

Vorlesung: Teilchenphysik I (Particle Physics I)

Particle Accelerators

Günter Quast

Fakultät für Physik Institut für Experimentelle Kernphysik

WS 20/21



- 1. History
- 2. Basics principles
- 3. Detectors and Accelerators
 - 1. Interaction of particles with matter
 - 2. Simulation of particle interactions with Monte Carlo
 - 3. Detector Systems
 - 4. Accelerators

Literature

K. Wille, *Physik der Teilchenbeschleuniger und Synchrotronstrahlungsquellen*, Springer Vieweg

K. Wille, *The Physics of Particle Accelerators*, Oxford University Press, 2000









Motivation for Particle Accelerators

Nature delivers

ultra-high energy particles:

- Ultra-high energies
- complicated detection medium (atmosphere)
- Iarge-area detectors required



Particle accelerators deliver high-energetic particles under laboratory conditions:

- Perfect control of initial conditions
- events originate in one place
- compact, tailored detector designs



- Production of new, heavy particles: maximum mass = centre-of-mass energy M = E_{CMS} /c²
- resolution of small structures: De-Broglie wave length of beam particles

$$\lambda = \frac{h}{p} = \frac{2\pi\hbar c}{pc} \rightarrow \lambda \,[\text{fm}] \approx \frac{1.24}{p[\text{GeV}]} \qquad \qquad \begin{array}{c} p = 1 \,\text{GeV} \rightarrow \lambda = 1.24 \cdot 10^{-15} \,\text{m} \\ p = 1 \,\text{TeV} \rightarrow \lambda = 1.24 \cdot 10^{-18} \,\text{m} \end{array}$$

Basic Principle

The Lorentz force
$$ec{F}_{ extsf{L}} = q(ec{E} + ec{v} imes ec{B})$$

Acceleration of charged partiles by electrical field(s)
 Deflection of charged particles by magnetic fields

Energy gain only from electrical fields:

$$\Delta E = \int\limits_{s_0}^{s_0+d} ec{\mathcal{F}}_{\mathsf{L}} \cdot \mathsf{d}ec{s} = q \int\limits_{s_0}^{s_0+d} ec{\mathcal{E}} \cdot \mathsf{d}ec{s} = q U$$

Acceleration voltage of 1 V corresponds to an energy gain of 1 eV

An Accelerator is a machine providing arrangements of electrical and magnetic fields to accelerate, store and focus charged particles.



Historical Accelerators

Historical Accelerators: electrostatic

Cockcroft-Walton

1930s; up to 4 MV, µs pulses of up to 100 mA





source: lecture on Accelerator Physics by Anke-Susanne Müller



Cockroft and Waltons elektrostatischer Beschleuniger mit Cockroft "im Labor"

http://www.accelerators-for-society.org/about-accelerators/ timeliner/img/1931.png

The Betatron

Wideröe's "ray transformer"



E.J.N. Wilson, An Introduction to Particle Accelerators, Oxford University Press, 2001

Betatron (2)

Wideröe's "ray transformer": exploiting

$$\mathbf{g} \quad \oint \vec{E} \cdot d\vec{r} = -\int \int \frac{d}{dt} \vec{B} \cdot d\vec{a}$$



Betatrons are still widely in use today (medical applications)

Very compact systems example: 30 MeV with 0.1 m radius



http://www.jme.co.uk/JME-Products-Betatron.aspx

http://commons.wikimedia.org/wiki/File:Betatron_6MeV_(1942).jpg

Linear Accelerdator ...

... the initial stage of every modern accelerator



- particles from source are acceletated in potention of first drift tube
- voltage is inverted while particle is inside the first tube
- particles leave first drift tube and are accelerated towards the scond tube
- lengths of tubes and distance between them increase, because speed of (low-energy) particles increases

Linac Structure



CERN Micorcosm

Linear Accelerator - principle





Energy after passing drift tube *i*

$$E_i = iqU_0\sin(\Psi_s)$$

- r = x kHF(x) is phase of particle kHF is the wave number of high voltage
- U₀ is maximum voltage of HF generator
- $-\Psi_{s}$ is phase of particle relative to HV

Only particles with phase $\Psi \approx \Psi_s$ can be accelerated

 \rightarrow leads to **particle bunches**

The (so far) largest Linear Accelerator





http://erlangen.physicsmasterclasses.org/exp_forsc/exp_forsc_11.html

operated on the Z resonance, precision electroweak physics with polarized beams

Circular Accelerators: the Cyclotron

(M.S. Livingston, E.O. Laawrence, 1930)

- Strong magnetic field bends path of particles on circular orbit

 repeated acceleration within same structure

 Design: D-shaped poles
 - ightarrow particle on spiral trajectory

Berkeley: 184-Zoll-Synchrozyklotron





Still used today for *protons/ions* beams of medium energy

- Nuclear physics
- Cancer therapy
- Material science (e.g. ZAG
 - Zyklotron AG, KIT Campus Nord)

Cyclotron Frequency

Ansatz: Lorentz force $\vec{F}_L(\vec{E}=0) = centripetal$ force \vec{F}_Z

Non-relativistic approximation:

$$qvB = mrac{v^2}{r} \quad \Rightarrow \quad \omega = rac{v}{r} = rac{qB}{m}$$

- Characteristic *cyclotron frequency* (independent of momentum)
- Typcial values for protons and B = 2 T: $\omega = 1.9 \cdot 10^8 \text{ s}^{-1}$ $\rightarrow \nu = 30.5 \text{ MHz}$ (radio frequency)
- Relativistic calculation:

$$\vec{F}_L = rac{\mathrm{d}\vec{p}}{\mathrm{d}t} = rac{\mathrm{d}}{\mathrm{d}t}(\gamma m \vec{v}) \quad \Rightarrow \quad \omega = rac{qB}{\gamma m}$$

Curvature radius R (cf. tracking): $R = \frac{p[\text{GeV}]}{0.3gB[\text{T}]}$

- Typical values R = 0.5 m, B = 0.5 T: maximum momentum p = 75 MeV
- Maximum energy limited by size (and strength) of magnet, typical sizes up to few 10 MeV

Weak Focusing in homogeneous B Field

Particles of the same energy have the same curvature radius in an homogeneous B field

→ particle trajectories with slightly displaced positions cross twice per turn



"weak focusing"

used in cyclotrons and early synchtrotrons

Accelerator Physics

- a brief overview -

Circular Accelerators: the Synchrotron

new idea: increase magnetic field syncronous to particle momentum (M. Oliphant, 1943)

keep beam radius ~constant, magnetic field only in beam tube





Circular Accelerators: the modern Synchrotron

breakthrough discovery: Phase Focussing (Veksler 1944, McMillan 1945)

Orbit length *L* in a circular accelerator is given by RF frequency f_{RF}:

L is a multiple *h* of the "RF wavelength" $\lambda_{RF} = c / f_{RF}$

- h is called "harmonic number"



Principle

(for relativistic particles) :

- fast particles arrive later
 → receive less acceleration
- slow particles arrive eariler \rightarrow recive more acceleration

Phase of particles oscillates around optimal phase, the **"stabe phase" Ψ**s

"Synchrotron Oscillation"

Phase of particles adjusts itself to compensate energy losses → Phase Focusing

also: Changes of beam energy by inceasing the magnic bending field

Accelerating RF Cavities

- Acceleration of particles by alternating electrical field in a resonating cavity
- enforces and retains bunch structure of beam
- radio frequency @ LHC: 400 MHz



RF power generated in high-power klystron (by electron-density modulation) induced into cavities via RF wave guides

Synchrotron: strong focusing

another important ingredient: use of **quadrupole magnets** to **focus beam** (Chrostofilos 1950, Courant, Livingston & Synder 1952)



Dipol B field

constant field across aperture; provides bending field

additional **sextupole** and **octupole** magnets are needed to control beam optics



Strong Focussing: principle

- Series of quadrupole magnets with *alternating field gradients* in x, y
- Second magnet in *focal point* of first, and so on
- \rightarrow beam is focussed in x and y





optical analogy

"strong focusing" in modern synchrotrons

Modern Synchrotron

Alternating-gradient principle reduces beam size and increases energy aperture

beam optics charachterized by "Momentum Compaction Factor" α_c





Components of a synchrotron

- deflection magnets (dipoles)
- focussing magnets (quadrupoles, sextupoles and octupolse)
- injection magnets (pulsed)
- extraction magnets (pulsed)
- RF acceleration cavities
- vacuum system
- beam diagnostics
- control system
- powerful power supplies

Transverse Beam Optics

Ensemble of particles, *not* all on ideal circular orbit

- (Co-moving) coordinate system:
 - beam direction z
 - transverse deviation from ideal trajectory x, y
- Expansion of particle trajectory for *small deviations*



Effect of *Lorentz force* on particles in magnetic field $\vec{B} = (0, B_y, 0)$

- Inverse radius of curvature: $\frac{1}{R(x,y,z)} = \frac{q}{p}B_y(x,y,z)$
- Beam dimensions $\ll R \rightarrow$ expansion of B_y in x (analogue for y)

$$\frac{q}{p}B_{y}(x,y,z) = \frac{q}{p}B_{y}(0,y,z) + \frac{q}{p}\frac{\partial B_{y}(0,y,z)}{\partial x} \cdot x + \frac{1}{2}\frac{q}{p}\frac{\partial^{2}B_{y}(0,y,z)}{\partial x^{2}} \cdot x^{2} + \dots$$
$$= \frac{1}{R} + k \cdot x + \frac{1}{2}m \cdot x^{2} + \dots$$
dipole quadrupole sextupole

Linear Transverse Beam Optics

Linear transverse beam optics

$$\frac{q}{p}B_{y}(x,y,z) = \frac{q}{p}B_{y}(0,y,z) + \frac{q}{p}\frac{\partial B_{y}(0,y,z)}{\partial x} \cdot x + \frac{1}{2}\frac{q}{p}\frac{\partial^{2}B_{y}(0,y,z)}{\partial x^{2}} \cdot x^{2} + \dots$$
$$= \frac{1}{R} + k \cdot x + \frac{1}{2}m \cdot x^{2} + \dots$$

- Terminate after linear term: deflecting force *constant* (dipole field) or *linear* with distance x from design trajectory (quadrupole field)
- Realistic accelerators: corrections by higher multipoles

Equation of motion in x in co-moving coordinate system

(assumption: storage ring, no change of momentum)

$$x''(s) + \left(\frac{1}{R^2(s)} - k(s)\right)x(s) = 0$$
 differential equation of Hill's type

 R(s), k(s): periodic functions in distance s along trajectory reflecting "magnetic lattice" of the machine

Solution:

$$x(s) = \sqrt{\epsilon\beta(s)} \cos [\Psi(s) + \phi]^{-1}$$

β(s): betatron function
ε: emmitance
Ψ(s): phase advance

Describes oscillation around ieal orbit ("betatron oscillations")

Betatron Oscillation



Betraton function $\beta(s)$

(also: 'beta function', 'amplitude function')

- Quantifies deviation from ideal orbit
- Depends on *beam focus* along s
- Important characteristic quantity:
 ^{3*}
 value of
 ³
 function at interaction
 point

value of β^* during LHC Run 2: 30 cm

Phase Space and Emmittance

Phase space of beam given

- by x(s) and x'(s) ($\propto p$)
- Solution to Hill's equation: *ellipse* in phase space
- Emittance ϵ proportional to area of ellipse: $\mathbf{A} = \pi \epsilon$

Liouville's theorem: particle density in phase space is constant for conservative forces

- Typically (approximately) the case in storage rings
- During fill, phase space *deformed* but *density conserved*



Emmittance

- Interpretation: quantifies spread in location and momentum of beam particles within ensemble (storage ring: ensemble = bunch)
- $\epsilon \propto 1/p$: use *normalised emittance* $\epsilon_n = \gamma \epsilon$ (independent of beam energy)
- Example LHC 2016: $\epsilon_n = 2.6 \,\mu\text{m} \rightarrow \sqrt{\epsilon\beta^*} = 12.3 \,\mu\text{m}$ (cf. https://lpc.web.cern.ch/lumi2.html)

Luminosity of a collider

In an accelerator with counter-rotating bunches of particles, the luminosity is given by the bunch parameters:

$$\mathcal{L} = f \cdot n_b \cdot \frac{N_1 \cdot N_2}{4\pi\sigma_x\sigma_y}$$



- N1, N2: number of particles per bunch
- $-\sigma_x$, σ_y : bunch dimensions in *x* and *y* directions
- f : collision frequency
- nb: numer of bunches

 \mathcal{L} , the **instantaneous luminosity**, is related to the **interaction rate** of a process with cross section σ by $\frac{dN}{dt} = \mathcal{L} \cdot \sigma$

The **integrated luminosity**, $L_{int} =: L = \int \mathcal{L} dt$ is related to the total number of observed events in a data set

unit: $[L] = cm^{-2}$, convenietly also $1/fb = 10^{39} cm^{-2}$

interpretation: a dataset of 1 fb⁻¹ contains (on average) one event of a process with cross section 1 fb

Luminosity: Emmitance and Beta function

Impact of emittance on *luminosity*

• Gaussian beam profile: betatron function of particles that are 1 standard deviation σ off the ideal orbit

$$\sigma(s) = \sqrt{\epsilon eta(s)} \quad o \quad eta(s) = rac{\sigma^2(s)}{\epsilon}$$

Strong quadrupoles near the interaction points locally reduce β ; - β^* is value of the beta function at the interaction point

can rewrite formula for the luminosity of an accelerator in terms of beam parameters :

$$\mathcal{L} = f \cdot n_b \cdot \frac{N_1 \cdot N_2}{4\pi \sqrt{\epsilon_x \beta_x^* \epsilon_y \beta_y^*}}$$

Luminosity: typical values

| | peak \mathcal{L} (cm ⁻² s ⁻¹) | L _{in} (fb ⁻¹) |
|-------------------------|--|-------------------------------------|
| LEP II | 1 · 10 ³² | 3 |
| KEKB / Belle | $2\cdot10^{34}$ | 710 |
| Tevatron Run-II | $4 \cdot 10^{32}$ | 12 |
| LHC Run-I (2010–2012) | $7.7\cdot10^{33}$ | 25 |
| LHC Run-II (since 2015) | $2\cdot 10^{34}$ | 122 |

CMS Integrated Luminosity Delivered, pp



Synchrotron Radiation

Lorentz-Transformation **QED:** accelerated charges emit photons \rightarrow particles kept on a circle Moving frame Lab frame in a synchrotron of electron emit "synchrotron radiation" Acceleration very desired effect in eleration synchrotron light sources 90° - constant energy loss of beam particles limits maximum energy of a circular electron accelerator ! $\pm \frac{1}{2}$ opening angle

desy.de

Energy loss per turn: $\Delta E = 2\pi \frac{R}{c}P$ scales with R^{-2} and m^{-4}

- Electrons at LEP (100 GeV beam energy): $\Delta E \approx 3$ GeV
- Protons at LHC (6.5 TeV beam energy): $\Delta E \approx 2 \text{ keV}$

Optical Resonances and Tune

Phase advance per turn: $\Delta \Psi = \Psi(s + L) - \Psi(s)$

Inserting in Hill's equation and integrating over one turn

$$\rightarrow \text{``tune''} \quad Q = \frac{\Delta \Psi}{2\pi} = \frac{1}{2\pi} \oint \frac{\mathrm{d}s}{\beta(s)}$$

tune is the number of oscillations per turn

- betatron tune Q_{x,y}
- analog: synchroton tune Q_s: number of logitudinal oscillations (or oscillations between max. and min. energy)

Danger: in case of integer tunes, m Q_x +n Q_y, perturbations hit beam particles always at the same phase;
→ resonant build-up → beam loss !

Optical Resonances and Tune



World Map of Accelerators

Karlsruher Institut für Technologie



e+e- Colliders

| Accelerator (Lab) | Operation | Type: Particles | Beam Energy (GeV) |
|-------------------|------------|------------------------------|----------------------|
| LEP (CERN) | 1989–2000 | Storage ring: e^+e^- | 45–104.6 |
| SLC (SLAC) | 1989–1998 | Linear accelerator: e^+e^- | 50 |
| KEKB (KEK) | 1999–2010 | Storage ring: e^+e^- | $e^-: 8.0, e^+: 3.5$ |
| PEP-II (SLAC) | 1999–2008 | Storage ring: e^+e^- | $e^-: 9.0, e^+: 3.1$ |
| Super-KEKB (KEK) | since 2017 | Storage ring: e^+e^- | $e^-: 7.0, e^+: 4.0$ |
| ILC (Japan?) | ? | Linear accelerator: e^+e^- | 250–500 |
| CEPC (China) | ?? | Storage ring: e^+e^- | 120 |
| CLIC (?) | ??? | Linear accelerator: e^+e^- | 1500 |
| FCC-ee (CERN) | ??? | Storage ring: e^+e^- | 45–175 |

Further at lower energies: VEPP (Novosibirsk), BEPC (Bejing), DAΦNE (Frascati), CESR (Cornell)

pdg.lbl.gov

Hadron Colliders

| Accelerator (Lab) | Operation | Type: Particles | Beam Energy (GeV) |
|--|--------------------------------------|---|---|
| HERA (DESY) Tevatron (Fermilab) RHIC (BNL) | 1992–2007 1987–2011 since 2000 | Storage ring: $e^{\pm}p$ Storage ring: $par{p}$ Storage ring: pp , heavy ions | <i>e</i> [±] : 30, <i>p</i> : 920 900–980 100/proton |
| LHC Run-I (CERN) | 2009–2012 | Storage ring: <i>pp</i> , heavy ions | 2010/11: 3500 2012: 4000 (2510/proton) |
| LHC Run-II (CERN) | since 2015 | Storage ring: <i>pp</i> , heavy ions | 6500 (2760/proton) |
| HL-LHC (CERN) FCC-hh (CERN) | 2026–2035 ??? | Storage ring: <i>pp</i> , heavy ions Storage ring: <i>pp</i> | 7000 50 000 |

pdg.lbl.gov

Energy increase with time – "Livingston Plot"

Empirically: doubling of energy every 6 years

1000

100

En (Mev)

10

IIIIII

1930

1940

1950

a

original plot current plot (M.S. Livingston, 1954) 10 TeV Hadron Colliders e*e* Colliders LHC (CERN) 1 TeV 0 NLC TEVATRON Constituent Center-of-Mass Energy (Fermilab) symmetrymagazine.org LEP II SPPS (CERN) LEP (CERN) SLC (SLAC) 100 GeV RISTAN (KEK) PETRA PEP (DESY) (SLAC) Cyclotron CESR (Cornell) ISR (CERN) 10 GeV VEPP IV (Novosibirsk) Josof Inco SPEAR II Electrostolic SPEAR DORIS VEPP III (SLAC) (DESY) (Novosibirsk) ADONE (Italy) 1 GeV **PRIN-STAN VEPP II** ACO (Stanford) (Novosibirsk) (France) 196 0 197 0 198 0 199 0 200 0 2010 Year of First Physics

ansruher institut für rechnologie

The CERN accelerator complex



Magnet Technologies

Normal conducting magnets

- Water-cooled copper coils with iron joke
- Limitation: magnetisation of iron saturates at → B ≤ 2 T

Superconducting magnets

- Charge only at surface: coils from NbTi filaments (7 µm) in copper matrix
- Operation below critical temperature: cooling with *liquid Helium at 4 K* (LHC: super-fluid He at 1.9 K)
- Limitation: collapse of superconductivity at *critical current* ('quench') → *B* ≤ 10 T for NbTi





Full cross-section



Rutherford cables: cross-section



View of the flat side, with one end etched to show the Nb-Ti filaments

cerncourier.com

LHC Dipoles

- Identical particles in each beam (e.g. pp) in opposite direction
 - Two beam pipes
 - Magnetic field lines in opposite direction



LHC Dipoles



LHC Layout

- LHC: 8 arcs and 8 straight sections ('insertions')
- Arcs (2.45 km)
 - 23 arc 'cells' with FODO structure (main dipoles, quadrupoles, other multipoles)



- Straight Sections (528 m)
 - Experiments
 - Beam injection
 - RF acceleration
 - Beam dump
- Interaction points: "low-β triplets" with *best-possible focusing*





SuperKEKB acce – an asymmetric B factory

SuperKEKB is an upgrade of

the former $\ensuremath{\mathsf{KEKB}}$ accelerator

- an example of an (asymmetric) electron-positron collider
- two rings, one for 4 GeV positrons and one for 7 GeV electrons
- centre-of-mass system at Y(4s) resonance is boosted to increase resolution on displaced vertices from B hadron decays
- aiming at a luminosity of 8 x 10³⁵ cm⁻¹ s⁻¹



Future accelerators

Future Accelerators

Discovery of new phenomena is possible via two roads:

- 1. higher energy to directly produce new particles Requires accelerators with higher energy and/or higher luminosity
 - luminosity increase of the LHC (High-Luminosity LHC, approved)
 - an new proton accelerator with a tunnel of 80 100km length

2. higher precision of measurements

Requires better control of initial conditions and a "clean" environment

- electron-positron collisions at energies of 500 GeV 1 TeV losses due to synchrotron radiation require either
 - a very large ring or
 - a linear collider
- a myon collider (?) very challenging

Higgs Signatures in e+e-



Simulated Higgs-boson signals with different decay final states for 240 GeV electron–positron collisions envisaged at CEPC, using a PFA-oriented detector design.

Ideas for a Future Circular Collider @ CERN





Large radius needed to keep particles in the ring:

$$\rho$$
 [m] = 3.336 $\frac{p$ [GeV/c]}{B [T]

Options:

- electron positron collisions @ 90 350 GeV (Z and Higgs Factory)
- hadron hadron collisions @ ~100 TeV
- electron/positron hadron collisions (?)

FCC: technological challenges





FCC needs 4 x more dipole magnets with twice the field of the LHC

High temperature superconductors for even higher beam energies and as an option for power distribution

FCC: more challenges

Energy in the LHC

■ Magnets: 10 GJ = dir5us A380 mit 700 km/h

Beam: 362 MJ

= 120 kg TNT oder 20 kg Schweizer Keise



CERN protons at 450 GeV V. Kain, H. Burkhardt, CERN

The International Linear Collider (ILC)



- a "mature" concept:
 - superconducting cavities already in use at DESY (European XFEL)
 - technical design report exists
 - experimental collaborations and detector proposals exist

possible place: Japan, but decision differed in March 2019

CLIC (CERN Linear Collider) @ 3 TeV

A novel concept for particle acceleration:

Cavities driven by a particle beam

drive beam 100 A, 239 ns 2.38 GeV - 240 MeV





Fig. 2.6: Principle of the two-beam scheme: The beam power in the Drive Beam is converted to RF power in PETS, each feeding two accelerating structures in the Main Beam running parallel at a distance of 60 cm.

CLIC CONCEPTUAL DESIGN REPORT. CERN-2012-007

CLIC (CERN Linear Collider) @ 3 TeV



A new Accelerator Complex in China ?

China's bid for

a circular electron– positron collider

and – later –

a proton-proton machine

in a ~100 km tunnel



Several sites in China under study for a possible 100 km-circumference collider

New concepts for acceleration

Laser Wake Field Accelleration in a plasma

VOLUME 43, NUMBER 4

PHYSICAL REVIEW LETTERS

23 JULY 1979

Laser Electron Accelerator

T. Tajima and J. M. Dawson Department of Physics, University of California, Los Angeles, California 90024 (Received 9 March 1979)

An intense electromagnetic pulse can create a weak of plasma oscillations through the action of the nonlinear ponderomotive force. Electrons trapped in the wake can be accelerated to high energy. Existing glass lasers of power density 10^{18} W/cm² shone on plasmas of densities 10^{18} cm⁻³ can yield gigaelectronvolts of electron energy per centimeter of acceleration distance. This acceleration mechanism is demonstrated through computer simulation. Applications to accelerators and pulsers are examined.

- Laser pulse generates plasma wave by ponderomotive force ∝∇l(r)
- Charge separation → longitudinal electric fields
- Acceleration gradients of GeV cm⁻¹ are achieved



Activities @ KIT









Contact: Prof. Dr. Anke-Susanne Müller