phi - \phi_0)^2}$$
- Split/merge nearby clusters



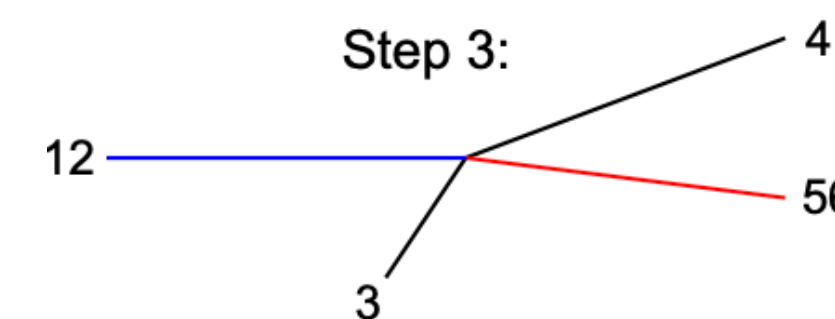
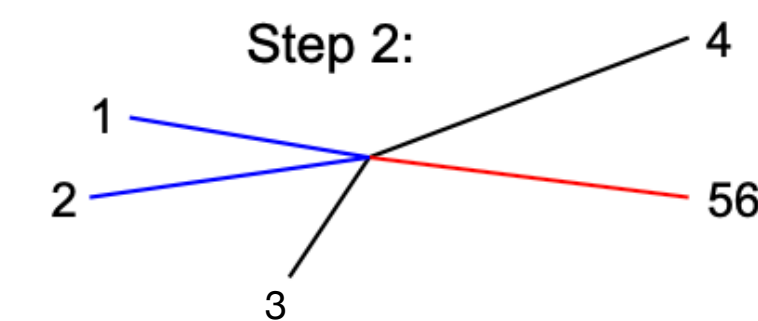
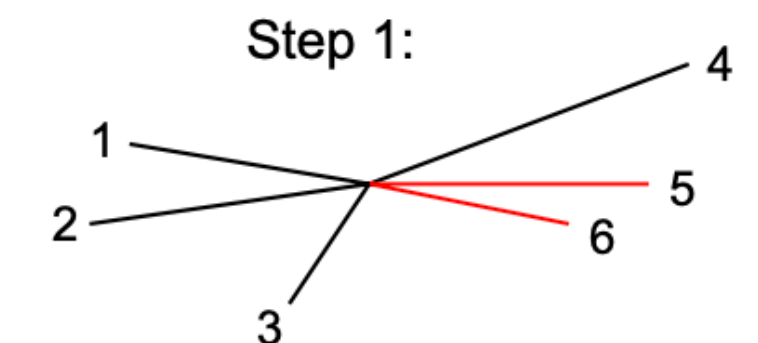
■ Sequential recombination “anti-kt”:

- compute distances ($R_{\text{LHC run 2}} = 0.4$):

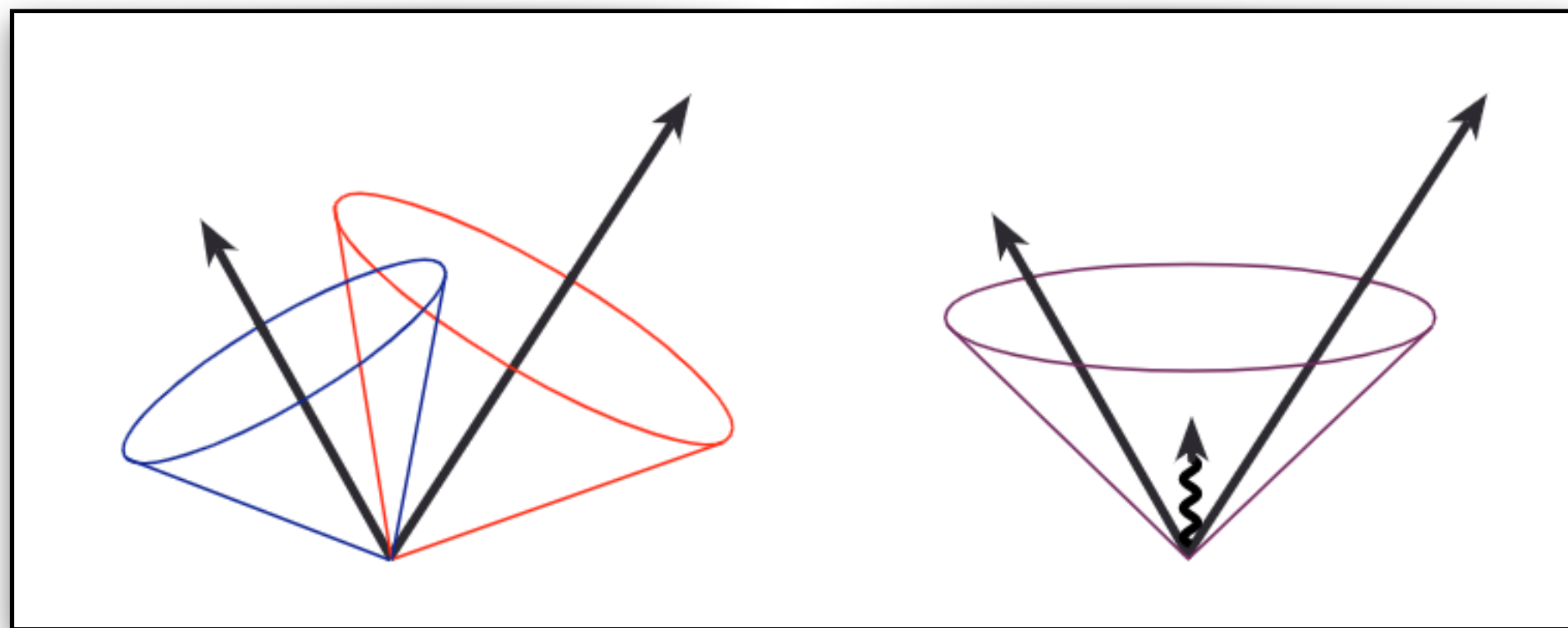
$$d_{ij} = \min(k_{t,i}^{-2}, k_{t,j}^{-2}) \frac{\Delta R_{ij}^2}{R^2}$$

- combine pairs with $d_{ij} < k_{t,i}^{-2}$

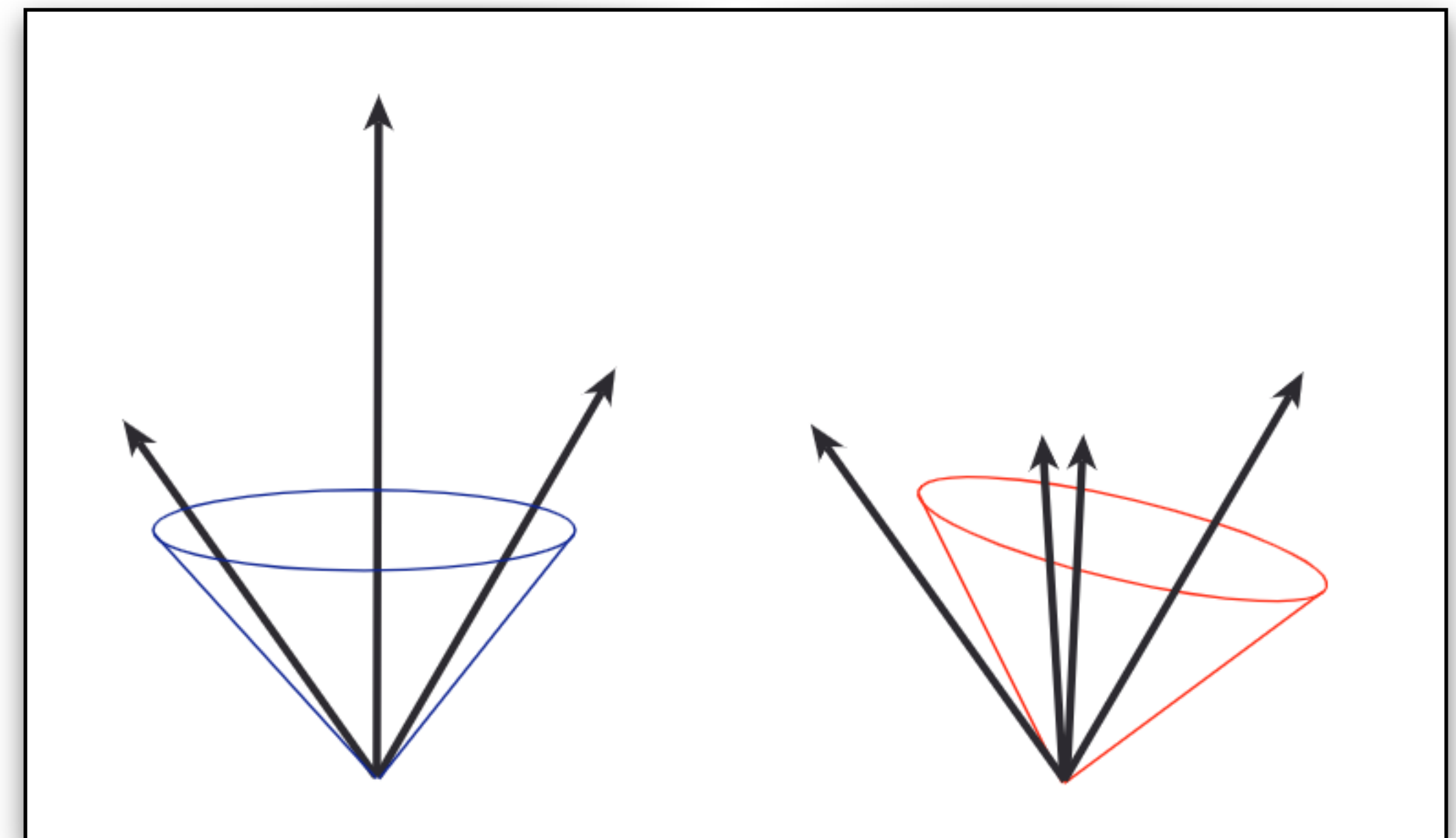
<https://arxiv.org/abs/0802.1189>



Not save cone: IR problems



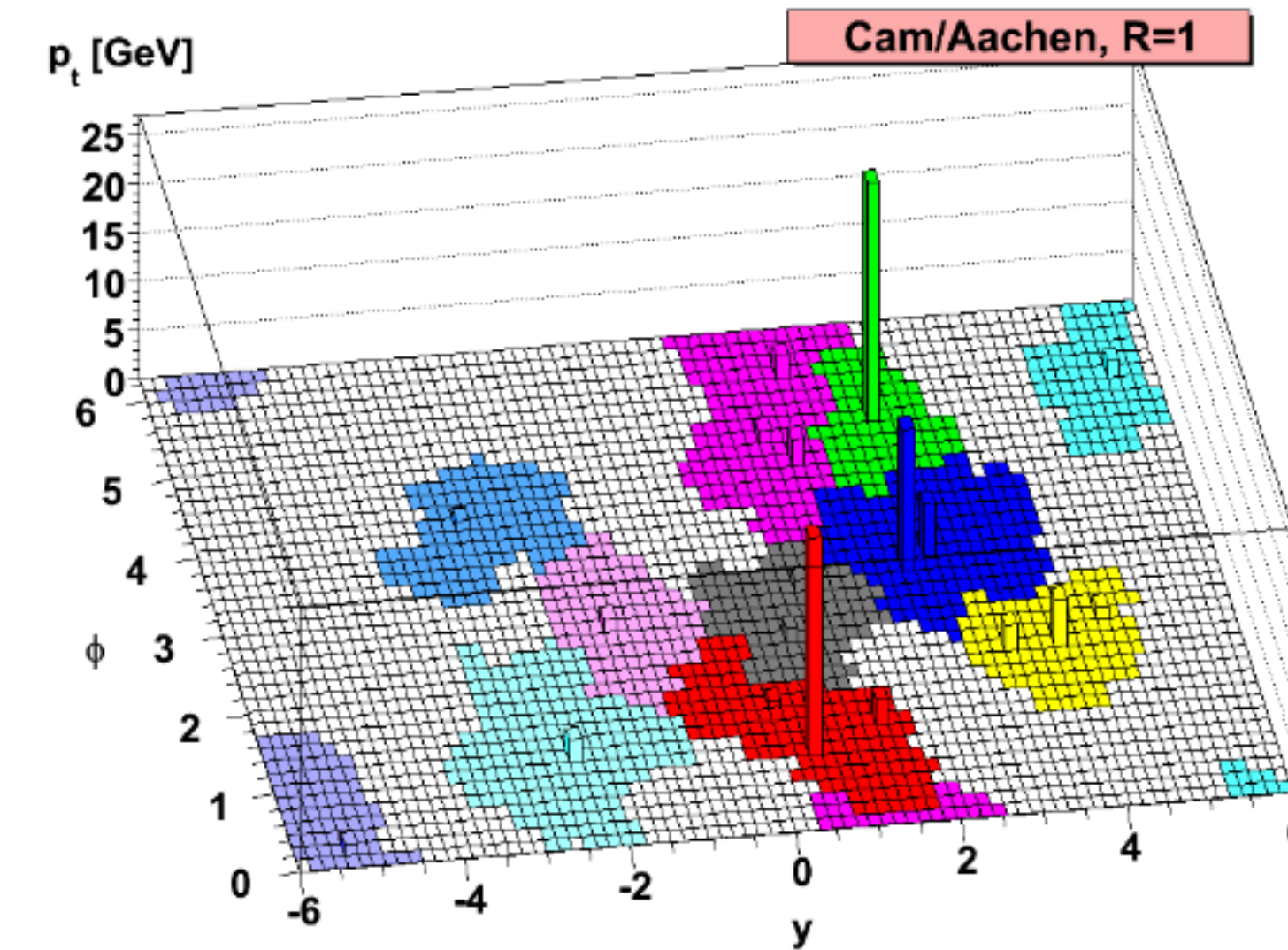
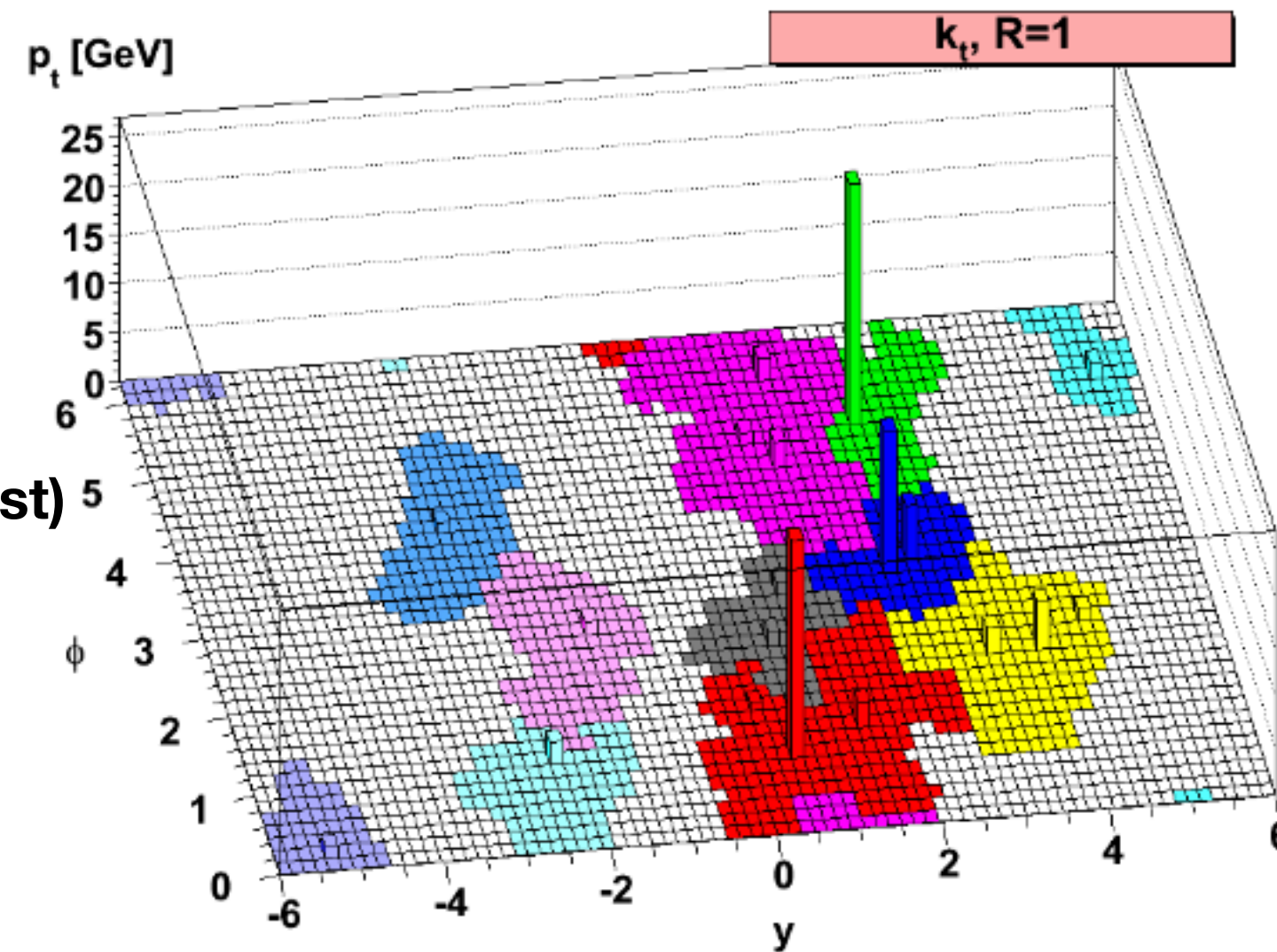
Not save cone: Collinear problems



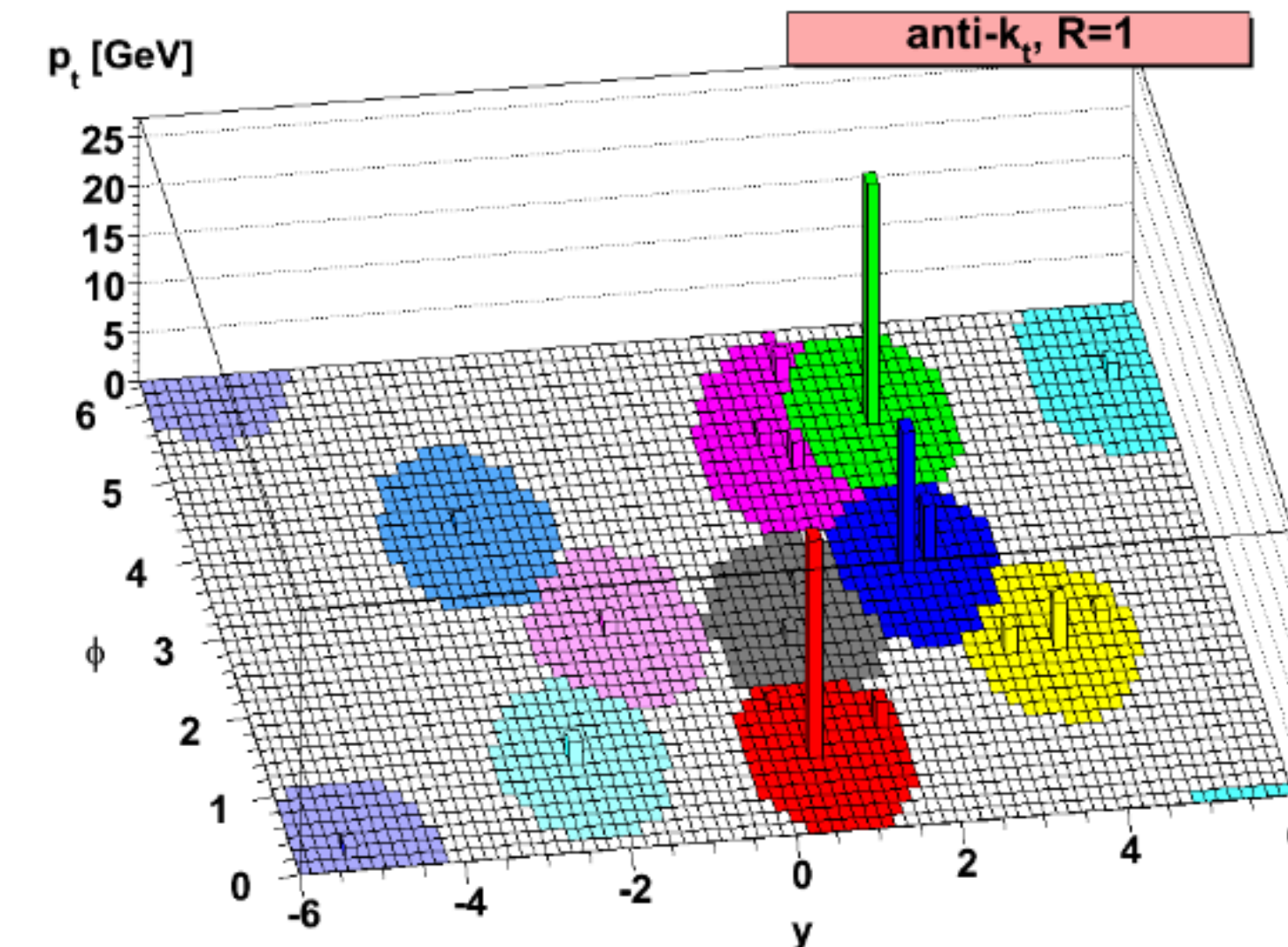
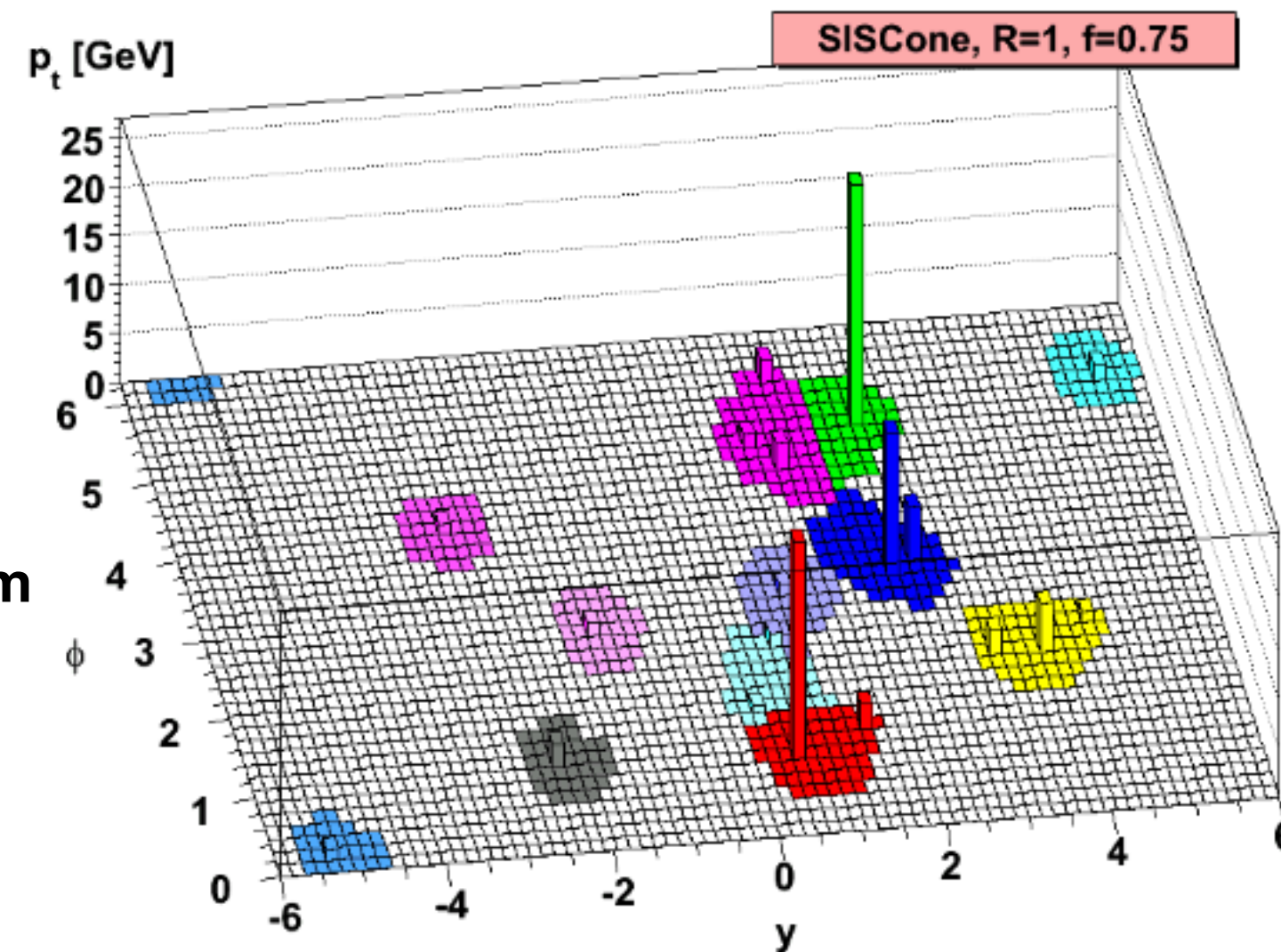
Source: S Catani

Jet reconstruction

kt algorithm (soft particles first)
→ patchwork

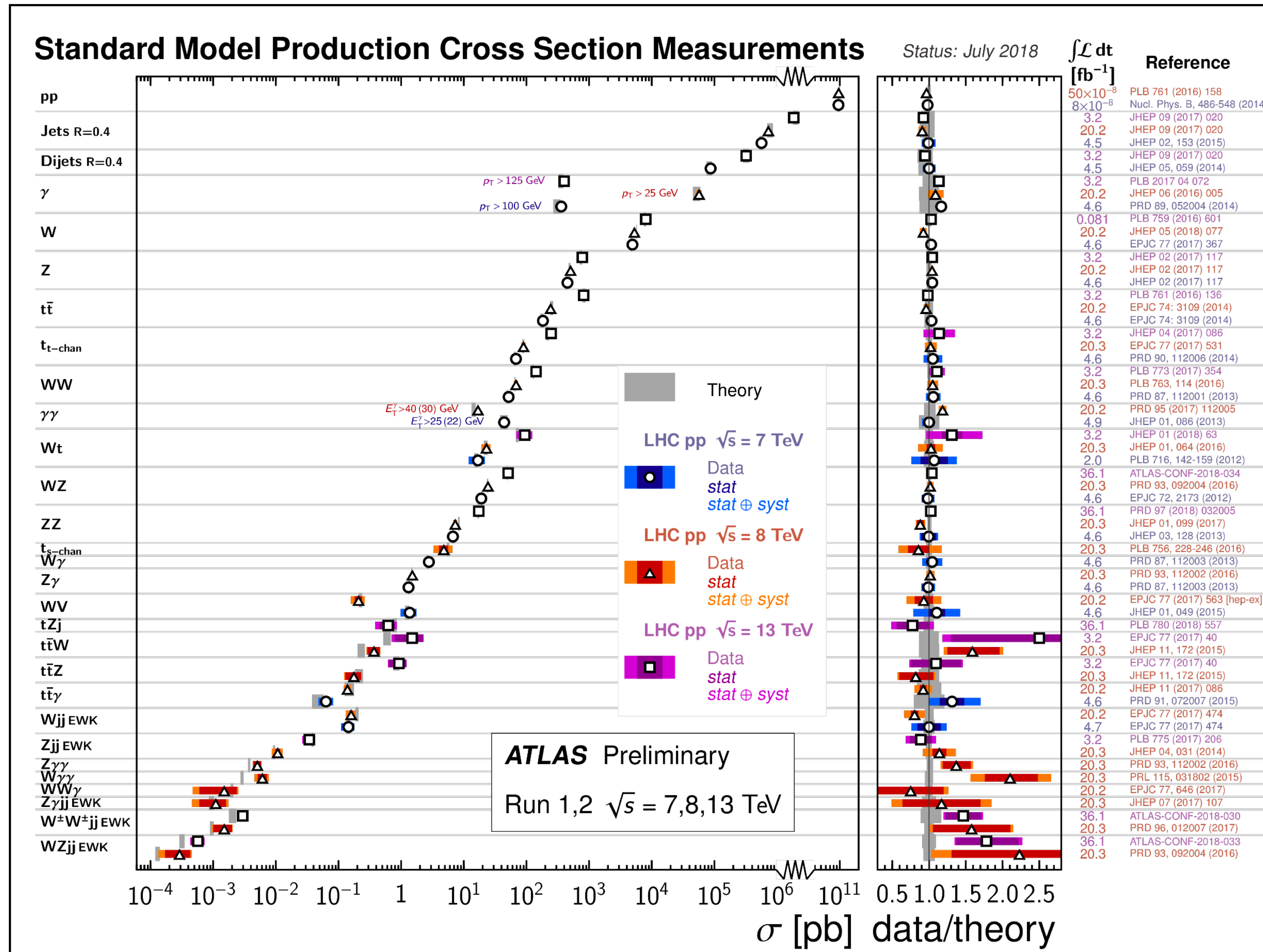


Advanced cone algorithm
→ jets cone-shaped



anti kt algorithm
→ jets cone-shaped

Jet cross section at the LHC



Jet production at the LHC

Total cross section

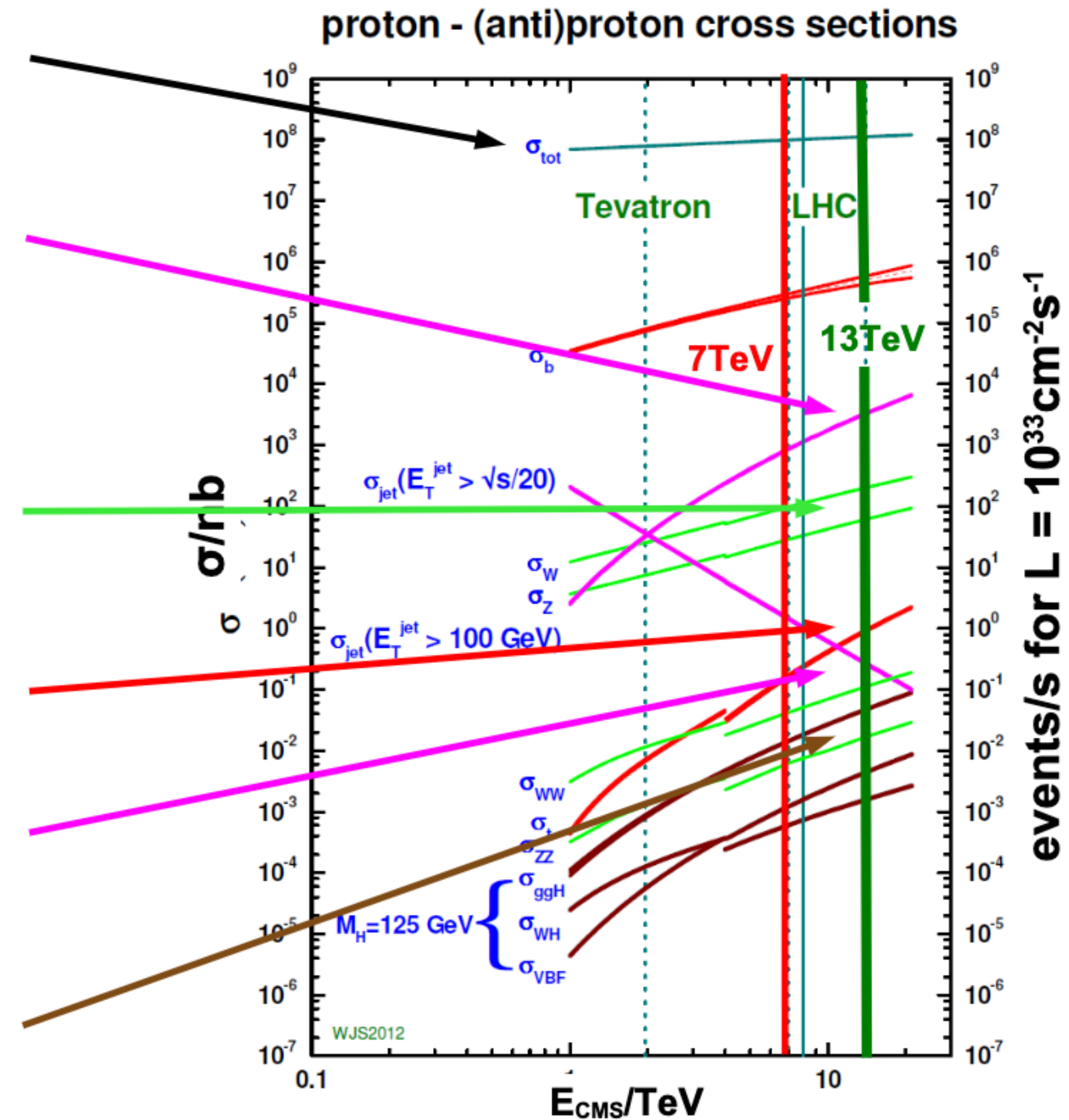
Jets: $\sigma_{\text{jet}}(E_T^{\text{jet}} > 100\text{GeV})$
 $\sim 2000 / \text{s}$

W & Z bosons: σ_W, σ_Z
 $\sim 200 / \text{s}, 50 / \text{s}$

Top quarks (σ_{tt})
 $\sim 1 / \text{s}$

Jets: $\sigma_{\text{jet}}(E_T^{\text{jet}} > 650\text{GeV})$
 $\sim 18 / \text{min}$

Higgs Bosons ($\sigma_{ggH}, \sigma_{WH}, \sigma_{VBF}$)
 $\sim 150 / \text{h}$



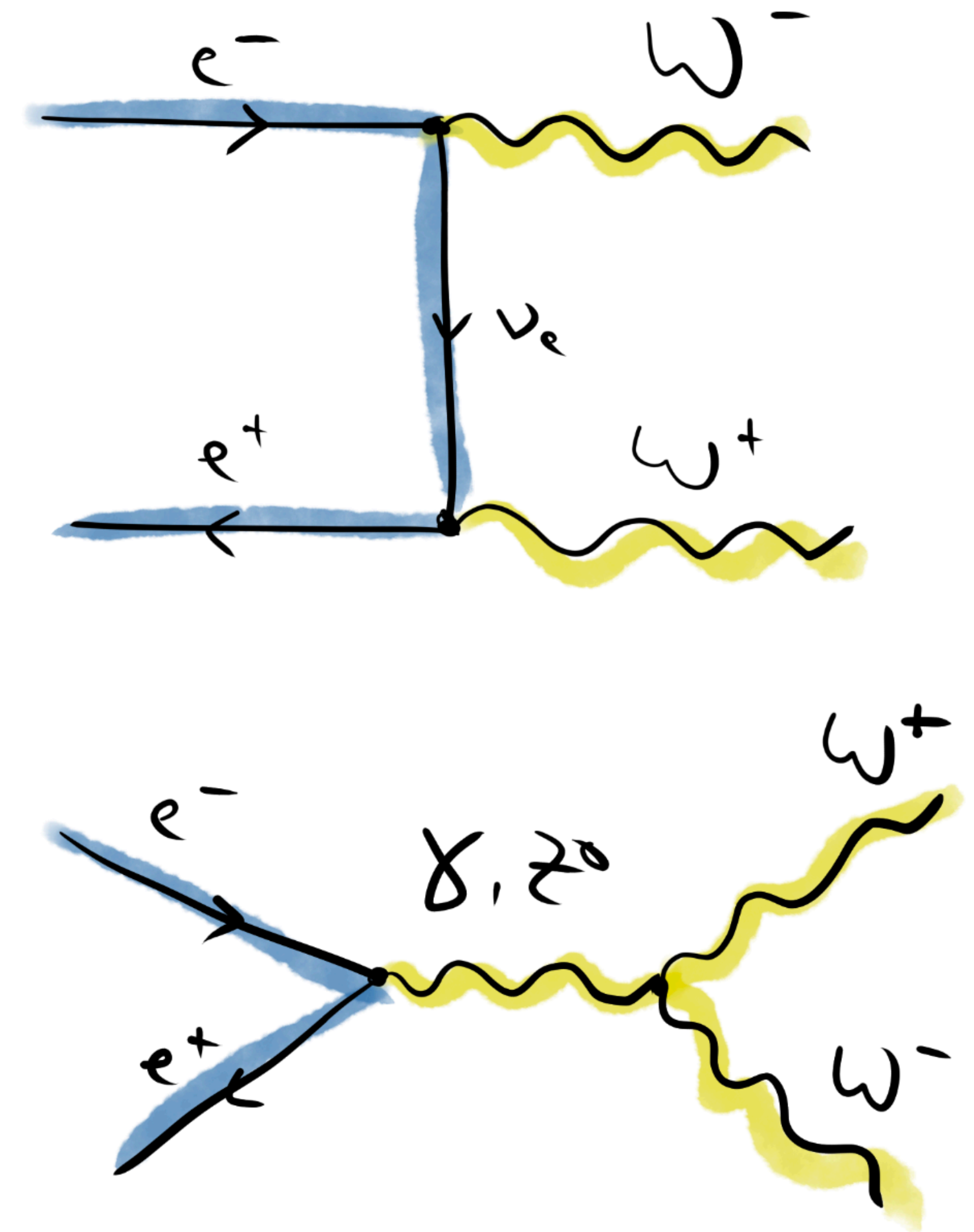
Credit: W. Stirling

W-production at LEP2 (not at LEP!)

- Kinematic production threshold:

$$\sqrt{s} \geq 2m_W$$

- **Threshold scan:** measure cross section as a function of $\sqrt{s}$ (scan of beam energies) $\rightarrow$ scattering matrix only unitary if both neutrino exchange and triple gauge boson (ZWW) vertex are considered



W decays

■ Leptonic decay: $W \rightarrow \ell \nu_\ell$

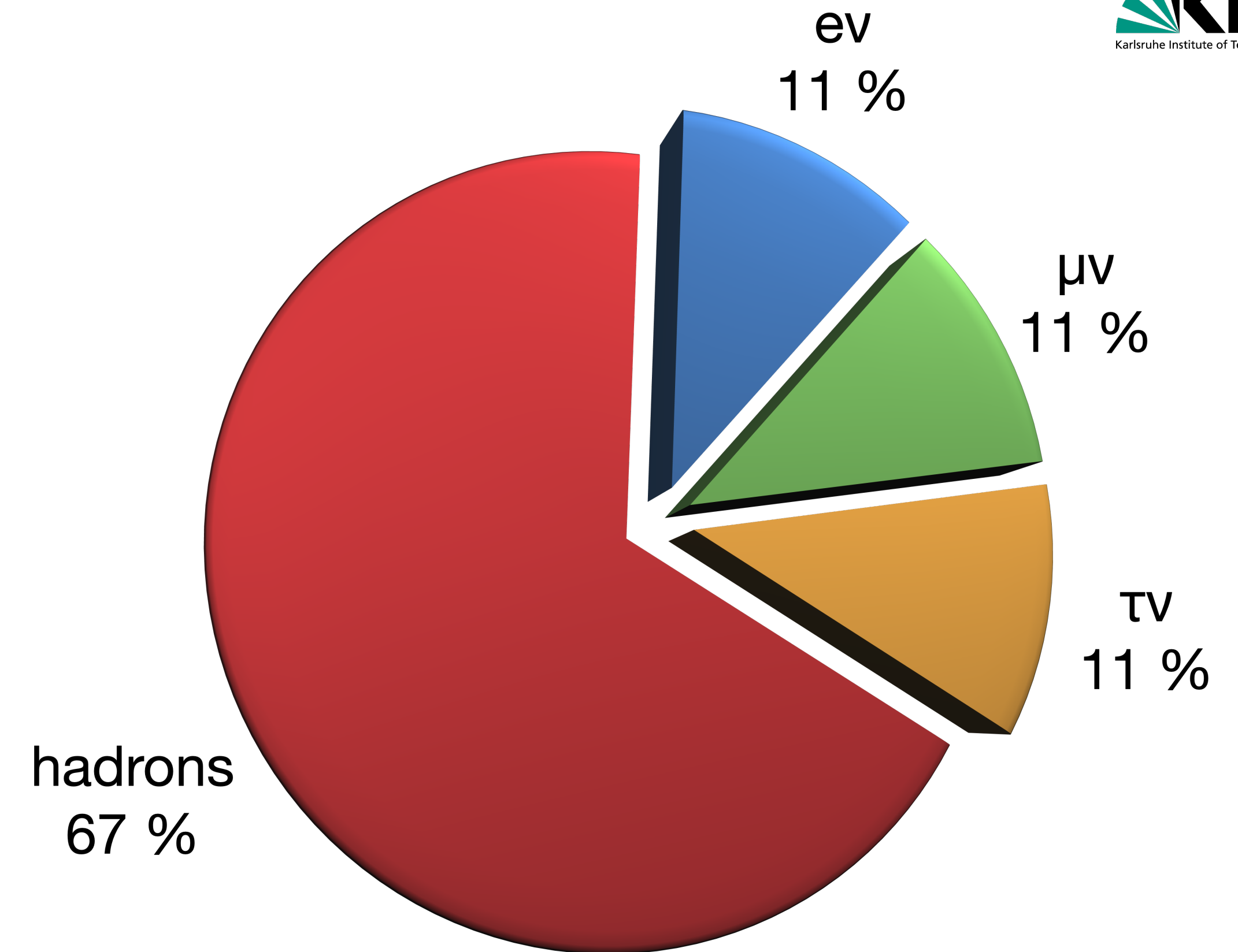
- Neutrino: missing transverse momentum
- $\ell = e, \mu$: experimentally very clean
- $\ell = \tau$: hadronic τ -decays $\rightarrow$ complicated

■ Hadronic decay $W \rightarrow q \bar{q}$

- Large QCD multijet background $\rightarrow$ complicated

■ Isolated leptons are a clean experimental signature of W or Z decay

■ QCD jets contain mostly non-isolated leptons from heavy quark decays inside the jet





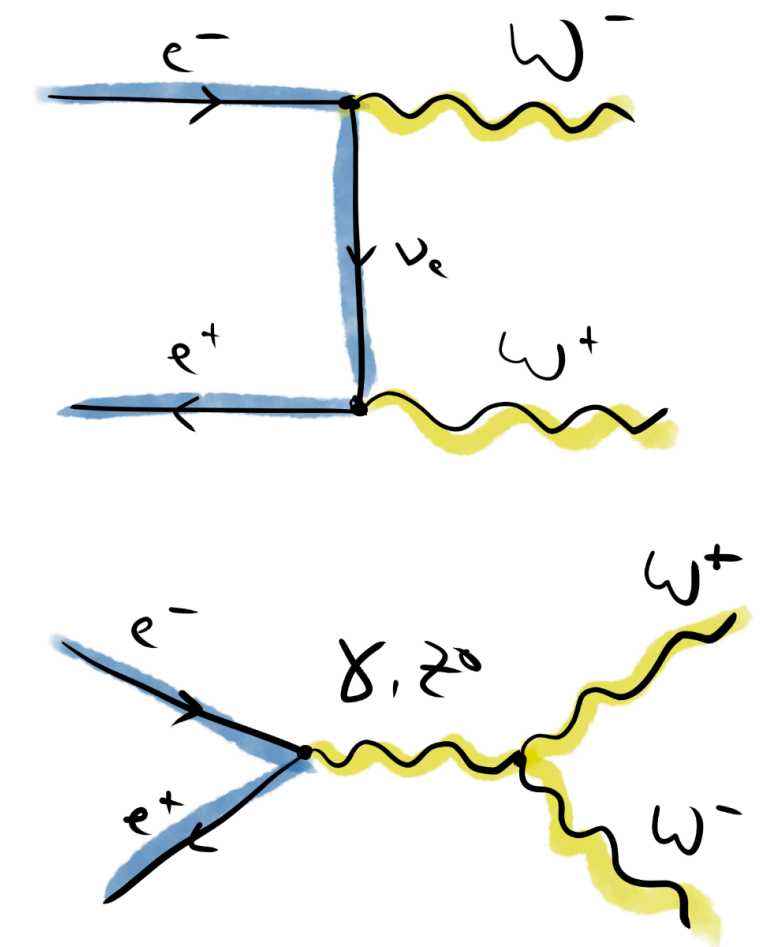
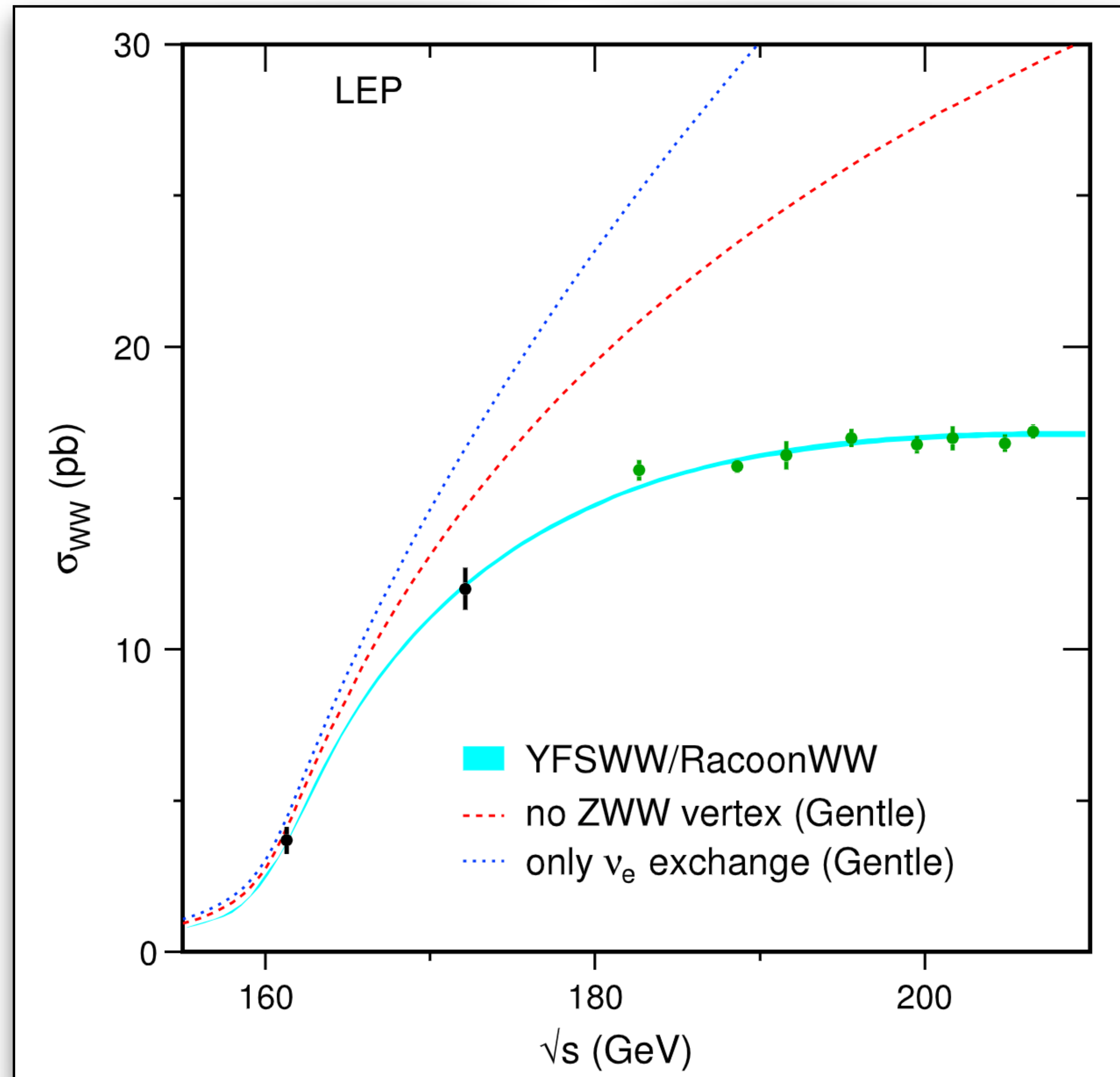
■ PINGO:

- Umfrage: Teilchenphysik 1 (WS 23/24)
- Zugangsnummer: 434521
- Link: <https://pingo.coactum.de/events/434521>

- Why is QCD jet production expected to be the most important background for the decay $W \rightarrow l\nu$?
 - Jets may be misidentified as charged leptons.
 - Jets always contain charged leptons.
 - Often QCD jet events contain large missing transverse momentum.
 - Detector noise may “fake” missing transverse momentum.
 - The production cross sections for W bosons and QCD jets are approximately of equal size.

- Why is QCD jet production expected to be the most important background for the decay $W \rightarrow l\nu$?
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 - The production cross sections for W bosons and QCD jets are approximately of equal size.

W-production at LEP2 (not at LEP!)

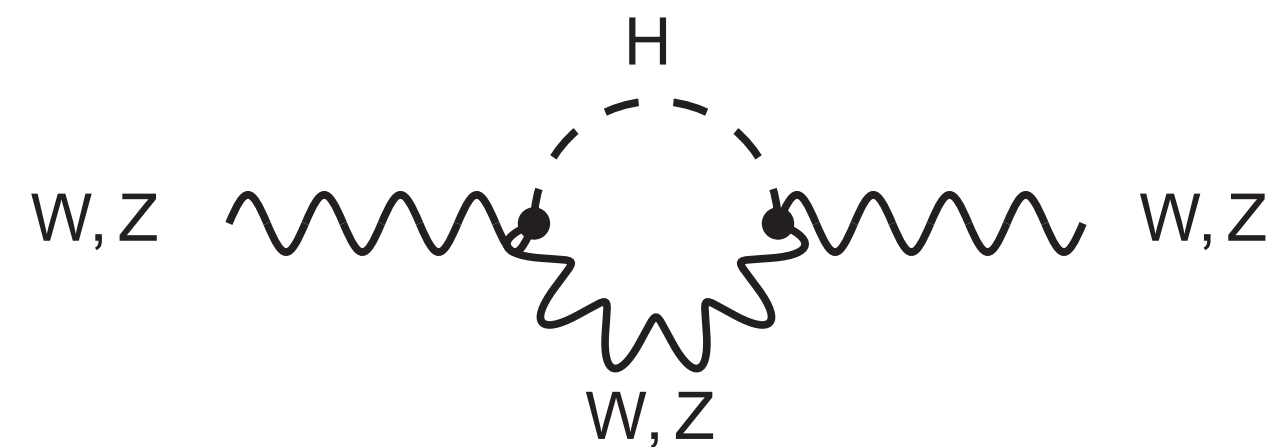


Indirect W properties

- W and Z boson masses related through **weak mixing angle**:

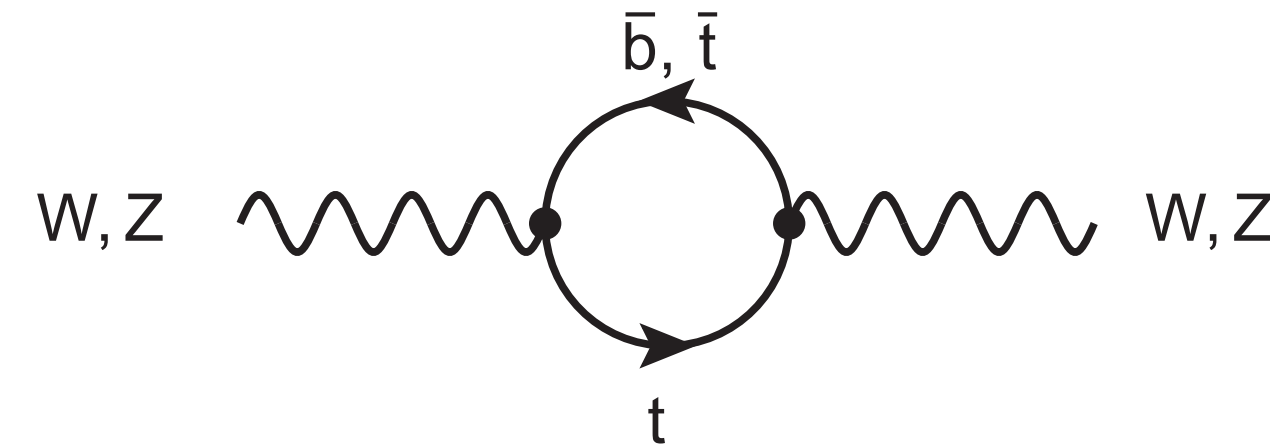
$$m_W^2 = \frac{g^2 v^2}{4}, m_Z^2 = \frac{v^2}{4}(g^2 + g'^2), \rho_0 = \frac{m_W^2}{m_Z^2 \cos \theta_W} = 1$$

- Relation with top-quark and Higgs-boson masses through loop corrections, e.g. W and Z boson “**self energy**”



$$\sim g' \ln(m_H / m_W)$$

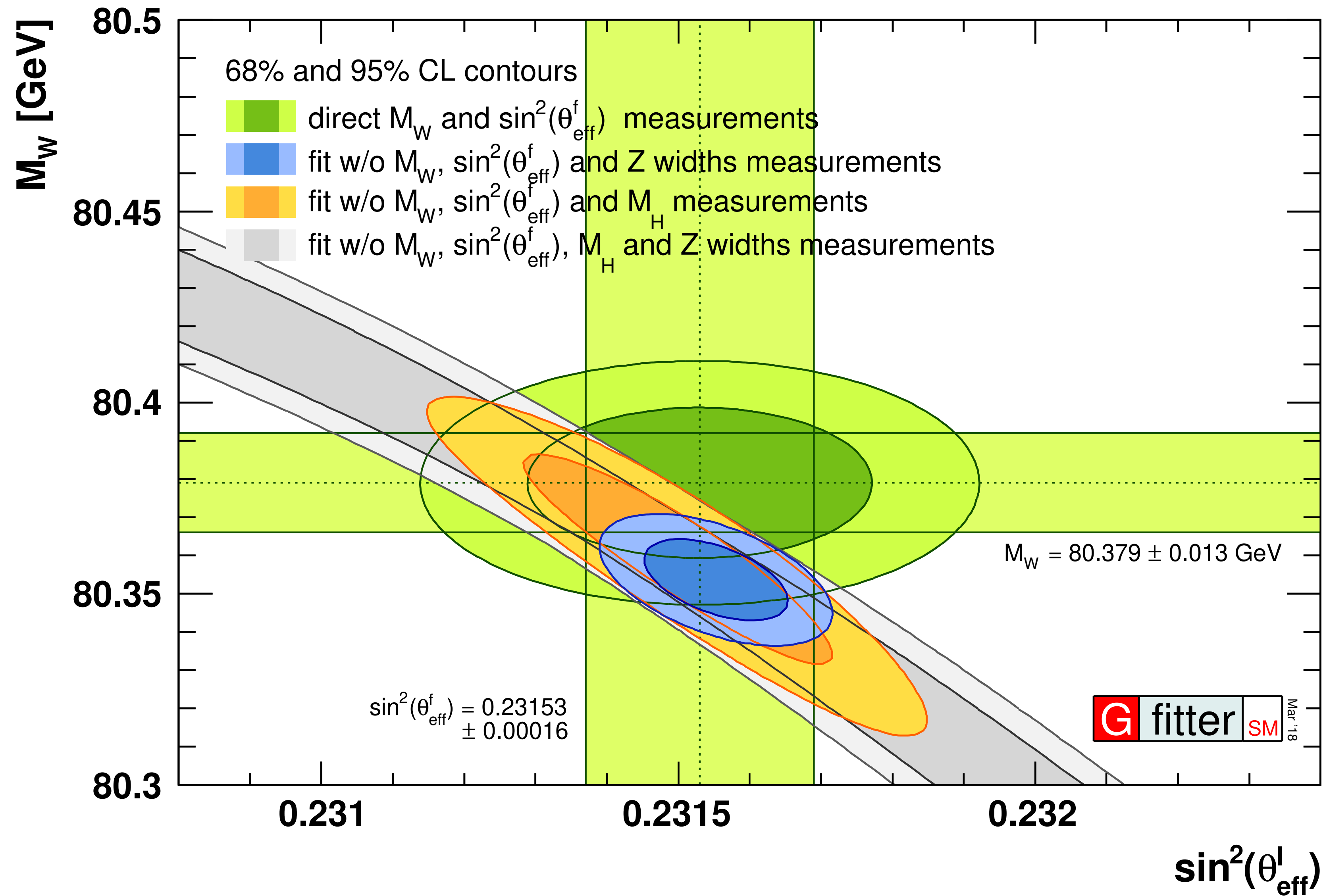
Weak dependence
(logarithmic)



$$\sim G_F m_t^2$$

Strong dependence
(quadratic)

Indirect W properties

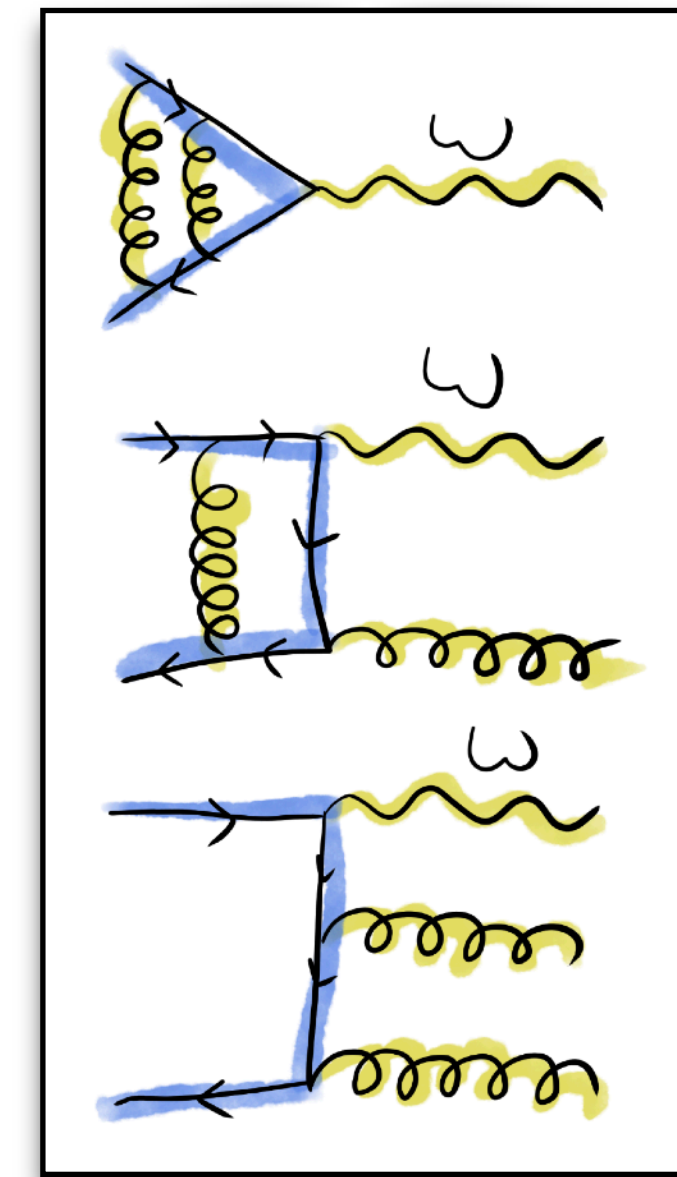
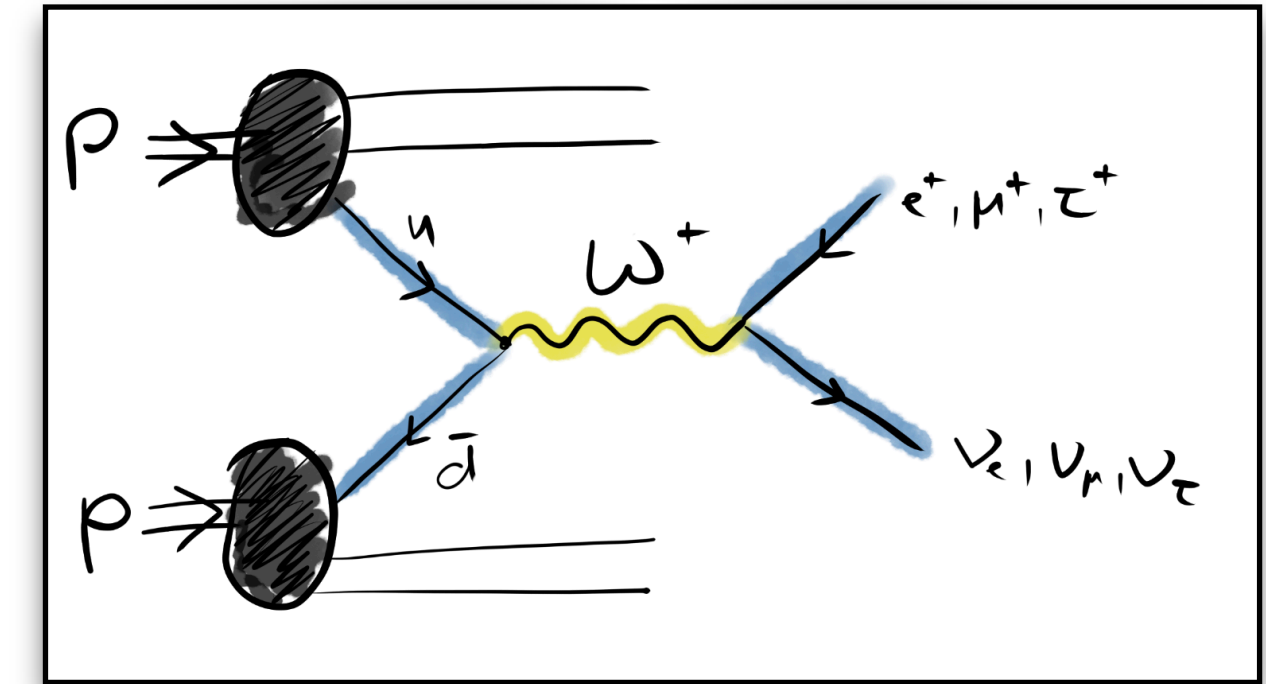


Differential W production cross section

- W boson production via quark-antiquark annihilation
- Partonic cross section (leading order):

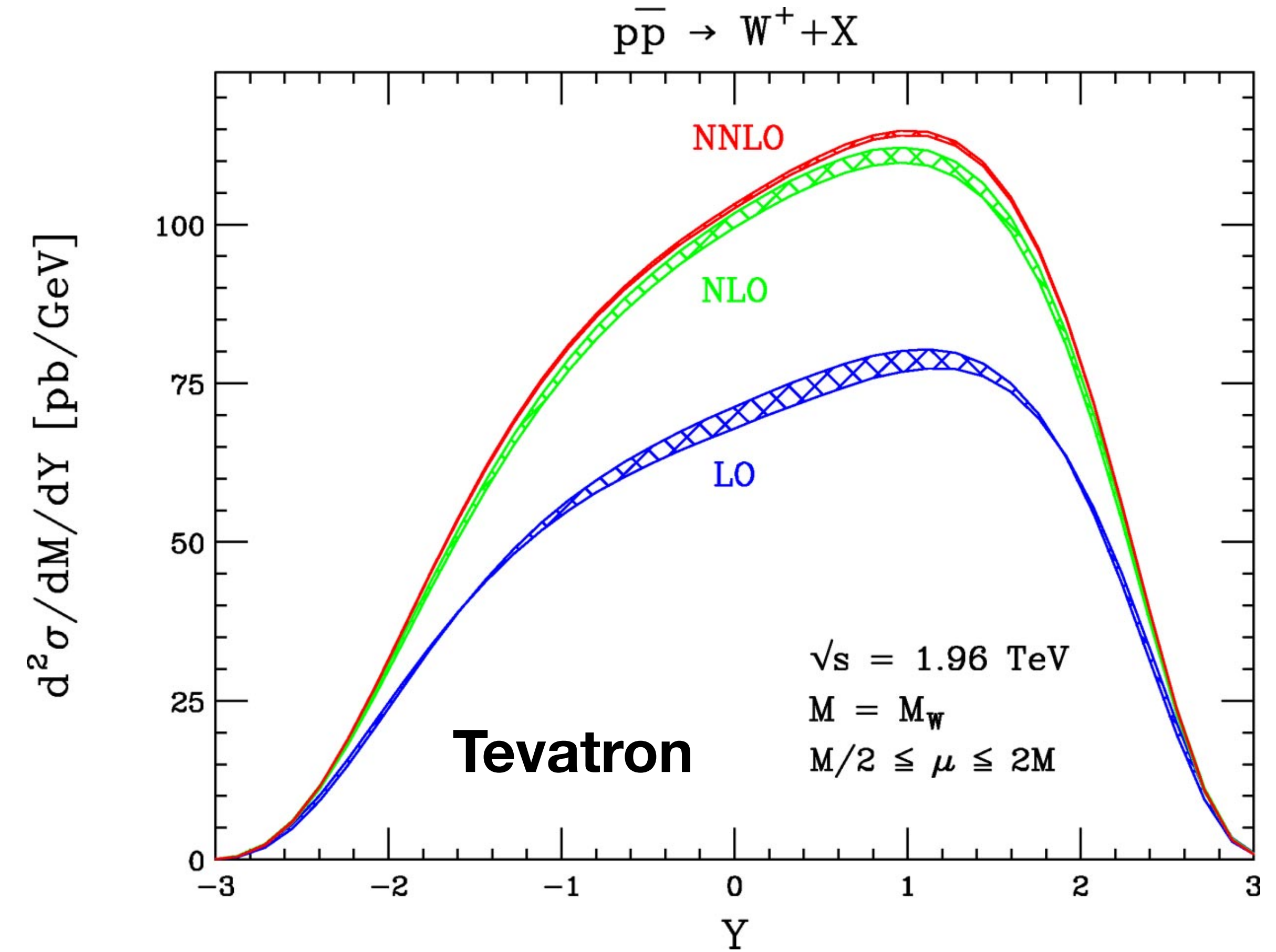
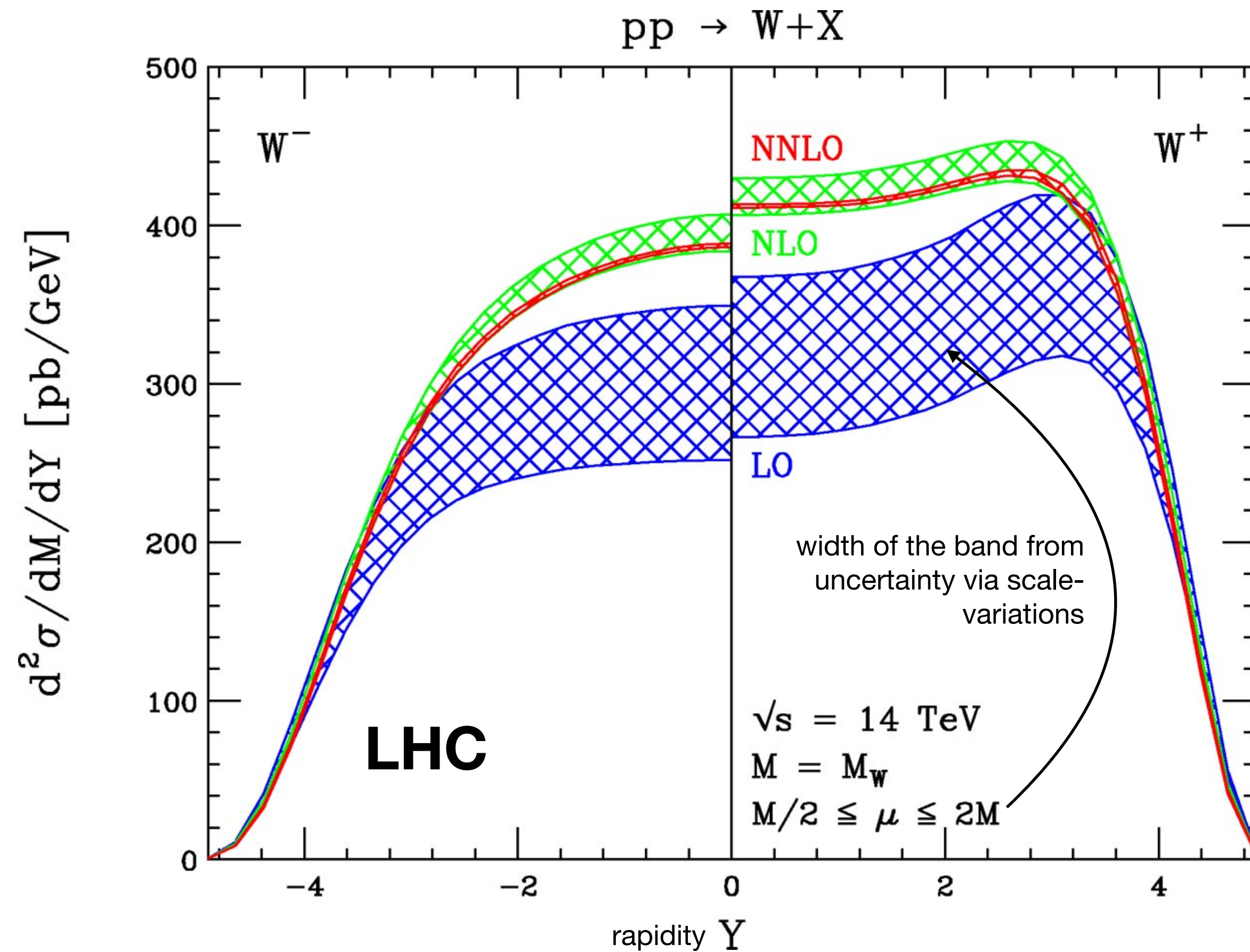
$$\hat{\sigma}(q\bar{q}' \rightarrow W) = \frac{\pi}{3} \sqrt{2} G_F m_W^2 |V_{q\bar{q}'}|^2 \delta(\hat{s} - m_W^2)$$

- Differential cross sections known theoretically up to next-to-next-to-leading order (NNLO) (next slide)



Differential W production cross section

Source: Phys. Rev. D 69, 094008 (2004)



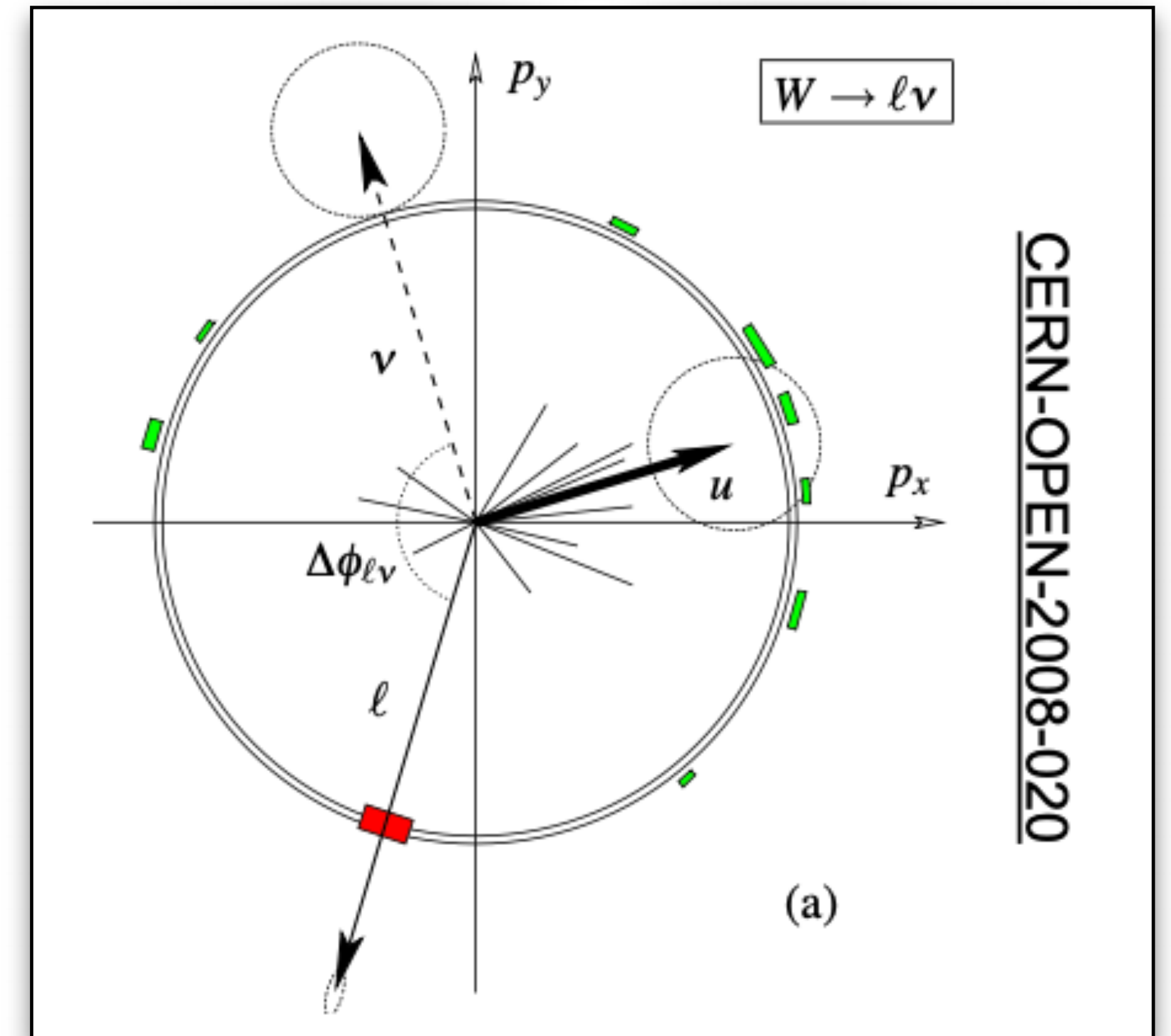
W^+ preferably moving in proton direction
 W^- (not shown here) preferably moving in antiproton direction

W boson mass at hadron colliders

- Use muonic $W^+ \rightarrow \mu^+ \nu_\mu$ decays
 - Signature: isolated, high-pt lepton
 - Often additional hadronic activity
 - Neutrino is invisible energy
- Define observable “transverse mass”:

$$m_T^2 = (E_T^\ell + E_T^\nu)^2 - (\vec{p}_T^\ell + \vec{p}_T^\nu)^2$$

$$\approx 2 |\vec{p}_T^\ell| |\vec{p}_T^\nu| (1 - \cos \Delta\phi_{\ell\nu})$$



W boson mass at hadron colliders

- Exploit significant feature in kinematic distributions: **Jacobian edge**

- Two-body decay kinematics:

- $p_T^\ell = p_T^\nu = \frac{m_W}{2} \sin \theta$

- $\cos \Delta\phi_{\ell\nu} = -1$ (“back-to-back”, 180°)

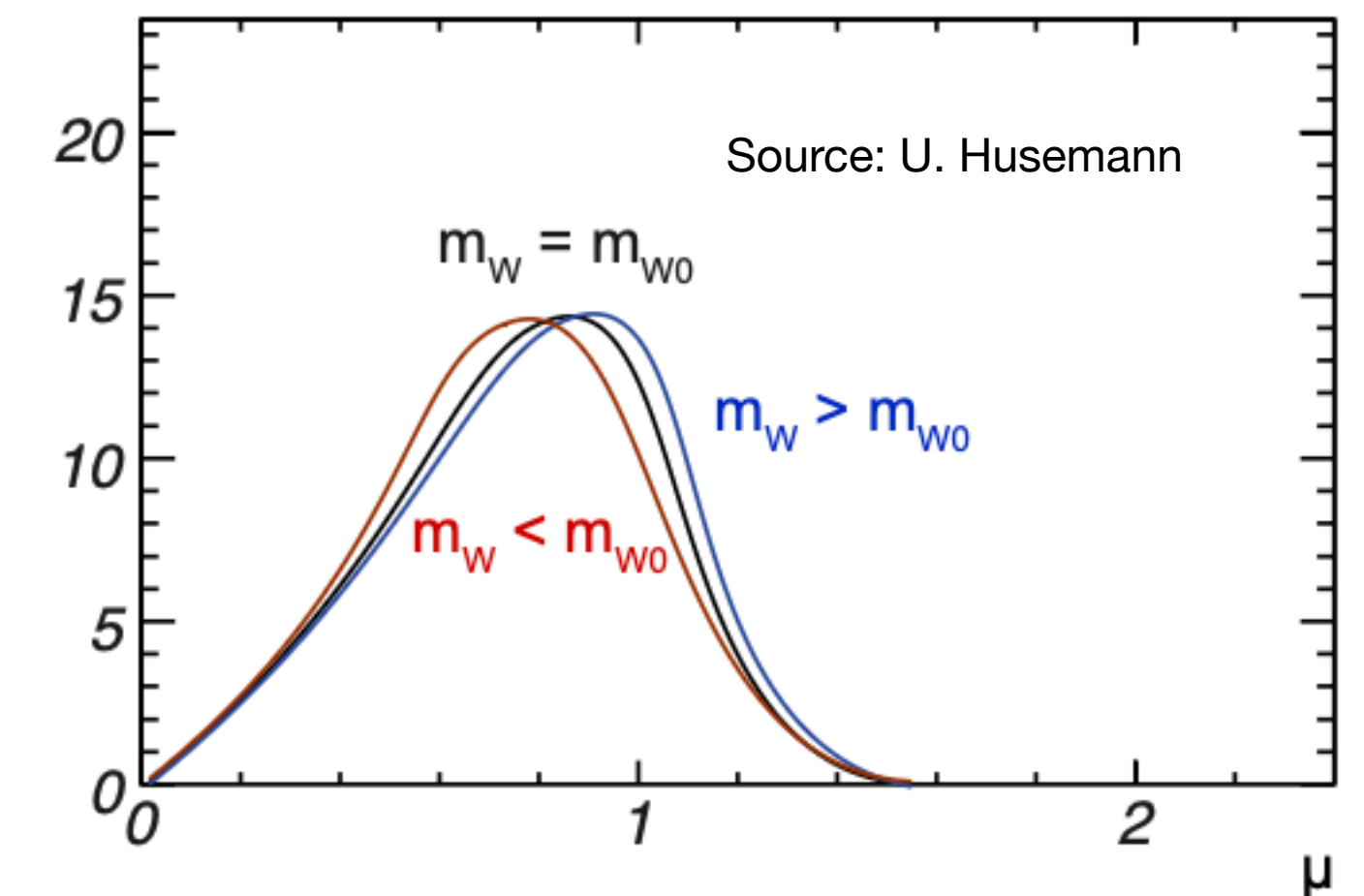
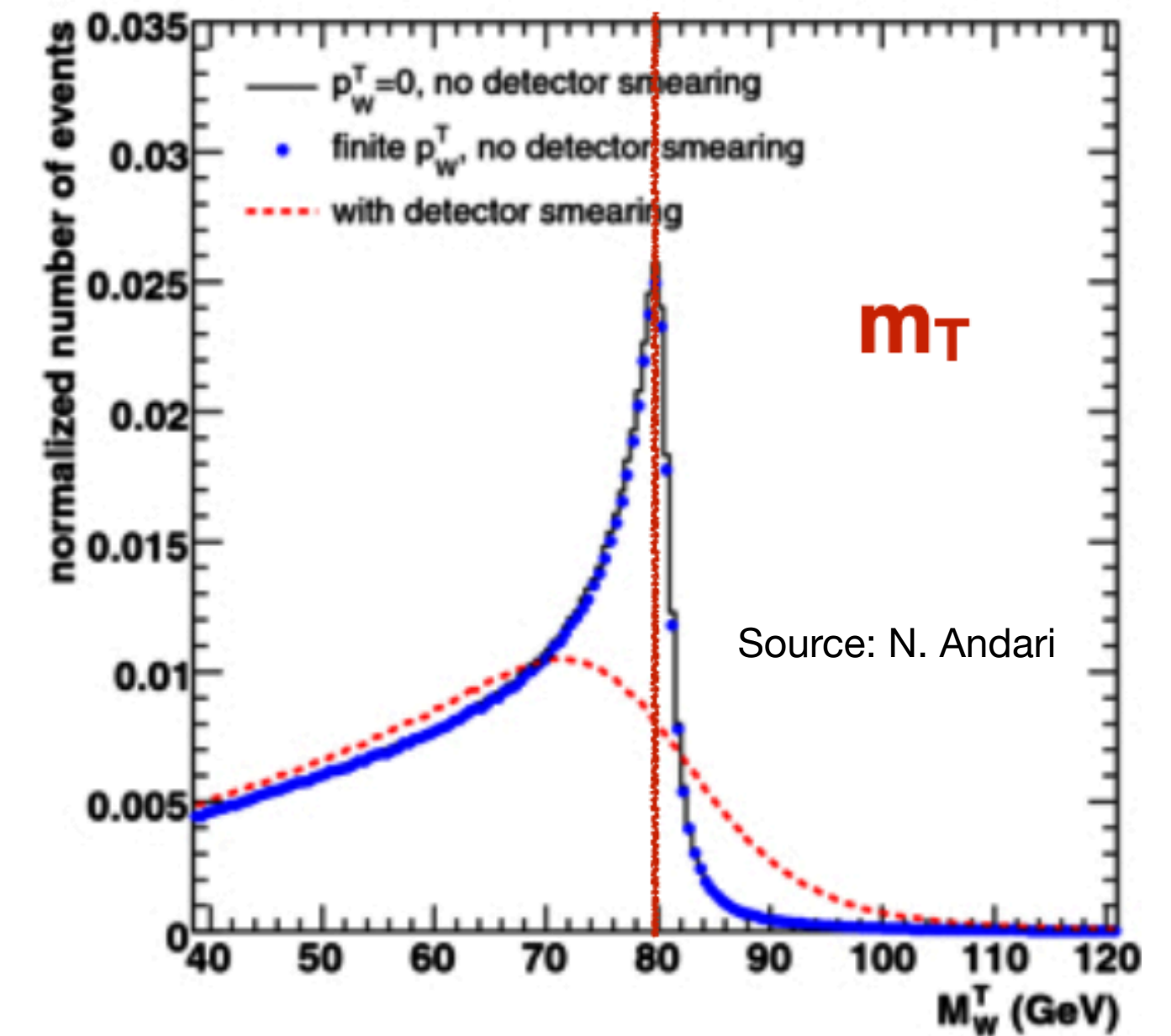
- $m_T^2 \approx 2 |\vec{p}_T^\ell| |\vec{p}_T^\nu| (1 - \cos \Delta\phi_{\ell\nu})$

- $\rightarrow m_T = m_W \sin \theta$, define $\mu = \frac{m_T}{m_W}$ and with $\cos^2 \theta = 1 - \sin^2 \theta \rightarrow \cos \theta = \sqrt{1 - \mu^2}$

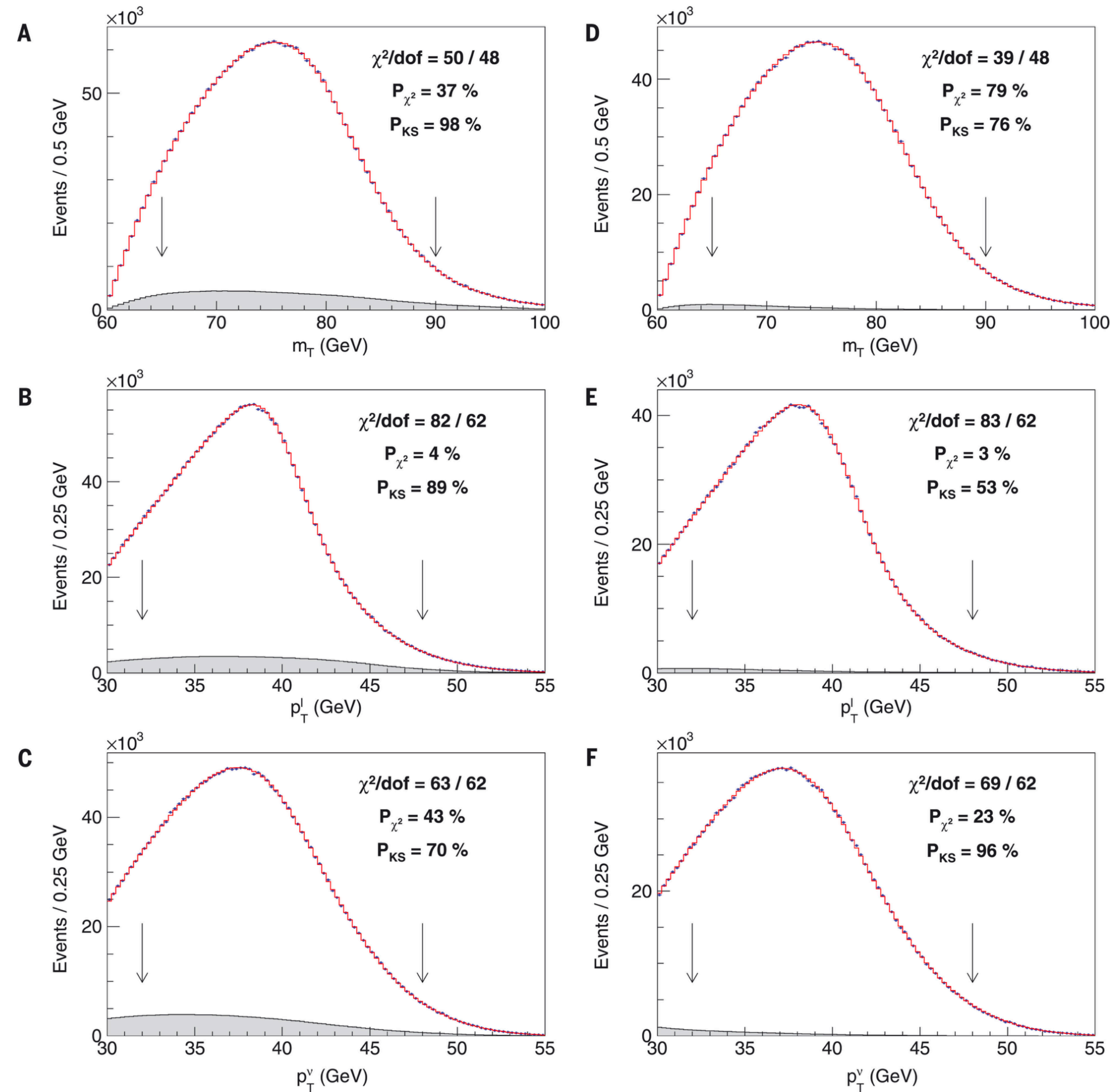
- $$\frac{d\sigma}{d\mu} = \frac{d\sigma}{d\cos\theta} \left| \frac{d\cos\theta}{d\mu} \right| = \frac{d\sigma}{d\cos\theta} \left| \frac{d\sqrt{1-\mu^2}}{d\mu} \right| = \frac{d\sigma}{d\cos\theta} \left| \frac{-\mu}{\sqrt{1-\mu^2}} \right|$$

W boson mass at hadron colliders

- Finite W-width (~ 2 GeV) and detector effects smear peak significantly
- Analysis: Maximum-likelihood fit used templates (from full detector simulations) for different W masses
- Precision traditionally limited by systematic effects (at CDFII statistical uncertainty $\sim$ systematics)

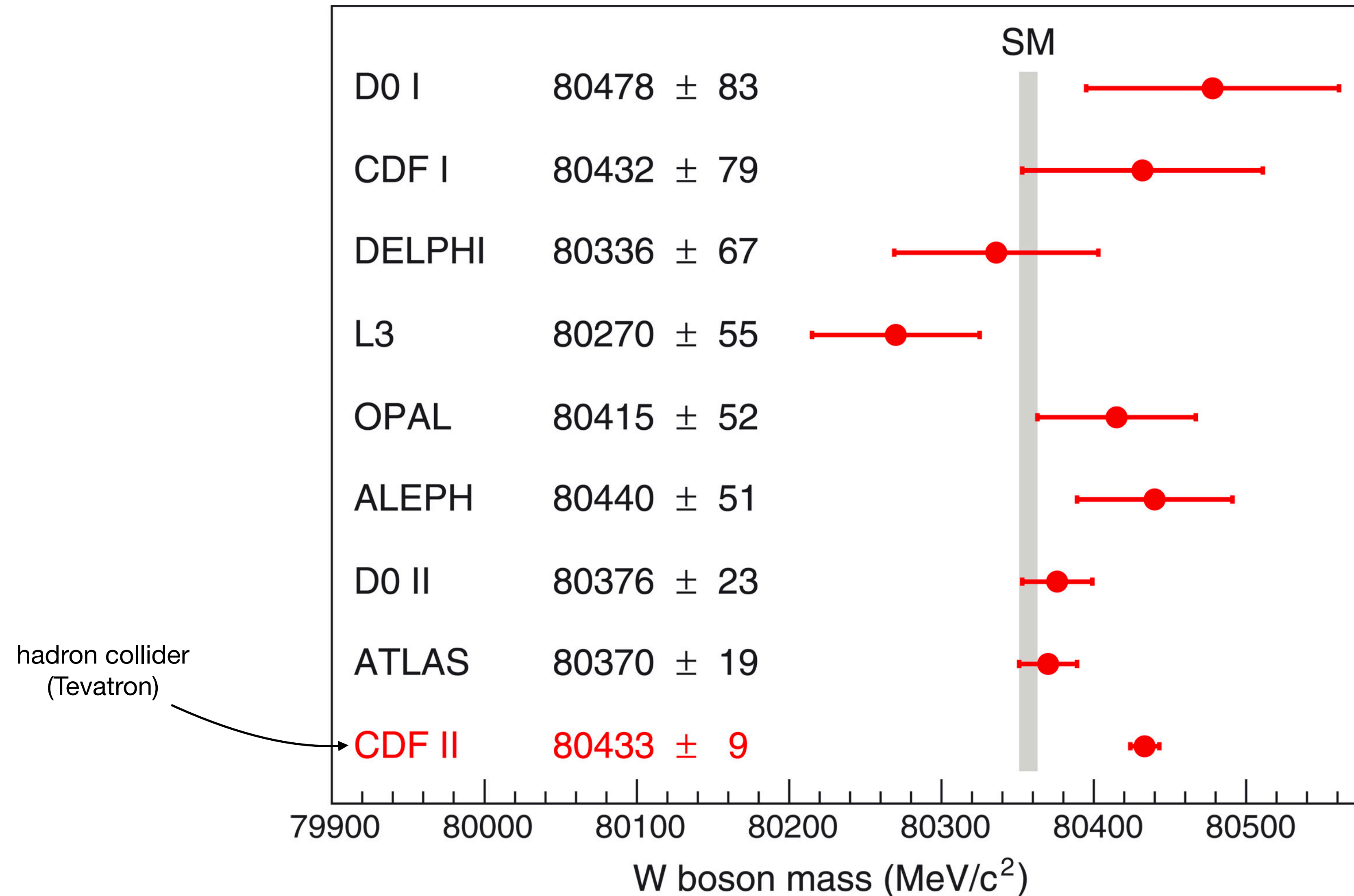


W boson mass at hadron colliders



Source: <https://www.science.org/doi/10.1126/science.abk1781>

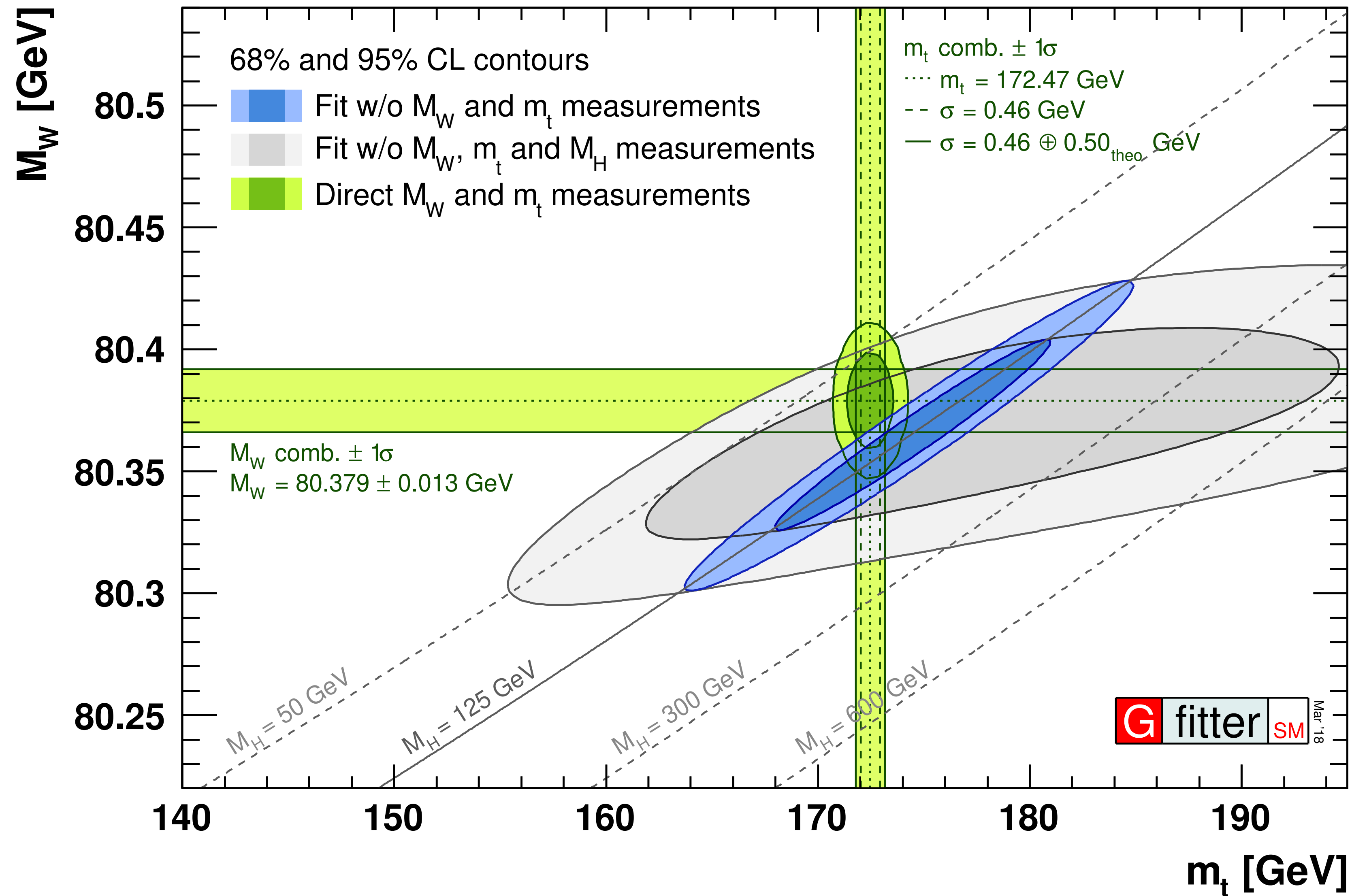
W boson mass summary



Top quark

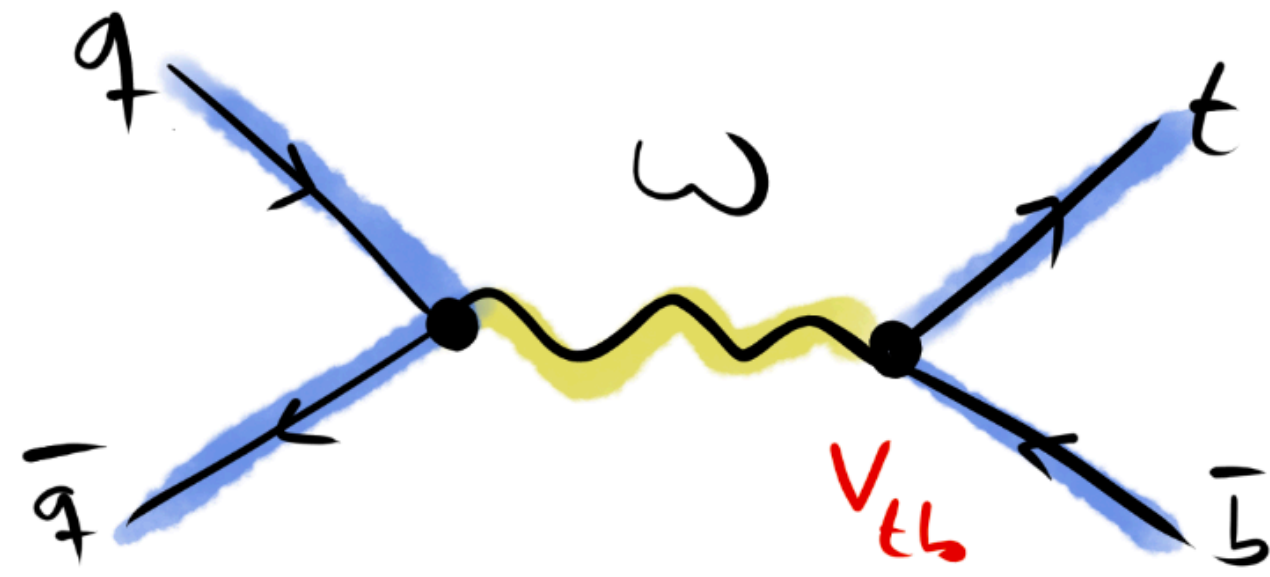
- 1973: three quark generations required for CP violation (Kobayashi & Maskawa)
- 1977: bottom quark discovery → first third-generation quark
- 1980s: search for “light top quarks” in decay $W \rightarrow tb$, indirect hints for “heavy tops” from B-mixing
- 1992: first direct indications for “heavy tops” in decay $t \rightarrow Wb$ at the Tevatron
- 1995: Tevatron experiments CDF and DØ publish discovery of the top quark with a mass of about 175 GeV

Indirect top properties

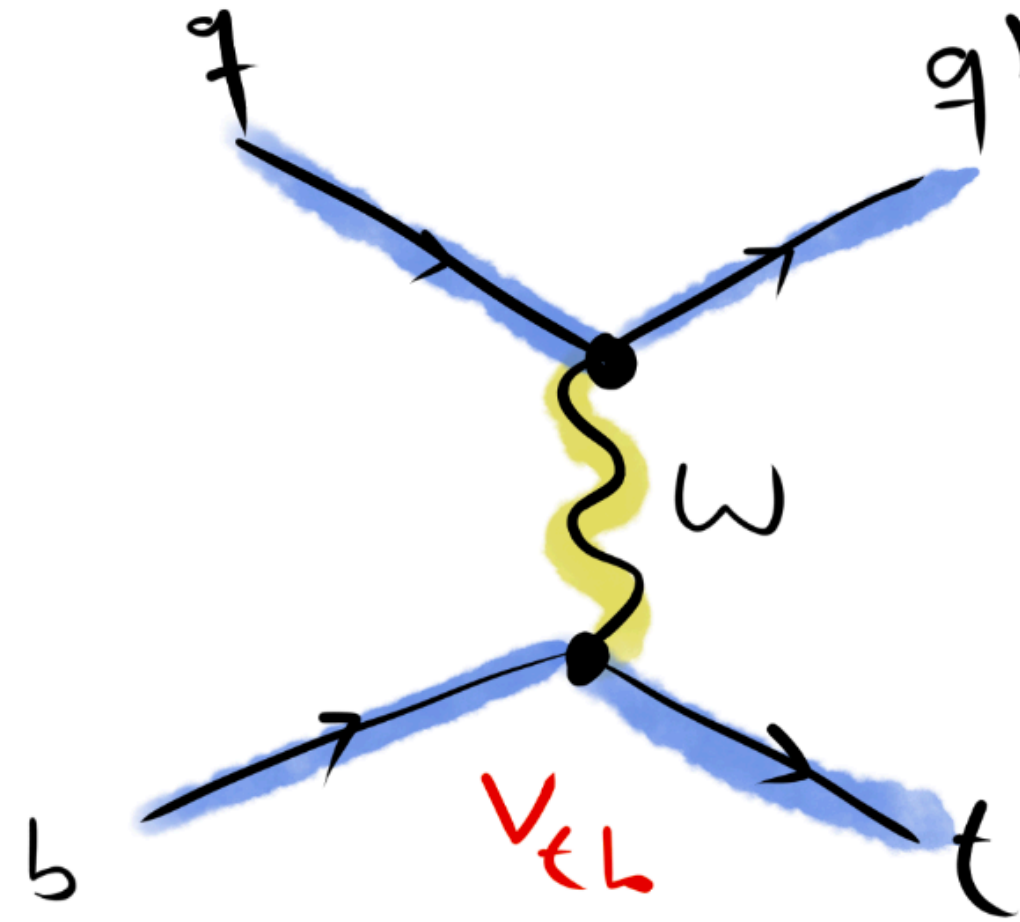


Single top production

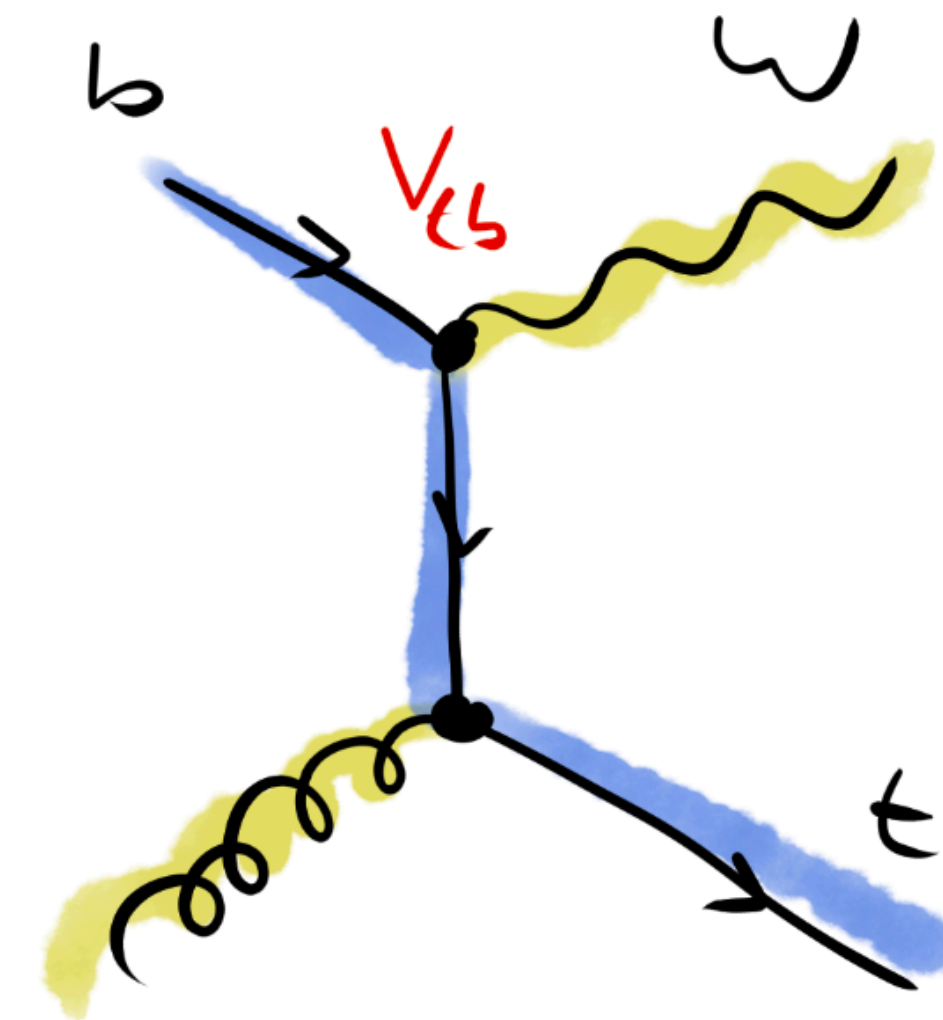
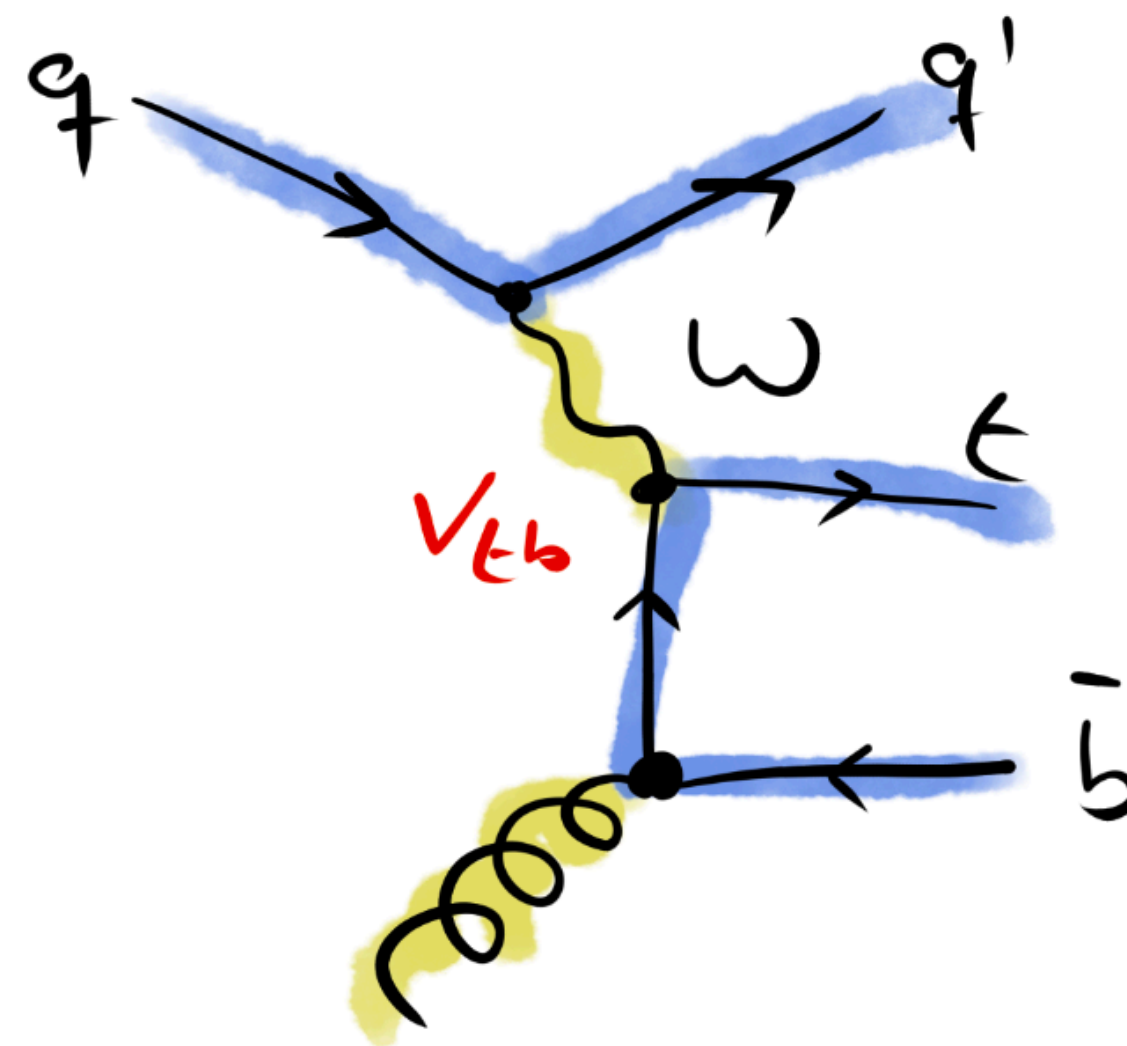
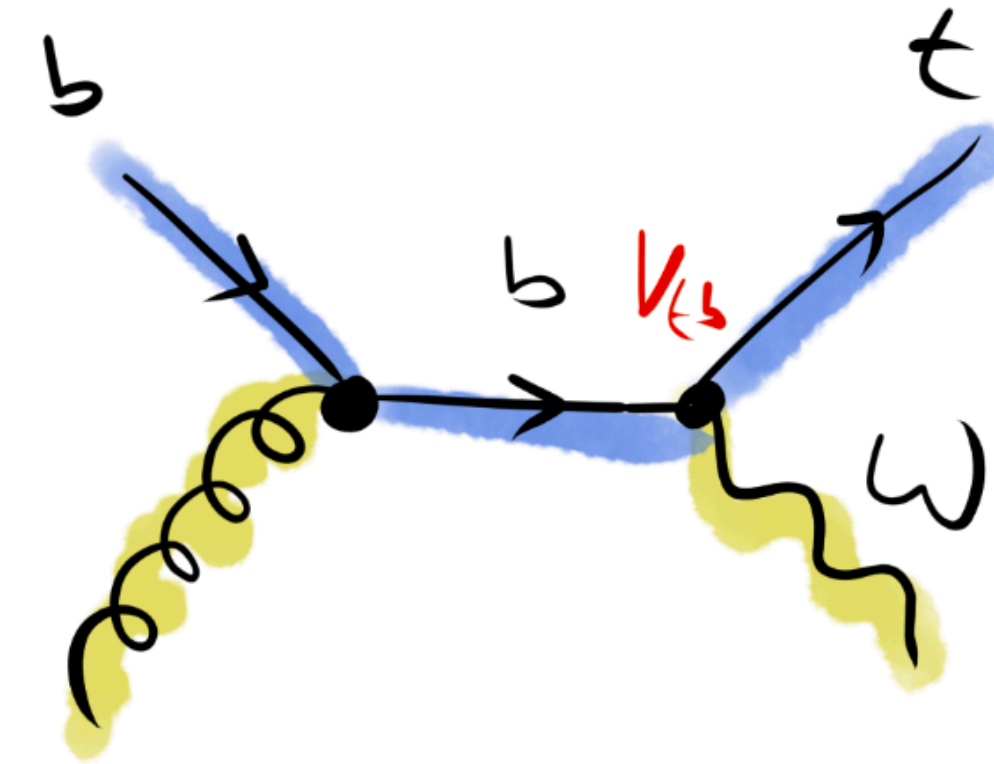
s-channel



t-channel (dominant)

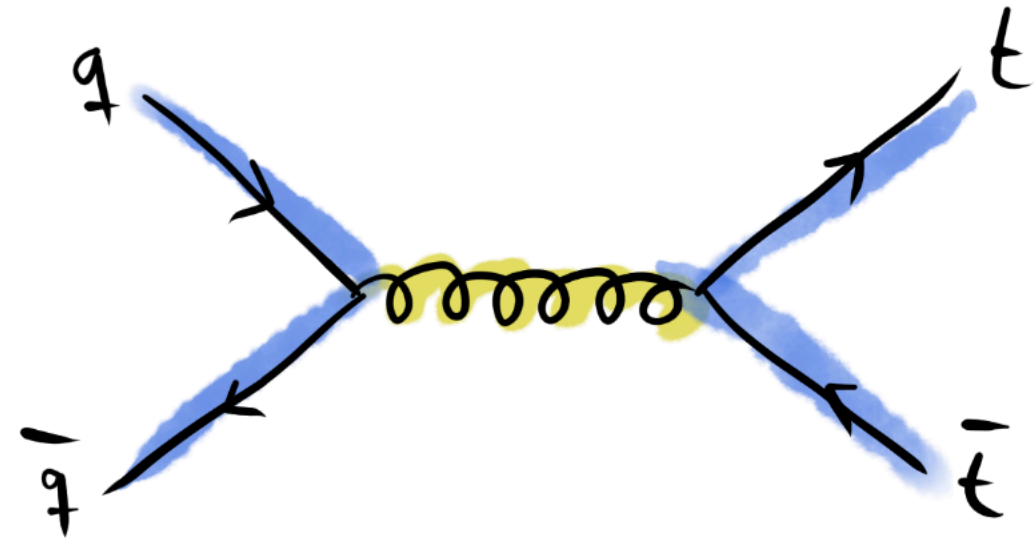


Wt-channel

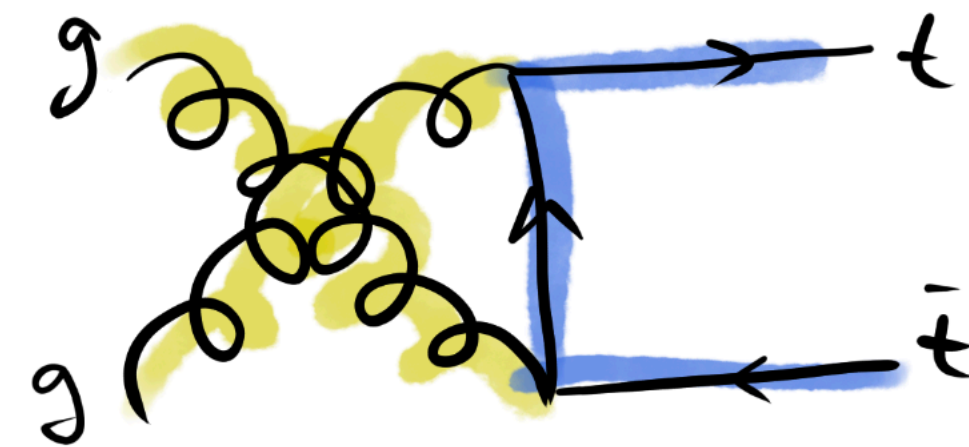
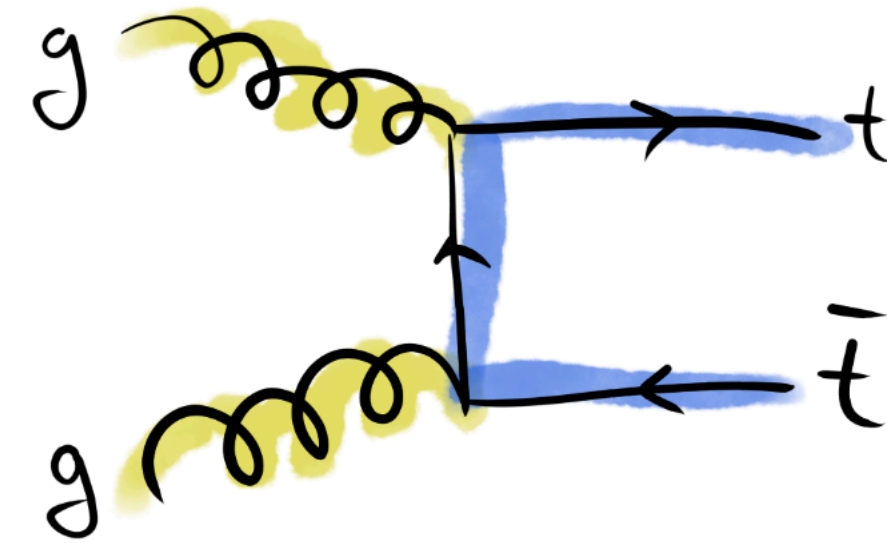
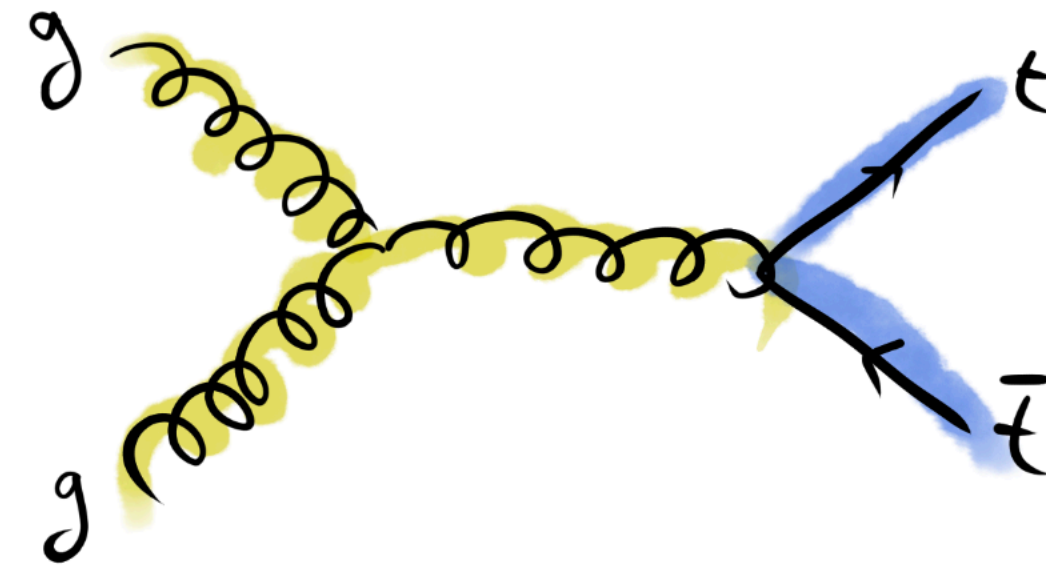


Top pair production

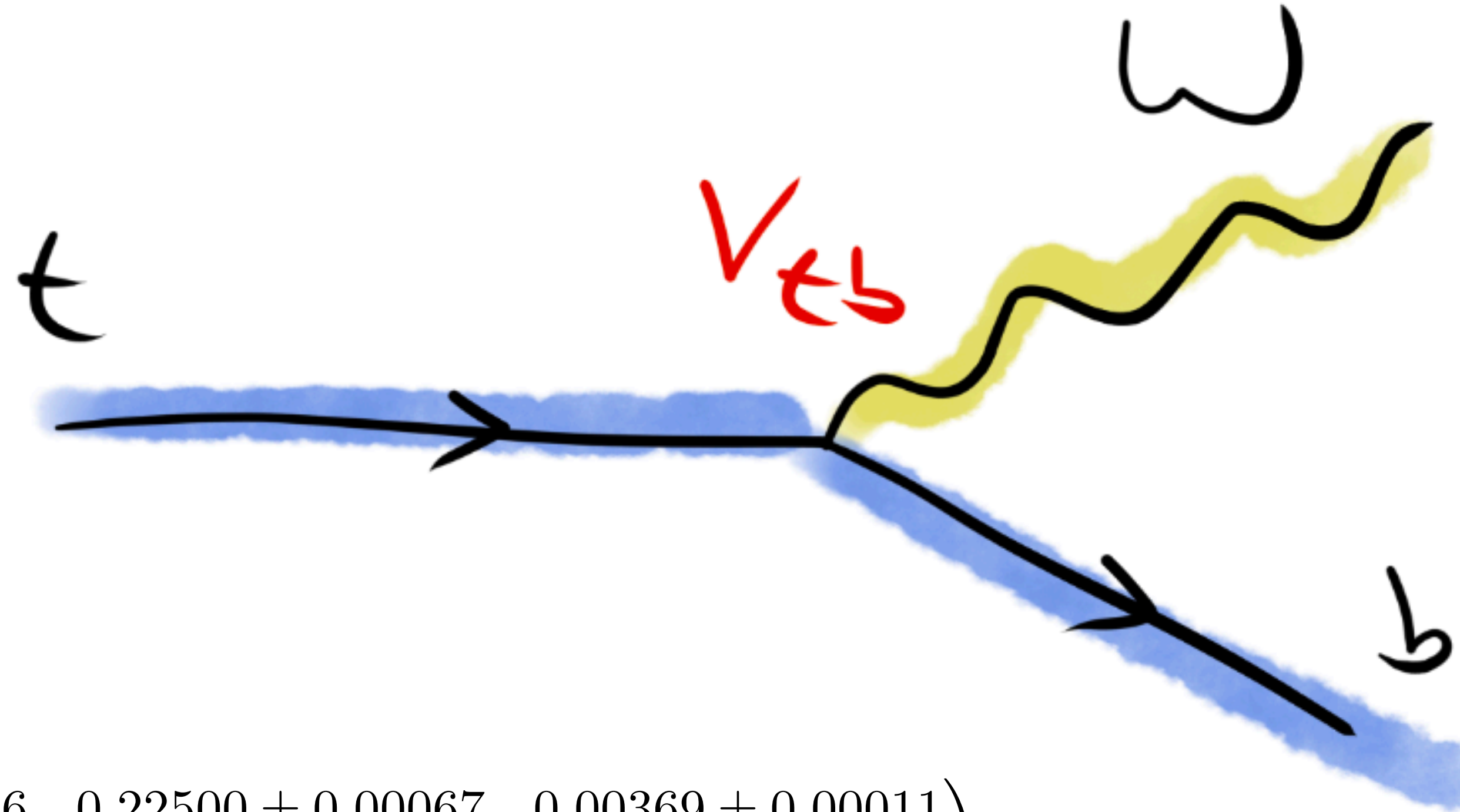
quark -antiquark annihilation (10% at LHC)



gluon-gluon fusion (90% at LHC)



Top decay(s): ~100% via one electroweak decay

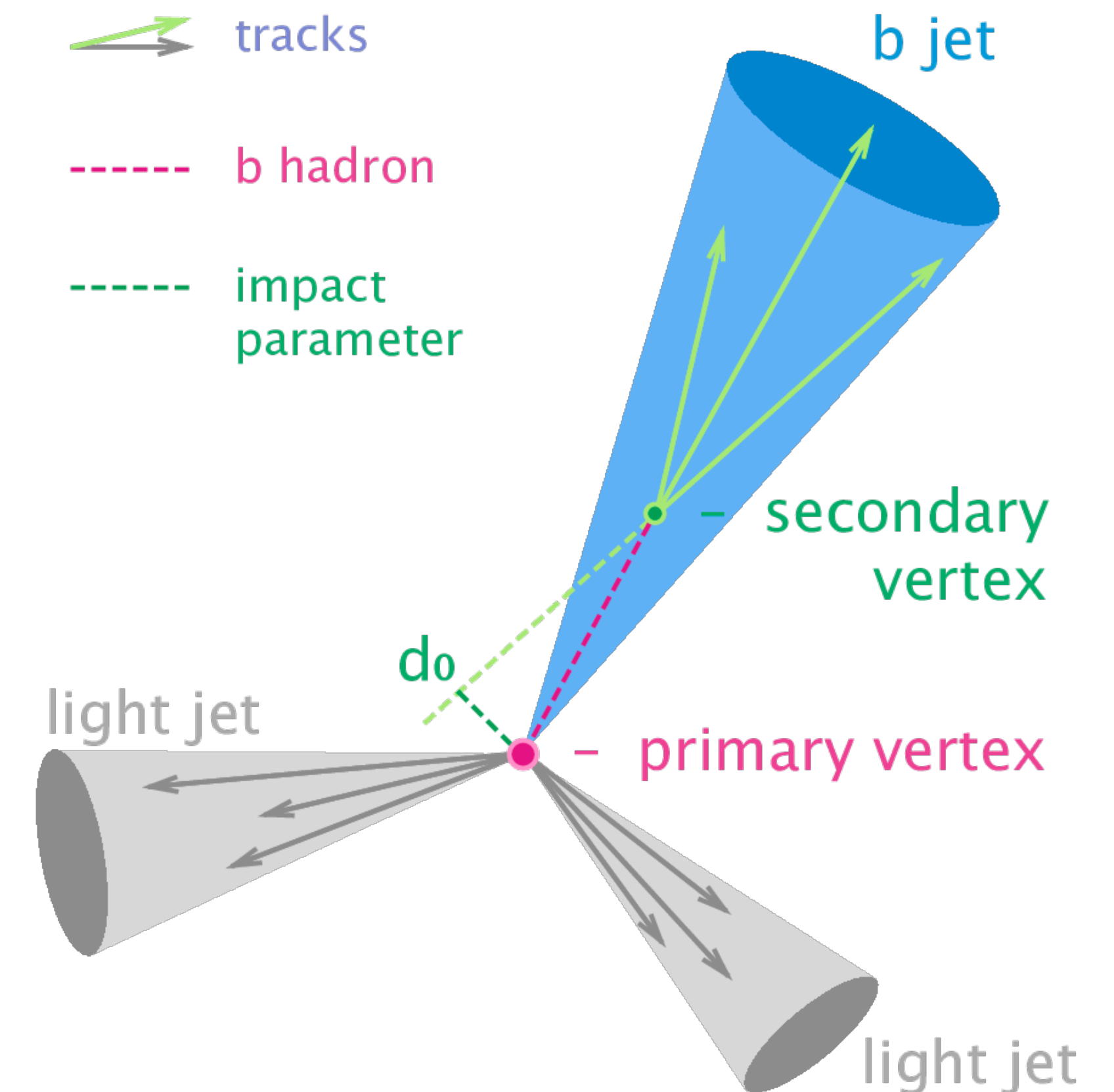


$$|V_{\text{CKM}}| = \begin{pmatrix} 0.97435 \pm 0.00016 & 0.22500 \pm 0.00067 & 0.00369 \pm 0.00011 \\ 0.22486 \pm 0.00067 & 0.97349 \pm 0.00016 & 0.04182^{+0.00085}_{-0.00074} \\ 0.00857^{+0.00020}_{-0.00018} & 0.04110^{+0.00083}_{-0.00072} & 0.999118^{+0.000031}_{-0.000036} \end{pmatrix}$$

Source: PDG 2022

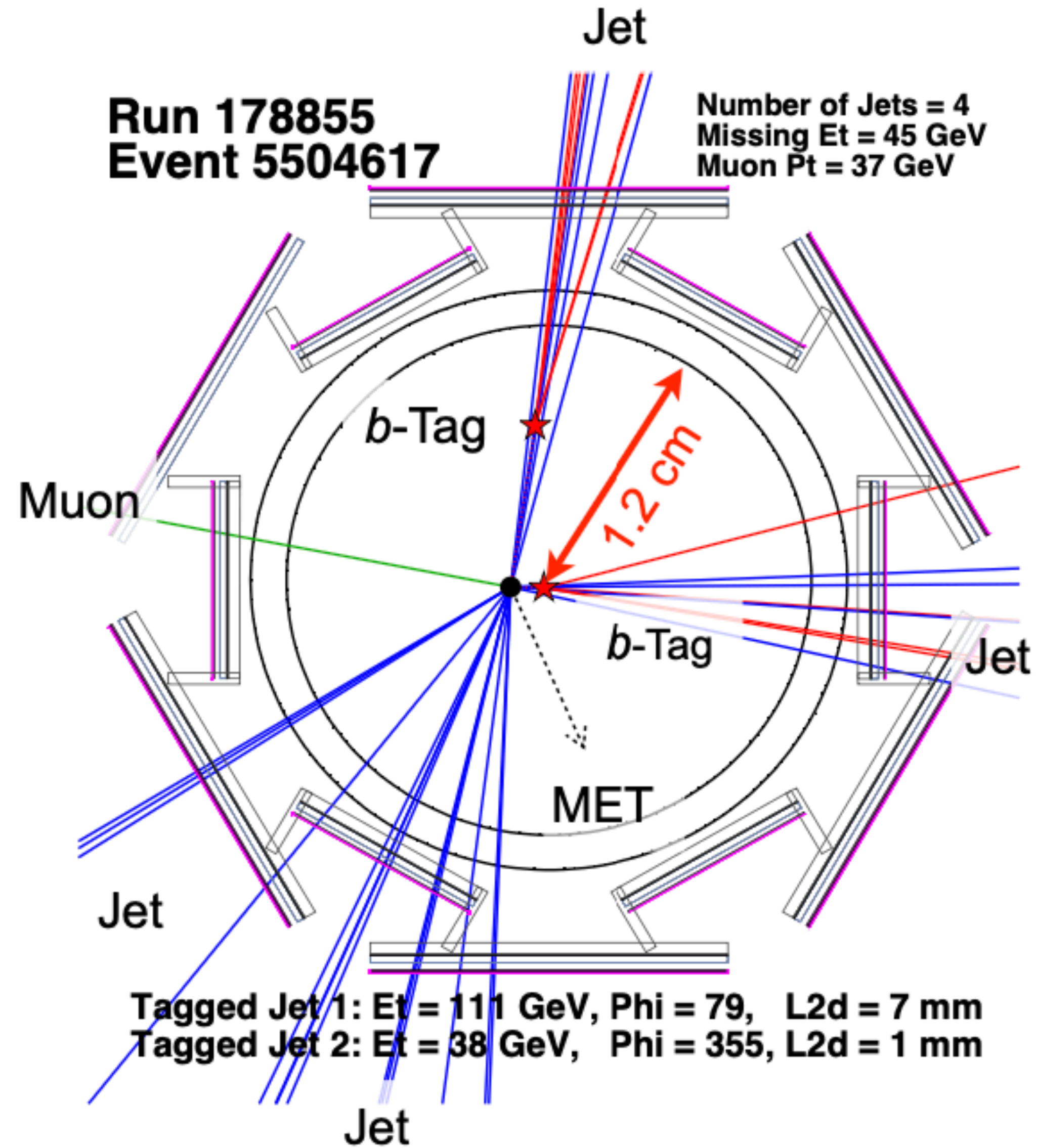
B-tagging

- SM decay $t \rightarrow Wb$: $t\bar{t}$ events have two b quarks $\rightarrow$ b identification is critical
- Lifetime-based b-tagging:
 - $b \rightarrow c$ transition CKM-suppressed:
 - $B^\pm$ proper lifetime: $c\tau = 491 \mu\text{m}$
 - Tracks with large impact parameters
 - Displaced secondary vertex
- Decay-based b-tagging:
 - Semileptonic decays: $B \rightarrow l\nu X$
 - Signature: jets containing non-isolated “soft leptons”



Credit: Nazar Bartosik - http://bartosik.pp.ua/hep_sketches/btagging

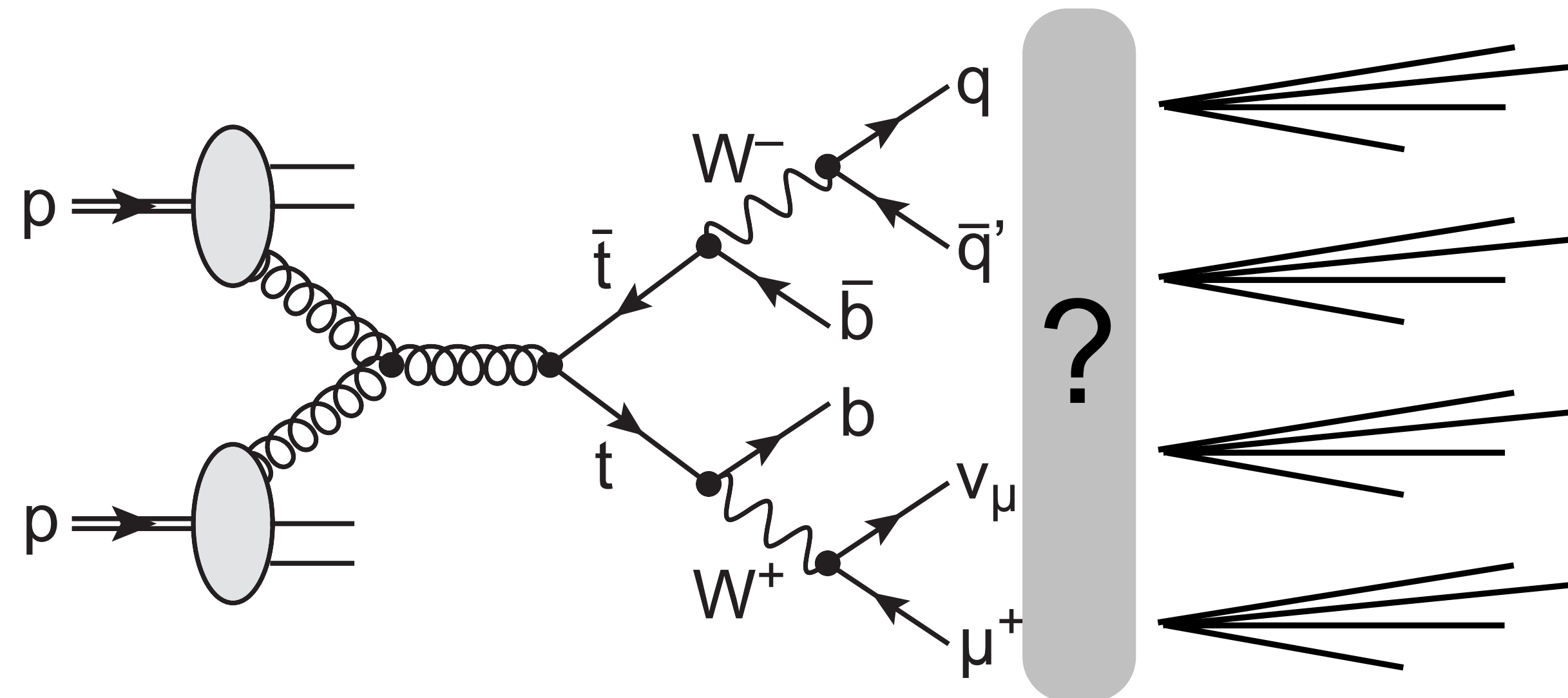
B-tagging



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Top mass from kinematics

- Direct measurement of top-quark mass: top-quark reconstruction → mass from event kinematics
- Example lepton+jets: kinematics overdetermined
 - One unknown: neutrino p_z
 - ≥ 1 possible constraints: e.g. mass of leptonically decaying W
- Challenge: combinatorics of jet-parton assignment (4 jets → 24 combinations) → which combination is the “best”?



- Top-quark mass m_t :
 - Important standard-model parameter, ambiguities in definition (loop corrections)
 - Several complementary methods to determine m_t (e.g. template fit)
 - $m_t \simeq 172.5$ GeV (0.3% precision)
- Further properties of the top quark:
 - Large total decay width (1.3 GeV) → lifetime shorter than typical time scale of hadronization
→ top quark is the only “free” quark
 - Standard model: top quark acquires mass through Yukawa coupling to Higgs boson: only quark with coupling constant of order one
 - V – A decay $t \rightarrow Wb$: source of polarized W bosons (70% longitudinal polarization, 30% left-handed polarization)

What questions do you have?