

Extra Material on Neutral Meson Mixing



Reading material and references

Lecture material based on several textbooks and online lectures/notes. Credits for material and figures include:

Literature

Perkins, Donald H. (2000), Introduction to High Energy Physics.

Griffiths, David J. (2nd edition), Introduction to Elementary Particles.

Stone, Sheldon (2nd edition), B decays.

Online Resources

Belle/BaBar Collaborations, The Physics of the B-Factories. http://arxiv.org/abs/1406.6311

Bona, Marcella (University of London), CP Violation Lecture Notes, http://pprc.qmul.ac.uk/ bona/ulpg/cpv/

Richman, Jeremy D. (UCSB), *Heavy Quark Physics and CP Violation*. http://physics.ucsd.edu/students/courses/winter2010/physics222/references/driver_houches12.pdf

Thomson, Mark (Cambridge University), Particle Physics Lecture Handouts, http://www.hep.phy.cam.ac.uk/ thomson/partIIIparticles/welcome.html

Grossman, Yuval (Cornell University), Just a Taste. Lectures on Flavor Physics, http://www.lepp.cornell.edu/ pt267/files/notes/FlavorNotes.pdf

Kooijman, P. & Tuning, N., CP Violation, https://www.nikhef.nl/ h71/Lectures/2015/ppII-cpviolation-29012015.pdf

Revisit neutral meson mixing

This time we'll also look at B_s mixing (hadron colliders only) And we'll study D^0 mixing, with a focus on the analysis

which first found evidence for D^0 mixing (Belle).

Mixing review (and some extra material)

Mixing is a $|\Delta F| = 2$ process

Process in which particle changes to its anti-particle and vice versa

Possible only in flavored neutral particle–anti-particle systems

Meson M	Flavors	Particle discovered	Mixing discovered	Implication
K^0	$\bar{s}d$	1950 (Caltech)	1956 (Columbia)	m_c
B_d^0	$ar{b}d$	1983 (CESR)	1987 (Desy)	m_t
B_s^0	$ar{b}s$	1992 (LEP)	2006 (Fermilab)	??
D^0	$car{u}$	1976 (SLAC)	2007 (KEK, SLAC)	??

In the Standard Model (SM) the expected $D^0 - \overline{D}^0$ mixing rate is small $\hookrightarrow D^0 - \overline{D}^0$ mixing could be sensitive to contributions of New Physics



In Lecture 2 we developed the time-dependent formalism of meson mixing in the neutral Kaon system.

In Lecture 4 we studied B^0 mixing when we looked at time-dependent CPV in $B^0 \rightarrow J/\psi K_S^0$ decays.

For completeness, lets touch on the remaining 2 systems: B_s mixing, and D^0 mixing.

To do so, lets introduce some dimensionless mixing parameters ¹ which will help us easily quantify the differences in the 4 systems.

¹A very nice derivation of this can be found on page 154 of http://www.lepp.cornell.edu/~pt267/files/notes/FlavorNotes.pdf

Teilchenphysik II

Neutral Meson Mixing

Mixing Phenomenology I - Time evolution

Time evolution of $M^0 - \overline{M}{}^0$ system \hookrightarrow solve time-dependent Schrödinger Eq.

$$i\frac{\partial}{\partial t} \binom{|M^0\rangle}{|\overline{M}^0\rangle} = \mathcal{H}_w \binom{|M^0\rangle}{|\overline{M}^0\rangle} \qquad \mathcal{H}_w = \mathbf{M} - i\frac{\mathbf{\Gamma}}{2}$$

Eigenstates of \mathcal{H}_w are mass eigenstates M_1 and M_2

 $\hookrightarrow \neq$ flavor eigenstates M^0 and \overline{M}^0

$$\left| |M_{1,2}\rangle = p|M^0\rangle \pm q|\overline{M}^0\rangle \right| \qquad p^2 + q^2 = 1$$

 \hookrightarrow with eigenvalues $\lambda_{1,2} = m_{1,2} - i\Gamma_{1,2}/2$

Time evolution of $M^0 - \overline{M}{}^0$ system

$$\begin{aligned} |M^{0}(t)\rangle &= \frac{1}{2} (g_{+}(t)|M^{0}\rangle + \frac{q}{p}g_{-}(t)|\overline{M}^{0}\rangle) \\ |\overline{M}^{0}(t)\rangle &= \frac{1}{2} (\frac{p}{q}g_{-}(t)|M^{0}\rangle + g_{+}(t)|\overline{M}^{0}\rangle) \end{aligned} \qquad g_{\pm}(t) = \left(e^{-i\lambda_{1}t} \pm e^{-i\lambda_{2}t}\right) \\ \end{aligned}$$

Dimensionless mixing parameters

$$x = \frac{m_1 - m_2}{\overline{\Gamma}}$$
 and $y = \frac{\Gamma_1 - \Gamma_2}{2\overline{\Gamma}}$ $\overline{\Gamma} = \frac{\Gamma_1 + \Gamma_2}{2}$ $\overline{m} = \frac{m_1 + m_2}{2}$

Teilchenphysik II

Neutral Meson Mixing

24/2/2021 7/27

Mixing Phenomenology II - Mixing probability

probability to observe an initial M^0 as M^0 or \overline{M}^0 after time t



decay time resolution to resolve oscillations in case of B_s^0 mesons

	111		y	I_{UM}	
time integrated mixing rate	K^0	0.946	0.997	0.994	
	B_d^0	0.776	< 0.01	0.23	
$R_M = \frac{\int_0^\infty \mathcal{P}_{\min}(t)dt}{\int_0^\infty \mathcal{P}_{\max}(t)dt} = \frac{x^2 + y^2}{2 + x^2 - u^2}$	B_s^0	26.1	0.15	0.997	
$J_0 / \operatorname{non-mix}(v) w = 2 + w = g$	D^0	0.01	0.01	10^{-4}	
	1 out of 10^4	D^0 meson	s oscillates l	pefore it de	cavs

 M^0

Teilchenphysik II

Neutral Meson Mixing

24/2/2021 8/27

P.,

B^0 mixing – Argus 1987

ARGUS experiment @ **DORIS**

A Russian-German-United States-Swedish collaboration @ DOppel RIng Speicher

OBSERVATION OF B° - B° MIXING



Theoretically:

$$\frac{N_{B^0 \to B^0}(t) - N_{B^0 \to \overline{B}^0}(t)}{N_{B^0 \to B^0}(t) + N_{B^0 \to \overline{B}^0}(t)} = \cos(\Delta m \Delta t)$$

Experimentally:

Belle, PRD71, 072003 (2005)



You can really see this because: B^0 mixing has same time scale as decay

$$\tau = 1.53 \text{ ps}$$
$$\Delta m = 0.51 \text{ ps}^{-1}$$

Teilchenphysik II

Neutral Meson Mixing

B_s^0 Mixing: 2006

🖷 Health & Medicine 📕 Mind & Brain 📲 Plants & Animals 📕 Earth & Climate 📕 Space & Time 📕 Matter &

Science News

... from universities, journals, and other research organizations

Scientists Precisely Measure Subtle Dance Between Matter And Antimatter

ScienceDaily (Apr. 12, 2006) — Scientists of the CDF collaboration at the Department of Energy's Fermi National Accelerator Laboratory announced the precision measurement of extremely rapid transitions between matter and antimatter. As amazing as it may seem, it has been known for 50 years that very special species of subatomic particles can make spontaneous transitions between matter and antimatter. In this exciting new result, CDF physicists measured the rate of the matterantimatter transitions for the Bs (pronounced "B sub s") meson, which consists of the heavy bottom quark bound by the strong nuclear interaction to a strange anti-quark, a staggering rate that challenges the imagination - 3 trillion times per second.

See Also:

Matter & Energy

- Quantum Physics
- Physics
- Nuclear Energy
- Energy Policy

Dr. Raymond Orbach, Director of the DOE Office of Science, congratulated the CDF collaboration on "this important and fascinating new result" from the experiment.

"Exploration of the anti-world's mysteries is a crucial step towards



The figure shows the CDF measurement of the Bs oscillation frequency at 28 trillion times per second. The analysis is designed such that possible oscillation frequencies have an amplitude consistent with 10 while those not present in the data will have an amplitude consistent with zero. Image courtesy CDF collaboration. (Image courtesy of DOE/Fermi National Accelerator Laboratory)

Ads by Google

B_s^0 Mixing: 2006

CDF at Tevatron (USA)



- Need:
 - B flavour at decay
 - Reconstruct decay mode
 - Flavour at production
 - Same- or opposite-side flavour tag
 - Decay proper time
 - vertexing

Perform extraction of oscillation frequency by introducing an ad hoc amplitude coefficient *A*, then perform frequency-domain analysis

- Amplitude should reach unity in presence of signal, and be zero elsewhere



 $P(t) \sim (1 \pm \mathcal{A}D \cos \Delta m_s t)$

CDF and D0 both reported evidence for mixing in spring 2006

CDF: Δm_s = 17.33 +0.42 -0.21 (stat) +- 0.07 (syst) ps⁻¹



Reconstruction of D^0 mesons

Reconstruction of D^0 mesons

Reconstruct tracks of long lived particles $(e^-, \mu^-, \pi^{\pm}, K^{\pm}, K^0_L, p, \gamma)$: measure their momenta $\vec{p_i}$ or energies E_i identify them (assign mass m_i) make combinations: $K^0_S \to \pi^+\pi^-, \phi \to K^+K^-, D^0 \to \phi K^0_S$



Decay time distribution



Production vertex

Proper decay time

$$t = \frac{m_{D^0}}{p_{D^0}} (\vec{r}_{\text{dec}} - \vec{r}_{\text{IP}}) \cdot \frac{\vec{p}_{D^0}}{p_{D^0}}$$

Distribution of proper decay time

$$\mathcal{F}(t) = \int Exp[-t'/\tau] \cdot R(t-t')dt'$$



Teilchenphysik II

Neutral Meson Mixing

Mixing in semileptonic decays $D^0 o K^{(*)-}\ell^+
u_\ell$

Mixing in semileptonic decays $D^0 \to K^{(*)-}\ell^+\nu_\ell$

U. Bitenc *et al.* [Belle Collaboration], PRD77, 112003 (2008). [$\mathcal{L} = 492 \text{ fb}^{-1}$] Wrong sign (WS) charge combination accessible only via mixing



24/2/2021 19/27

Mixing in semileptonic decays $D^0 \to K^{(*)-}\ell^+\nu_{\ell}$



24/2/2021 20/27

 $0.013 \pm 0.022 \pm 0.020$ %

 $(1.3 \pm 2.2 \pm 2.0) \times 10^{-4}$

0.110 + 0.300 %

0.004 +0.070 %

0.160 + 0.290 + 0.290 %

 6.1×10^{-4} @ 90% C.L.

Mixing and CPV in $D^0 \to K^+ K^-$, $\pi^+ \pi^-$ decays

M. Staric *et al.* [Belle Collaboration], PRL98, 211803 (2007). $[\mathcal{L} = 540 \text{ fb}^{-1}]$

Measurement of lifetime difference between $D^0 \to K^- \pi^+$ (*CP*-mixed) and $D^0 \to K^+ K^-$, $\pi^+ \pi^-$ (*CP*-odd) decays

Conserved CP symmetry

$$\hookrightarrow \frac{dN(D^0 \to f_{CP})}{dt} \propto e^{-(1+y_{CP})\Gamma t}$$

$$\hookrightarrow \frac{dN(D^0 \to f)}{dt} \propto e^{-\Gamma t}$$

$$y_{CP} = rac{ au(f)}{ au(f_{CP})} - 1$$

$$y_{CP} = y$$

 $\begin{array}{l} CP \text{ Violation} \\ \hookrightarrow \tau(D^0) \neq \tau(\overline{D}^0) \\ \hookrightarrow CP \text{ violating parameter} \end{array}$

$$A_{\Gamma} = \frac{\tau(\overline{D}{}^{0} \rightarrow f_{CP}) - \tau(D^{0} \rightarrow f_{CP})}{\tau(\overline{D}{}^{0} \rightarrow f_{CP}) + \tau(D^{0} \rightarrow f_{CP})}$$
$$y_{CP} = y \cos \phi - \frac{1}{2} A_{M} x \sin \phi \qquad A_{\Gamma} = \frac{1}{2} A_{M} y \cos \phi - x \sin \phi$$

Mixing and CPV in $D^0 \to K^+ K^-$, $\pi^+ \pi^-$ decays



Mixing and CPV in $D^0 \rightarrow K^+ K^-$, $\pi^+ \pi^-$ decays

First evidence for $D^0 - \overline{D}^0$ mixing!



No evidence for CPV.

Time integrated CPV in $D^0 \to K^+ K^-, \pi^+ \pi^-$ decays

M. Staric *et al.* [Belle Collaboration], PLB670, 190 (2008). $[\mathcal{L} = 540 \text{ fb}^{-1}]$

Measure CP-Violating asymmetry

$$\hookrightarrow \qquad A_{CP} = \frac{\mathcal{B}(D^0 \to f) - \mathcal{B}(\bar{D}^0 \to \bar{f})}{\mathcal{B}(D^0 \to f) + \mathcal{B}(\bar{D}^0 \to \bar{f})}, \quad f = K^+ K^- \text{ or } \pi^+ \pi^-$$

 $\hookrightarrow \qquad A_{CP} = a_f^d + a_f^m + a_f^i \text{ (direct + indirect CPV contributions)}$

Measured asymmetry:

$$N_{D^0}^{\rm reco} = N_{D^{*+}}^{\rm prod} \cdot \mathcal{B}(D^{*+} \to D^0 \pi^+) \cdot \mathcal{B}(D^0 \to f) \cdot \varepsilon_f \cdot \varepsilon_{\pi_S^+}$$

Contributions to measured asymmetry:

$$\hookrightarrow \left| A^{ ext{meas}} = A^{D^{*+}}_{FB} + A^f_{CP} + A^f_{\epsilon} + A^{\pi_S}_{\epsilon}
ight|$$

 A_{FB}^{*+} : production asymmetry (anti-symmetric function of $cos\theta^*$)

 A_{CP}^f : CP asymmetry

 $\begin{array}{l} \pmb{A_{\epsilon}^{f}} \colon D^{0} \to f \text{ efficiency asymmetry} \\ (\text{zero for } K^{+}K^{-} \text{ or } \pi^{+}\pi^{-}) \end{array}$

Time integrated CPV in $D^0 \to K^+ K^-, \pi^+ \pi^-$ decays

$$A_{\text{corr}}^{\text{reco}}(\cos\theta^*) = \frac{N(D^0) - N(\bar{D}^0)}{N(D^0) + N(\bar{D}^0)}$$
$$= A_{FB}^{D^{*+}} + A_{CP}^f$$

$$A_{CP} = \frac{A_{\text{corr}}^{\text{reco}}(\cos\theta^*) + A_{\text{corr}}^{\text{reco}}(-\cos\theta^*)}{2}$$
$$A_{FB} = \frac{A_{\text{corr}}^{\text{reco}}(\cos\theta^*) - A_{\text{corr}}^{\text{reco}}(-\cos\theta^*)}{2}$$





BaBar

$A_{CP}^{KK} = ($	$0.00 \pm 0.34(\text{stat}) \pm 0.13(\text{syst}))\%$
$A_{CP}^{\pi\pi} = (-$	$-0.24 \pm 0.52(\text{stat}) \pm 0.22(\text{syst}))\%$

BaBar, PRL100, 061803 (2008)

Consistent with no CPV!

SM expectations: $A_{CP} \sim \mathcal{O}(10^{-5} - 10^{-4})$ PRD51,3478(1995); RNCIB,26N7,11(2003)

Impact – Constraints on NP models from mixing

E. Golowich et al., PRD76,095009

Constraints on new physics models from $D^0 - \overline{D}{}^0$ complementary to those obtained in B and K sector \hookrightarrow FCNC transitions with *down-like* quarks in charm sector (unique feature)

21 NP models considered \rightarrow 17 with useful constraints





Impact – Constraints on NP models from mixing

E. Golowich $et~al.,~\mathrm{PRD76,095009}$

Constraints on new physics models from $D^0 - \overline{D}{}^0$ complementary to those obtained in *B* and *K* sector \hookrightarrow FCNC transitions with *down-like* quarks in charm sector (unique feature)

21 NP models considered \rightarrow 17 with useful constraints

Example: quark b' from 4^{th} generation



$$\label{eq:Vcb'} \begin{split} |V_{ub'}V_{cb'}| < 0.002 \\ \text{order of magnitude stronger constraint} \\ \text{as from CKM unitarity} \end{split}$$

Providing complementary and improved constraints!